

Simulations in Radiation Therapy and medical physics

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Planning et objectifs

- DQPRM 2^{ème} année – promo 2024-2026
- Simulations Monte-Carlo en radiothérapie (TC 1.5)
- 28 Janvier 2025
 - 10h – 12h: cours, salle A1
 - 13h30 – 16h30: TD salle info (146-148)
- 29 Janvier 2025
 - 9h – 12h et 13h30 – 16h30 : TD salle info (146-148)
- Introduction GATE et prise en main

DQPRM 2025 - PDF

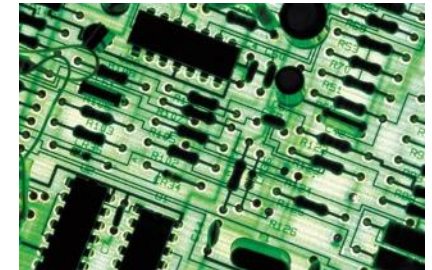


<https://128.pl/ONclf>



Simulations in Medical Physics

- What ? Numerical model, computer
- Why ? To predict, to analyse, to reduce the nb of measurements
- When ? 100% treatment, 100% design imaging systems
- Who ? MedPhys in clinic, industrial, research
- Where ? Hospital, labs, industry ; RT and NM ; maybe Radiology
- How ? Design simulation. Run. Analyse. Redo

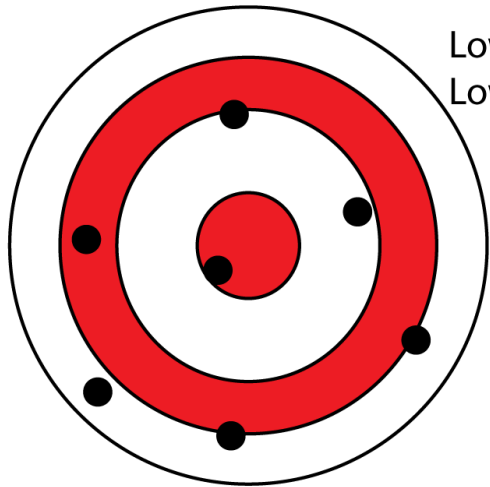


Simulations

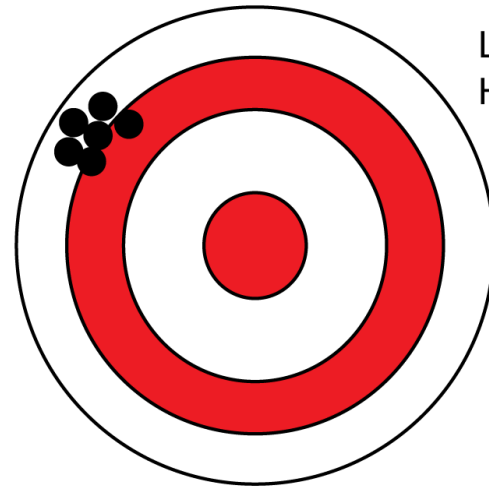
- Analytical approach (determinist)
 - Monte-Carlo approach (stochastic)
 - Hybrid approach
-
- Validation : compare to measurements
 - Calibration: commissioning, parameters
 - Parameters: tradeoff precision-speed
 - Uncertainties: precision, accuracy



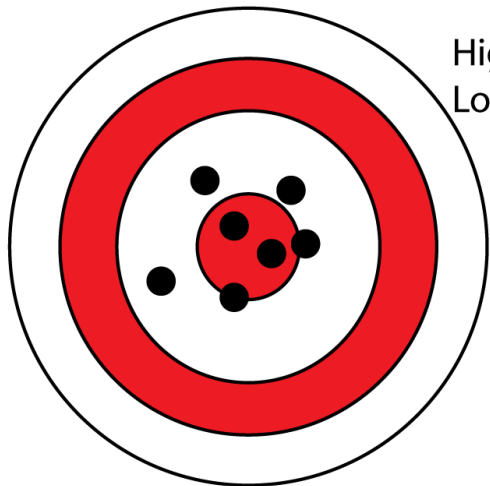
Precision/accuracy - précision/exactitude



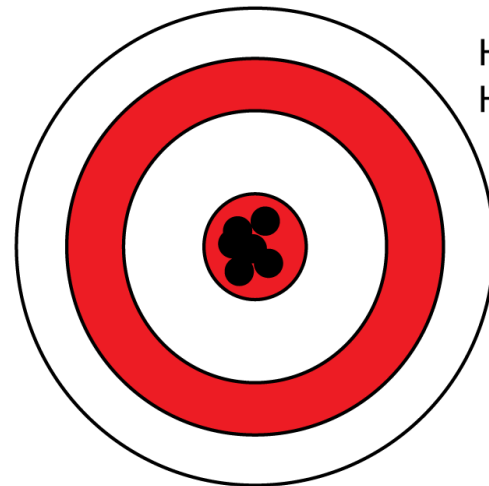
Low accuracy
Low precision



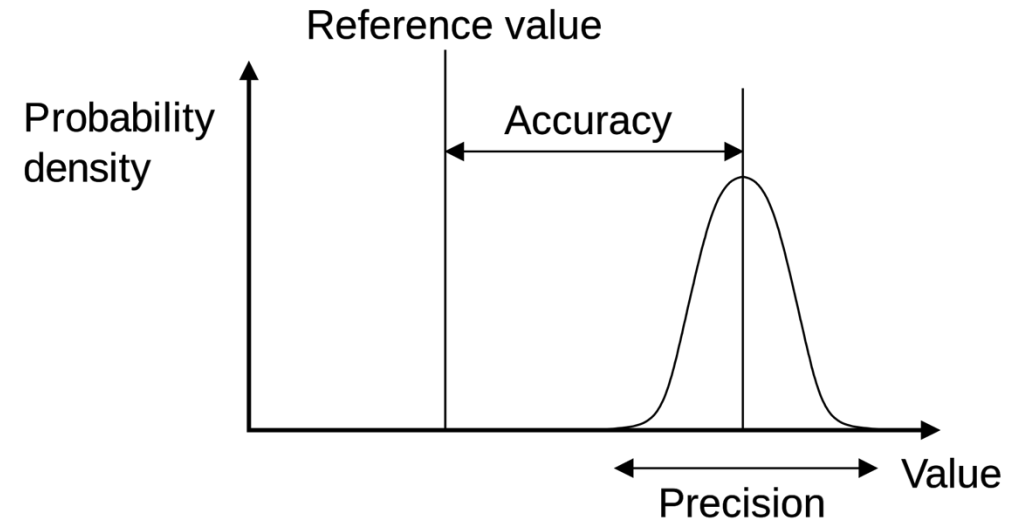
Low accuracy
High precision



High accuracy
Low precision

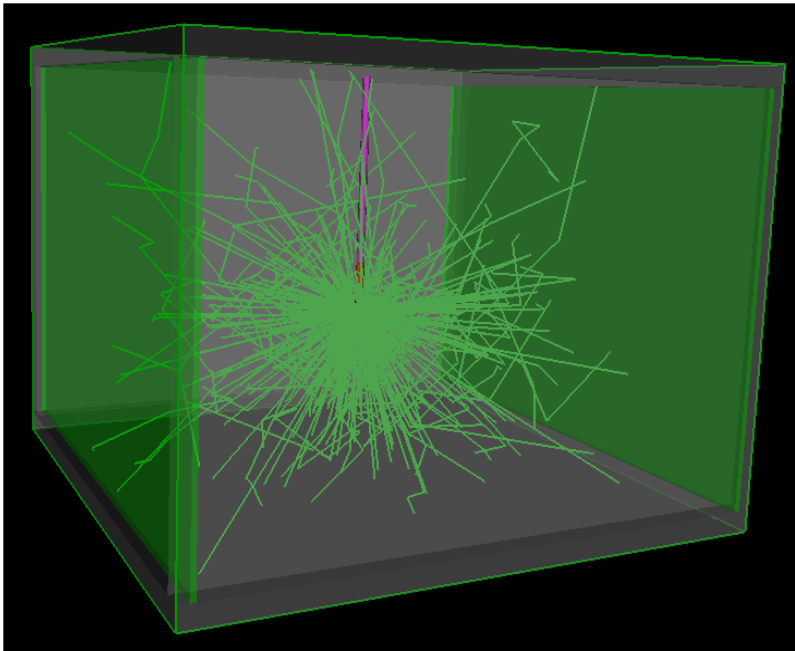


High accuracy
High precision

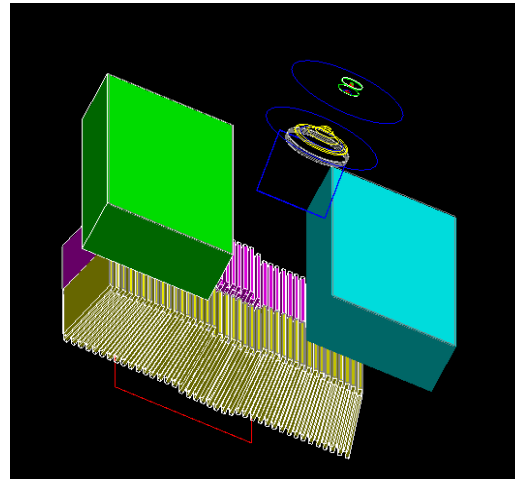


Monte-Carlo in Medical Physics

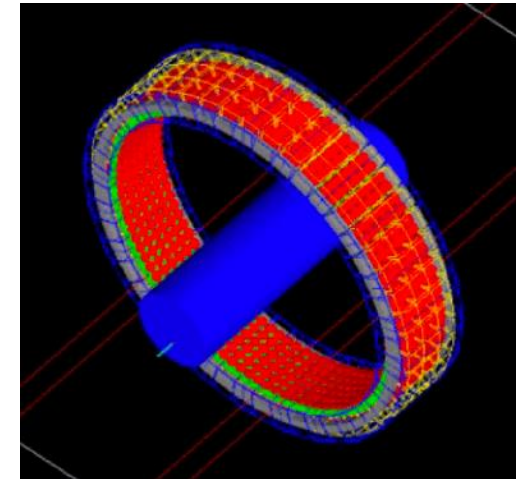
- Simulate particles path, interactions, energy loss
- Monte-Carlo considered as a reference method



Particles tracking



Radiation Therapy



Nuclear Medicine



Robert Oppenheimer

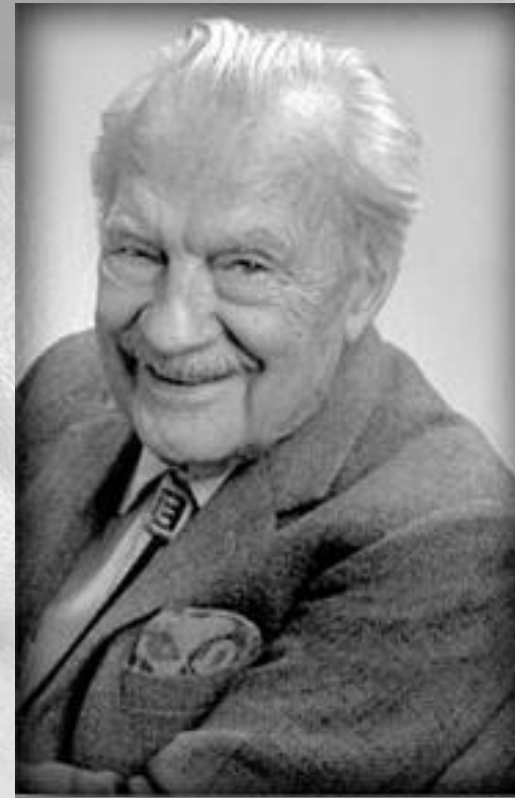
Nuclear physics Monte Carlo simulations



Edward Teller



Stanisław Ulam



Nicholas Metropolis



ENIAC 1947

Metropolis, Nicholas; Stanislaw Ulam (1949).
"The Monte Carlo method". Journal of the American Statistical Association. 44 (247): 335-341
[doi:10.1080/01621459.1949.10483310](https://doi.org/10.1080/01621459.1949.10483310)

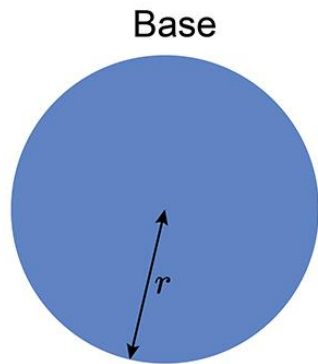
Monte-Carlo



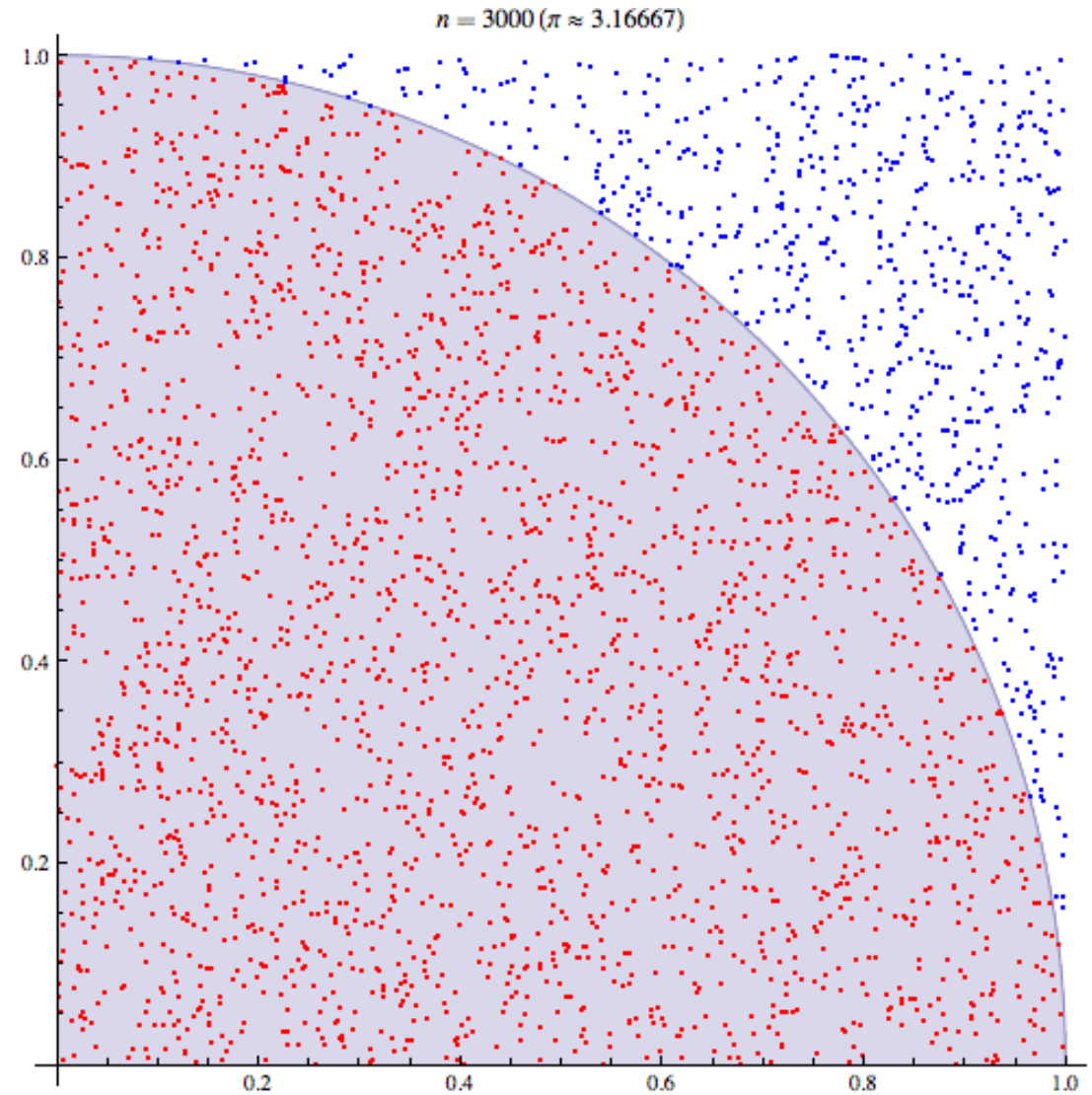
- History : WW2, Manhattan Project, casinos
- What ?
A class of computational algorithms that rely on repeated stochastic sampling to compute results.
- Why ?
When the problem is *many-dimensional* and approximations that factor the problem into products of lower dimensional problems are inaccurate.
A less important reason is that if one has a *complicated geometry*, a MC algorithm may be simpler than other choices.
- Drawback ?
There is a statistical error. Sometimes there is a tradeoff between statistical error and systematic error and one needs to find the best compromise. Could be slow to converge.

[Cyrus J. Umrigar]

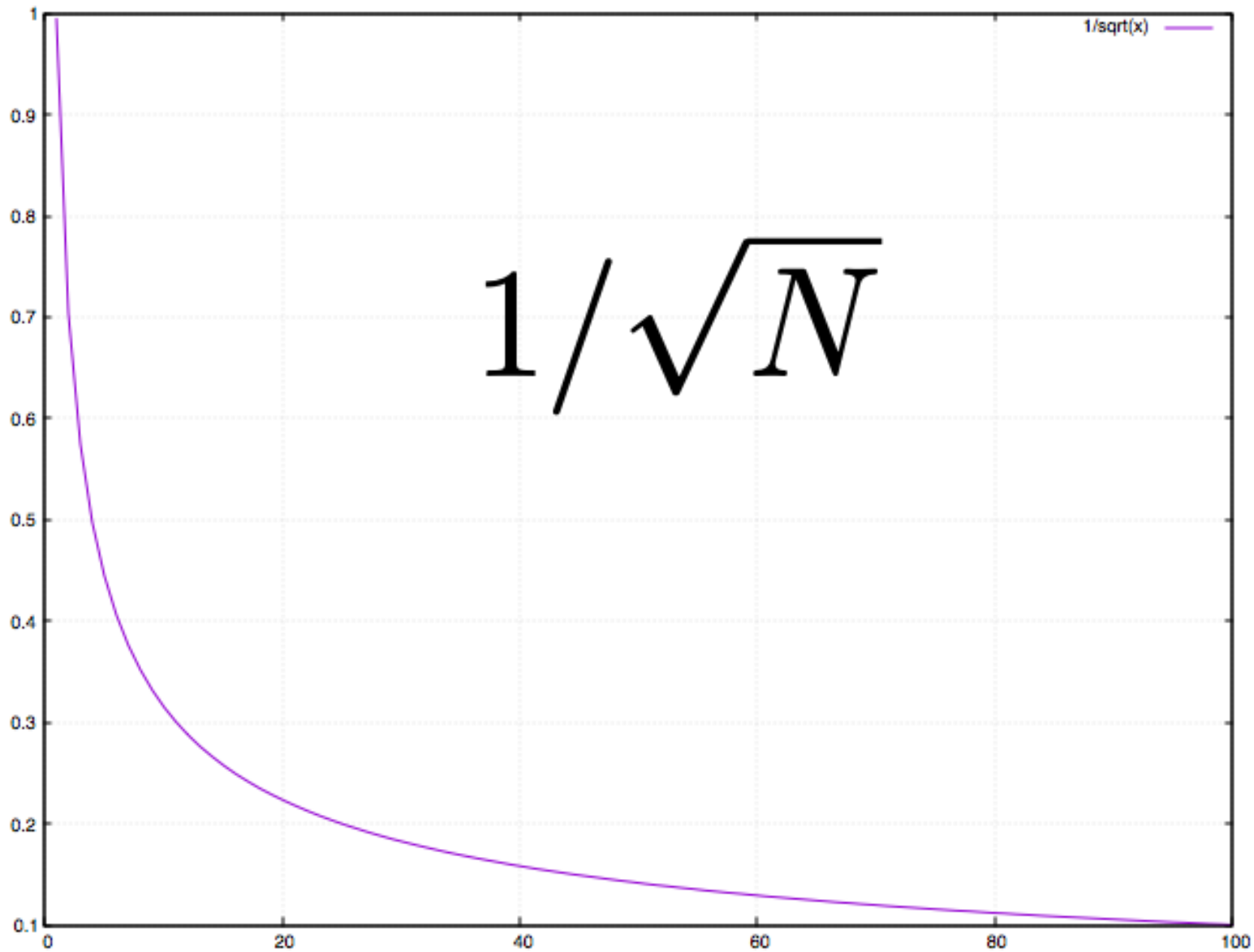
Monte-Carlo estimation



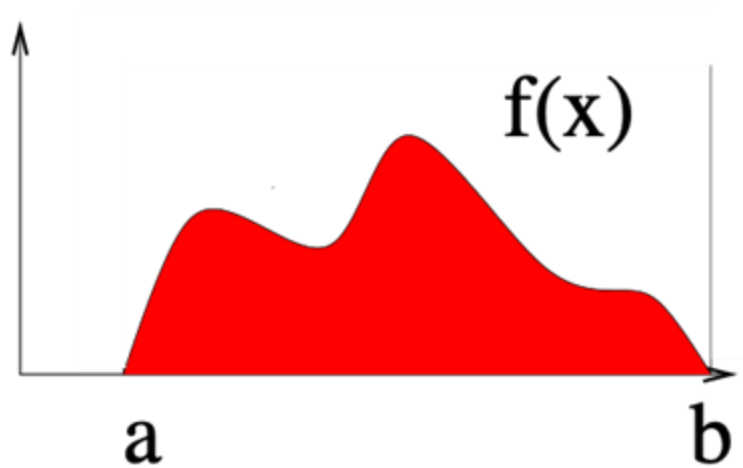
$$\text{Area} = \pi r^2$$



... chaque chiffre significatif supplémentaire,
nécessite un coût de simulation 100 fois supérieur.

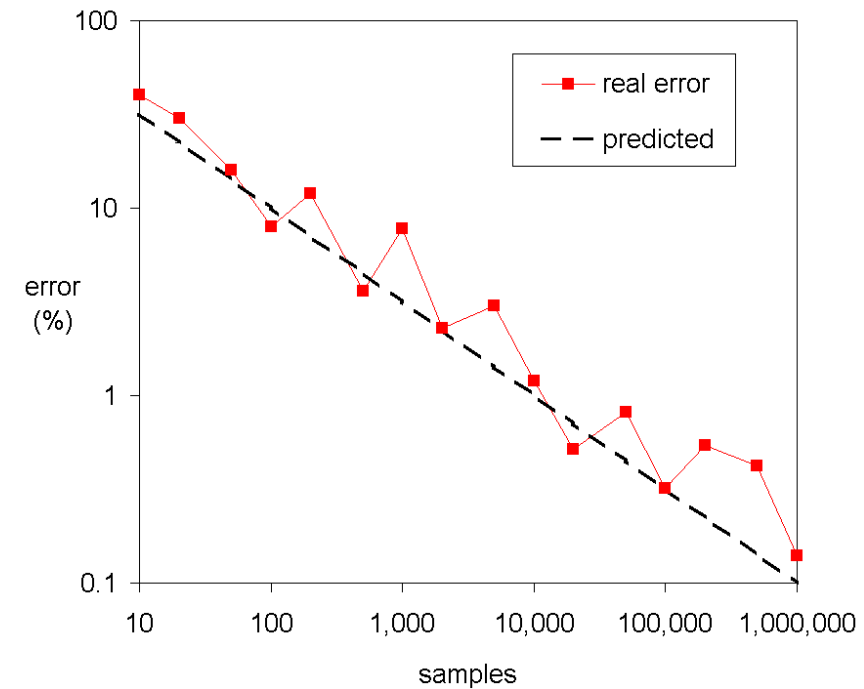


Monte-Carlo



$$I = \int_a^b dx f(x)$$

$$I \approx \frac{b-a}{N} \sum_{i=1}^N f(x_i)$$



Error: $\propto 1/\sqrt{N}$

Error: central limit theorem
independent of the dimension

Monte-Carlo simulations

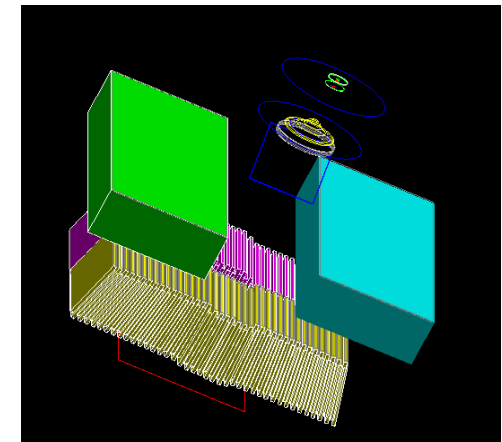
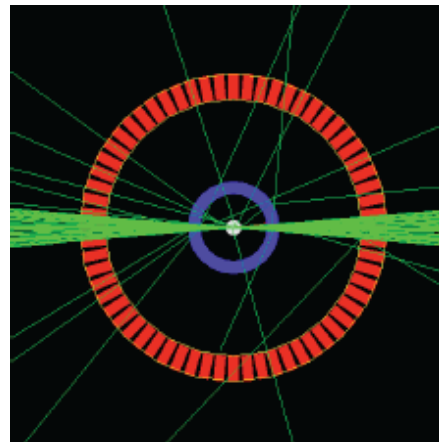
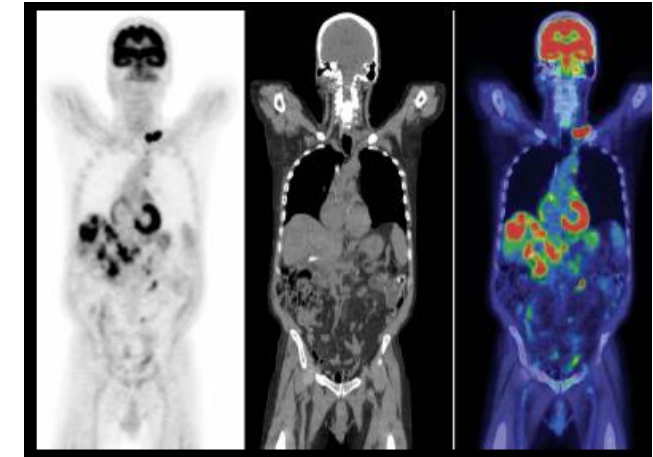
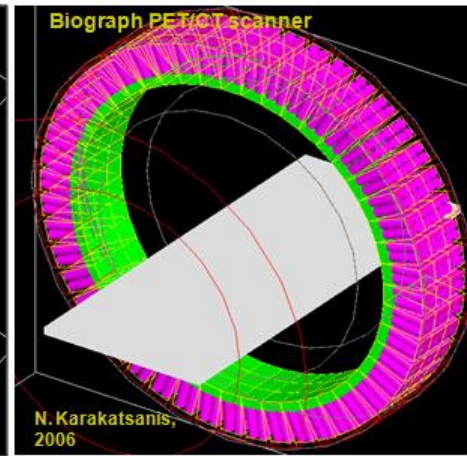
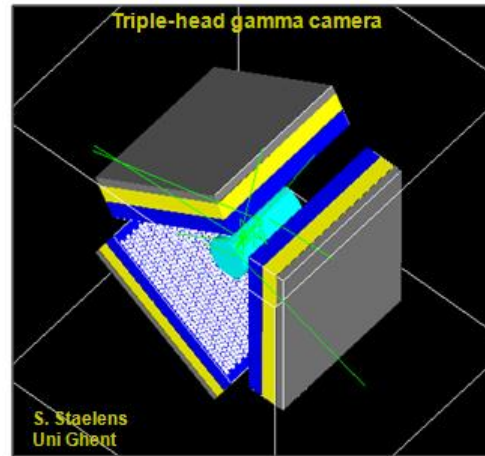
- Requirement : system and physical processes can be modelled from known probability density functions (pdfs)
- Random sampling of the pdfs
- Notions :
 - Random number generator (seed, period)
 - Sampling techniques ; cumulated pdf ; importance sampling
 - Statistical uncertainties / errors ; stopping criteria
 - Variance reduction technique
 - Convergence rate (speed, efficiency)



Applications

Nuclear and radiation imaging modalities

- PET
- SPECT
- Compton Camera
- Prompt gamma
- Proton Rad/CT
- CT
 - Cone Beam
 - Spectral CT
 - Dual Energy
 - Phase Contrast



Particles tracking

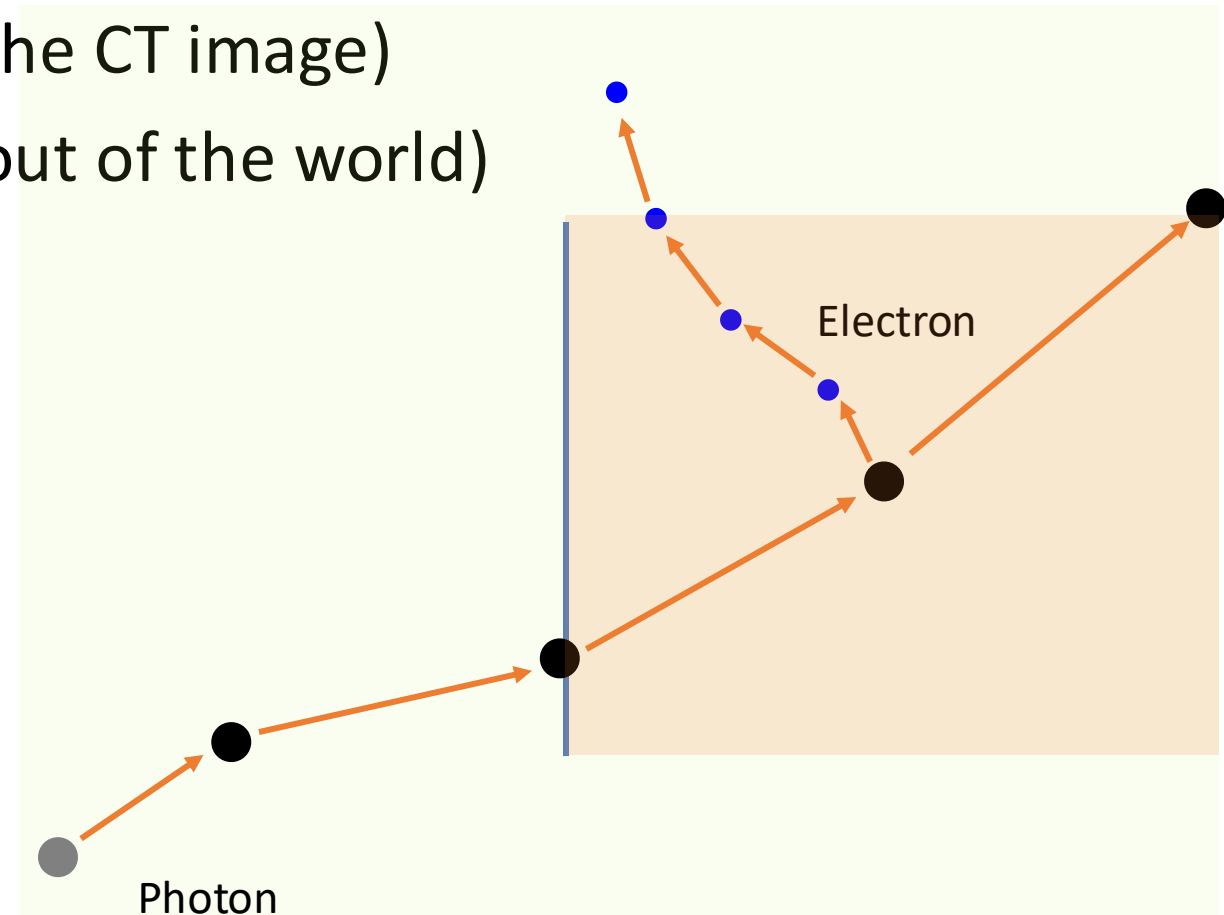
Particles tracking

- From the « *source* »
- Through the « *phantom* »
- To the « *detector* »
- Track all particles individually
 - Tracking path, decomposed in **steps**
 - Several **physical processes**
 - **Probability distributions**

(*ex nihilo* particle creation)

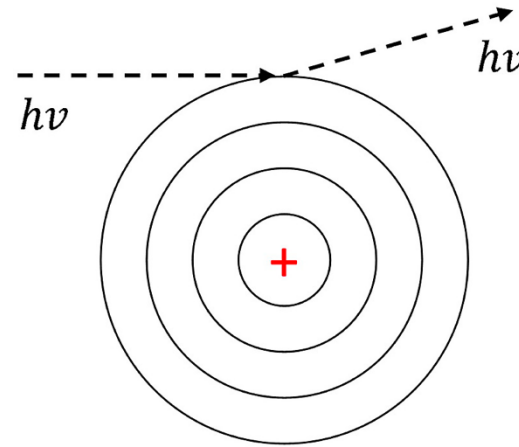
(or the CT image)

(or out of the world)

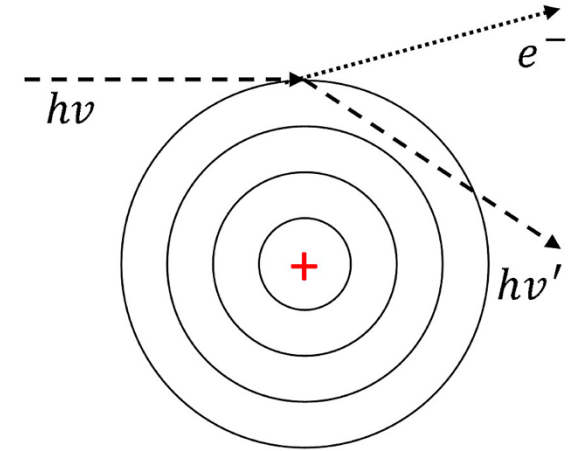


Physical processes

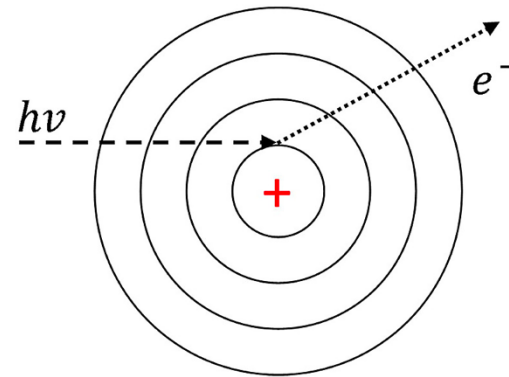
- Example for photon
 - Scattering (Rayleigh, Compton)
 - Photoelectric
 - Pair production
 - Photonuclear ...



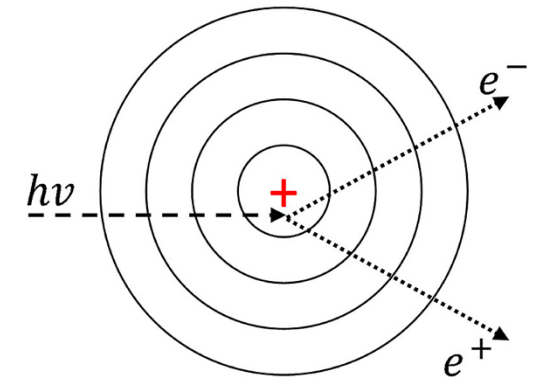
Coherent scattering
(a)



Compton scattering
(b)



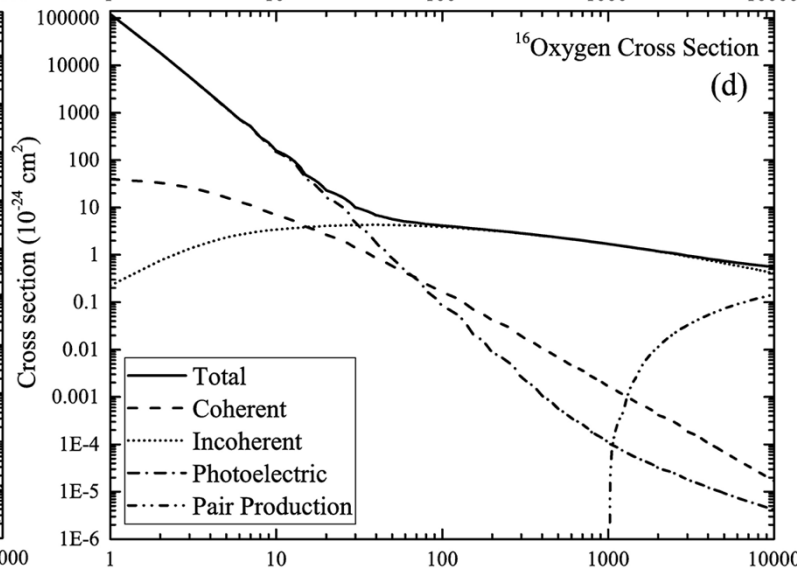
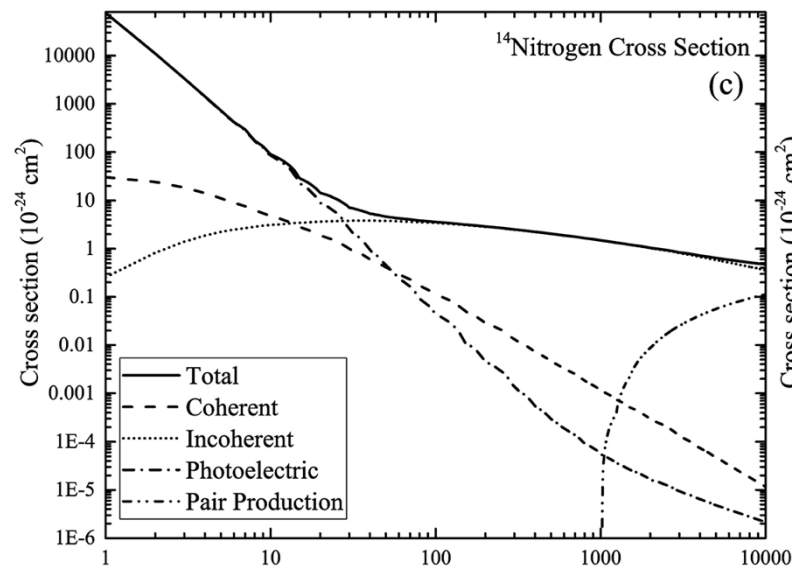
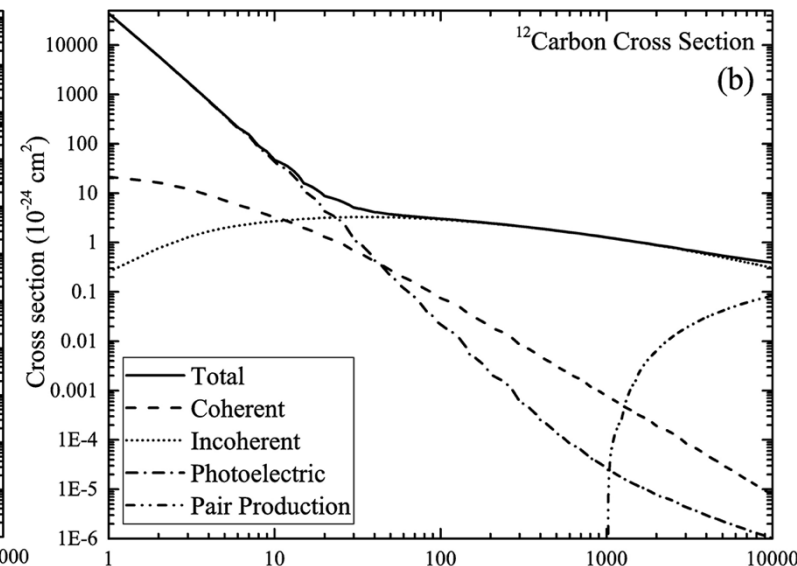
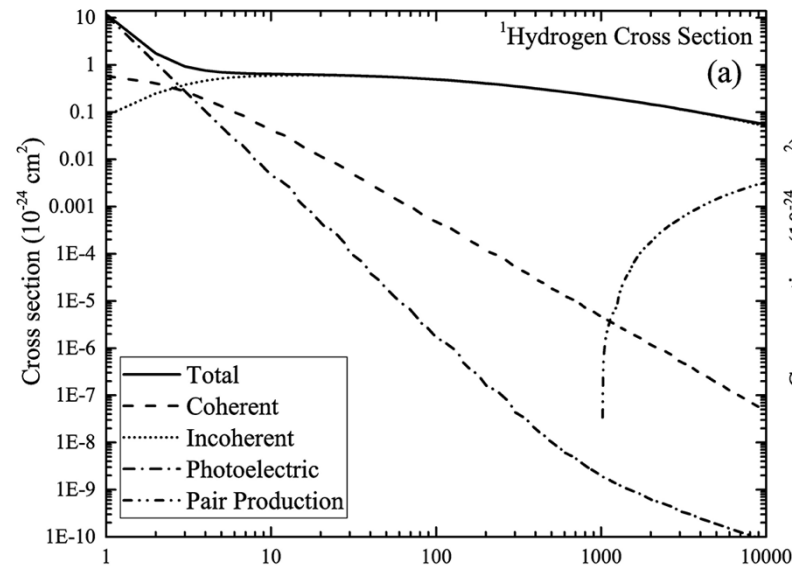
Photoelectric effect
(c)



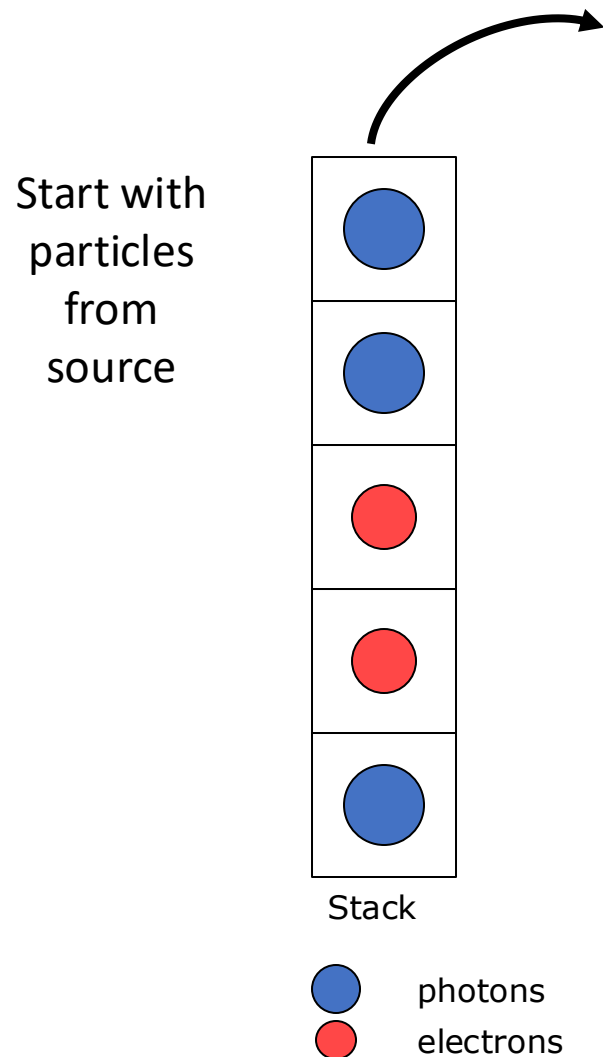
Pair production
(d)

Physical processes

- Cross section
 - Interaction probability
 - wrt material
 - wrt energy
- For all particles
- For all processes
- Large database needed

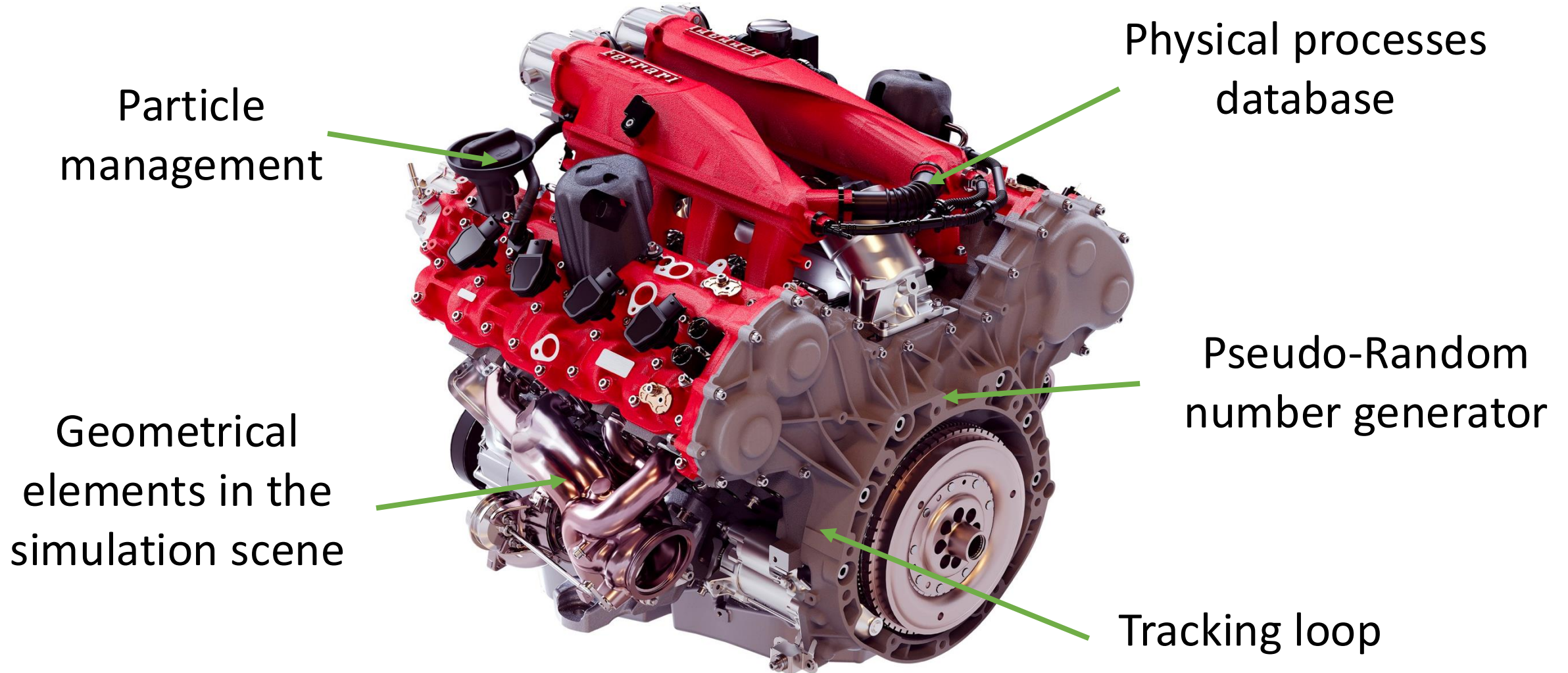


MC engine - Tracking loop (simplified)



- Un-stack a particle p
 - Consider properties of p (E, position, direction, time ...)
 - Consider current material composition at position
 - **Sample** random distance to next interactions
 - Given a set of possible physical processes
 - Given the properties & material
 - **Transport** p to this interaction point
 - Check not exiting the current material
 - Check not exiting the “world”
 - **Model** the selected interaction
 - If absorption: end
 - If new particle: insert in the stack
 - Change properties, generate secondary particles (stack)
 - Next step
- Next particle

Monte Carlo engine



Difficulty & Challenges

- Computation time: Variance Reduction Technique
- Tradeoff: speed – complexity – accuracy
- Validation against experiments (uncertainties)
- Access to industrial data
- Input models (physics, biological ...)
- Multi-scale aspects
- Multi-disciplinary: physics, mathematic, biology, medicine, computer sciences



Monte Carlo simulations evolution

- Around 60+ years evolution
 - More accurate physical databases
 - More generic codes (MCNPX, EGSNRC, Penelope, Geant4, Gate)
 - Faster algorithms
 - Use of powerful computing infrastructures (cluster, GPU)
- However
 - Increasing need for detailed and accurate physical processing (TOF, SiPM, CZT, etc)
 - Still long simulations times
 - Generic vs Specific codes
 - IA ?

INSTITUTE OF PHYSICS PUBLISHING

PHYSICS IN MEDICINE AND BIOLOGY

Phys. Med. Biol. **51** (2006) R287–R301

[doi:10.1088/0031-9155/51/13/R17](https://doi.org/10.1088/0031-9155/51/13/R17)

REVIEW

Fifty years of Monte Carlo simulations for medical physics*

D W O Rogers

Physics Department, Carleton University, Ottawa, Ontario K1S 5B6, Canada

E-mail: drogers@physics.carleton.ca

Received 23 February 2006, in final form 3 May 2006

Published 20 June 2006

Online at stacks.iop.org/PMB/51/R287

Abstract

Monte Carlo techniques have become ubiquitous in medical physics over the last 50 years with a doubling of papers on the subject every 5 years between the first PMB paper in 1967 and 2000 when the numbers levelled off. While recognizing the many other roles that Monte Carlo techniques have played in medical physics, this review emphasizes techniques for electron–photon transport simulations. The broad range of codes available is mentioned but

Available MC codes

- **Industrial software** : in TPS
- **Multi-purpose, research** : MCNPX, EGS-nrc, Penelope, Geant4, GATE, Fluka, ...
- **Characteristics ?**
 - Available physics : particles, models, energy limits, models, database tables
 - Description of various geometrical shapes (voxels etc)
 - Description of various source types
 - Available types of observable (dose)
 - Variance reduction techniques
 - Possibility to evolve
 - Validation – reputation
 - Ease of use
 - Community, documentation
 - Code language,
 - Open-source





- 1 Go to wooclap.com
- 2 Enter the event code in the top banner

Event code
JOPIXG



- 1 Send **@JOPIXG** to **06 44 60 96 62**
- 2 You can participate

 Disable answers by SMS

Geant4 & GATE

Geant4



- Geant4 is a **toolkit**
- Developed by CERN & international community
- Since 1999 ; about 2 releases/year ; now version 11.3 (December 2023)
- Features :

“Geant4 is a toolkit for simulating the passage of particles through matter. It includes a complete range of functionality including tracking, geometry, physics models and hits. ”

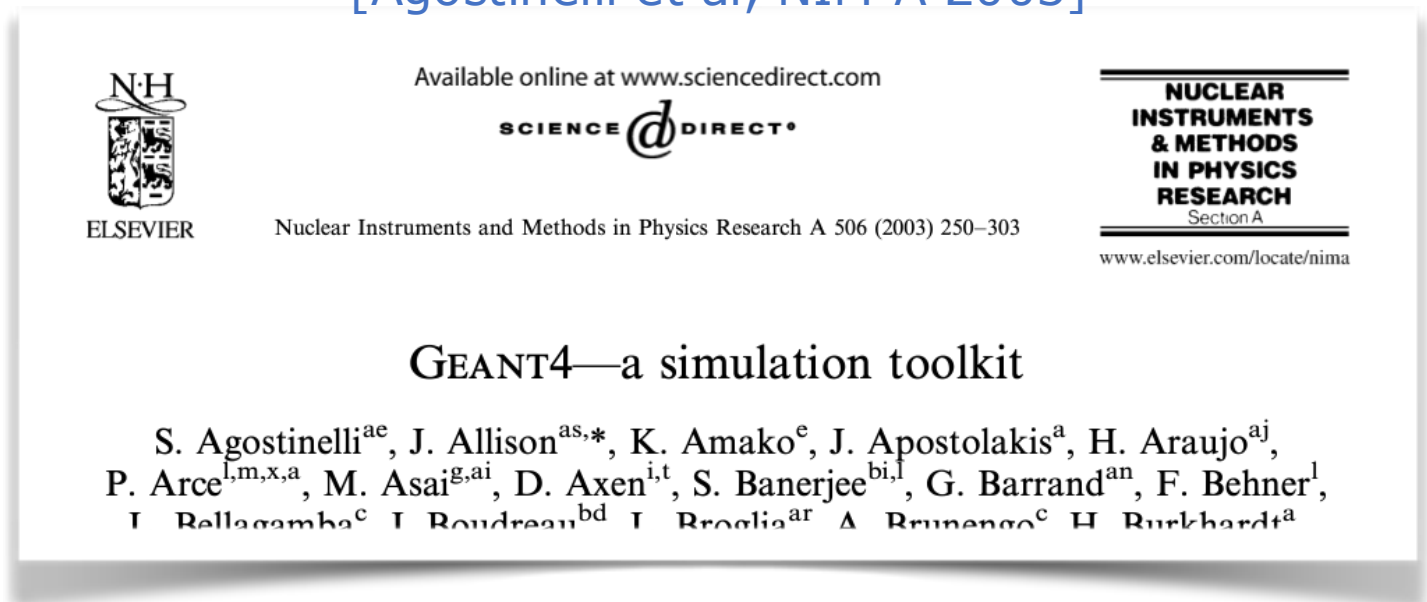
- LHC : Higgs boson, high energy physics
- Large user community
- Open-source
- **Usage**
 - Code your simulation in C++
 - Use classes, functions provided by Geant4
 - Compile your code, obtain a executable
 - Run it



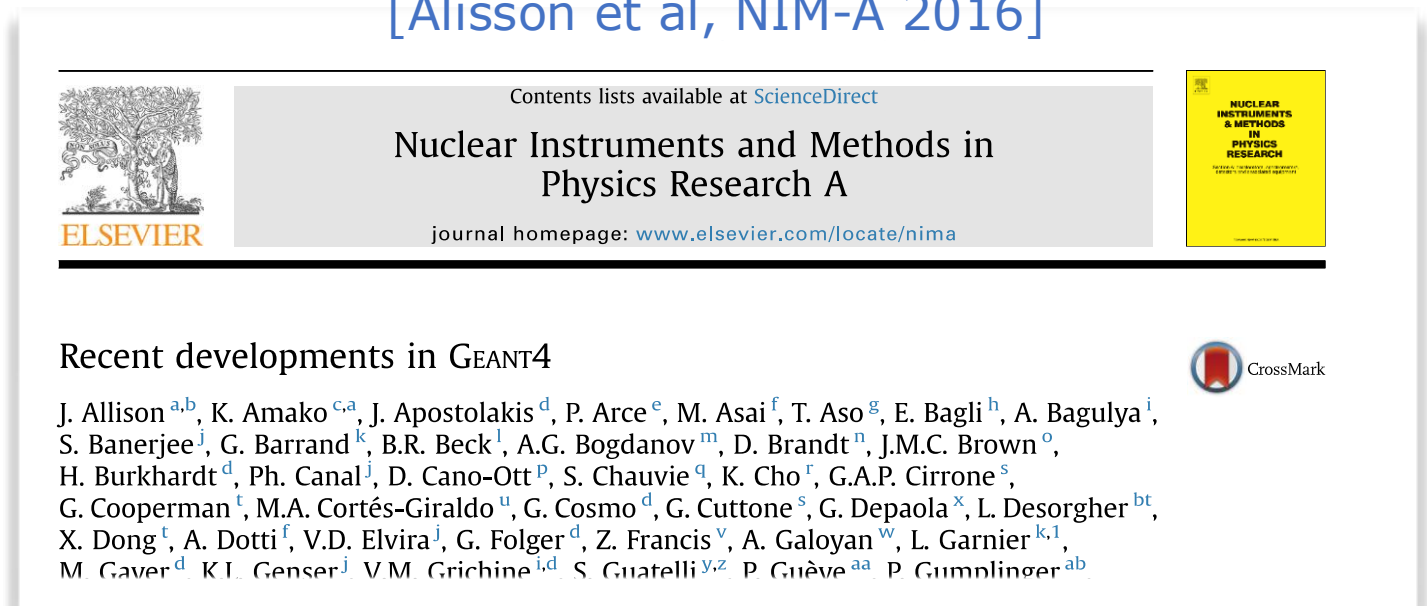
Geant4

- Web site
 - Download code
 - Installation guide
 - User guide
 - Developer guide
 - Mailing list
- Workshop, formation

[Agostinelli et al, NIM-A 2003]



[Alisson et al, NIM-A 2016]



Create a simulation with G4

- Geant4 simulation
- Need C++ code
 - Main.cpp
 - +3 files (classes)
 - Compile to get executable file
- Powerful, but can be tedious
- Not easy to re-use among users

Listing 1 Simplest example of main()

```
#include "G4RunManager.hh"
#include "G4UImanager.hh"

#include "ExG4DetectorConstruction01.hh"
#include "ExG4PhysicsList00.hh"
#include "ExG4ActionInitialization01.hh"

int main()
{
    // construct the default run manager
    G4RunManager* runManager = new G4RunManager;

    // set mandatory initialization classes
    runManager->SetUserInitialization(new ExG4DetectorConstruction01);
    runManager->SetUserInitialization(new ExG4PhysicsList00);
    runManager->SetUserInitialization(new ExG4ActionInitialization01);

    // initialize G4 kernel
    runManager->Initialize();

    // get the pointer to the UI manager and set verbosity
    G4UImanager* UI = G4UImanager::GetUIpointer();
    UI->ApplyCommand("/run/verbose 1");
    UI->ApplyCommand("/event/verbose 1");
    UI->ApplyCommand("/tracking/verbose 1");

    // start a run
    int numberOfEvent = 3;
    runManager->BeamOn(numberOfEvent);

    // job termination
    delete runManager;
    return 0;
}
```

GATE

Geant4 Application for Emission Tomography, Transmission Tomography, Radiotherapy

- **GATE is a Geant4 application**
 - Written in C++
 - Using the Geant4 toolkit
 - Provide extension to the Geant4 macro language
- **Applications**
 - PET, SPECT, CT imaging
 - Dosimetry radiation therapy, hadrontherapy, molecular radiotherapy, brachytherapy,
 - Detector design, optimisation of acquisition protocol, assessment of quantification methods, etc ...



GATE: a brief history

- Initial idea around 2001 (C. Morel, I. Buvat et al)
- First release in 2004 (S. Jan): TEP, SPECT
- Increase range of application since Gate 6 (2010): radiation therapy, particle therapy
- About 1-2 releases/year
- Now: **GATE 10**



More than 100 peer-reviewed GATE-related papers produced by members of the collaboration

- Best paper citation price in PMB 2004
- Best paper citation price in PMB 2011

GATE: reference papers

INSTITUTE OF PHYSICS PUBLISHING

PHYSICS IN MEDICINE AND BIOLOGY

Phys. Med. Biol. **49** (2004) 4543–4561

PII: S0031-9155(04)80763-2

GATE: a simulation toolkit for PET and SPECT

S Jan¹, G Santin^{2,24}, D Strul^{2,25}, S Staelens³, K Assié⁴, D Autret⁵, S Avner⁶, R Barbier⁷, M Bardès⁵, P M Bloomfield⁸, D Brasse⁶, V Breton⁹, P Bruyndonckx¹⁰, I Buvat⁴, A F Chatzioannou¹¹, Y Choi¹², Y H Chung¹², C Comtat¹, D Donnarieix^{9,13}, L Ferrer⁵, S J Glick¹⁴, C J Groiselle¹⁴, D Guez¹⁵, P-F Honore¹⁵, S Kerhoas-Cavata¹⁵, A S Kirov¹⁶, V Kohli¹¹, M Koole³, M Krieguer¹⁰, D J van der Laan¹⁷, F Lamare¹⁸, G Largeron⁷, C Lartizen¹⁹, D Lazaro⁹, M C Maas¹⁷, L Maigne⁹, F Mayet²⁰, F Melot²⁰, C Merheb¹⁵, E Pennacchio⁷, J Perez²¹, U Pietrzyk²¹, F R Rannou^{11,22}, M Rey², D R Schaart¹⁷, C R Schmidtlein¹⁶, L Simon^{2,26}, T Y Song¹², J-M Vieira², D Visvikis¹⁸, R Van de Walle³, E Wieërs^{10,23} and C Morel²

A review of the use and potential of the GATE Monte Carlo simulation code for radiation therapy and dosimetry applications

David Sarrut^{a)}

Université de Lyon, CREATIS; CNRS UMR5220; Inserm U1044; INSA-Lyon; Université Lyon 1; Centre Léon Bérard, France

Manuel Bardès

Inserm, UMR1037 CRCT, F-31000 Toulouse, France and Université Toulouse III-Paul Sabatier, UMR1037 CRCT, F-31000 Toulouse, France

Nicolas Bousson

INSERM, UMR 1101, LaTIM, CHU Morvan, 29609 Brest, France

Nicolas Buvat

Phys Med Biol 2004
Phys Med Biol 2011
Medical physics 2014
Phys Med Biol 2021
Phys Med Biol 2022

IOP PUBLISHING

PHYSICS IN MEDICINE AND BIOLOGY

Phys. Med. Biol. **56** (2011) 881–901

doi:10.1088/0031-9155/56/4/001

GATE V6: a major enhancement of the GATE simulation platform enabling modelling of CT and radiotherapy

S Jan¹, D Benoit², E Becheva¹, T Carlier^{3,4}, F Cassol⁵, P Descourt⁶, T Frisson⁷, L Grevillot⁷, L Guigues⁷, L Maigne⁸, C Morel⁵, Y Perrot⁸, N Rehfeld², D Sarrut⁷, D R Schaart⁹, S Stute², U Pietrzyk¹⁰, D Visvikis⁶, N Zahra⁷ and I Buvat²

IOP Publishing

Phys. Med. Biol. **66** (2021) 10TR03

<https://doi.org/10.1088/1361-6560/abf276>

Physics in Medicine & Biology



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TOPICAL REVIEW

Advanced Monte Carlo simulations of emission tomography imaging systems with GATE

David Sarrut^{1,*}, Mateusz Bala², Manuel Bardès³, Julien Bert⁴, Maxime Chauvin⁵, Konstantinos Chatzipapas⁶, Mathieu Dupont⁷, Ane Etxebeste¹, Louise M Fanchon⁸, Sébastien Jan⁹, Gunjan Kayal^{5,10}, Assen S Kirov⁸, Pawel Kowalski¹¹, Wojciech Krzemien¹¹, Joey Labour¹, Mirjam Lenz^{12,13}, George Loudos⁶, Brahim Mehadj⁷, Laurent Ménard^{14,15}, Christian Morel⁷, Panagiotis Papadimitroulas⁶, Magdalena Rafecas¹⁶, Julien Salvadori¹⁷, Daniel Seiter¹⁸, Mariele Stockhoff¹⁹, Etienne Testa²⁰, Carlotta Trigila²¹, Uwe Pietrzyk¹³, Stefaan Vandenberghe¹⁹, Marc-Antoine Verdier^{14,15}, Dimitris Visvikis⁴, Karl Ziemons¹², Milan Zvolosky¹⁶ and Emilie Roncali²¹

¹ Université de Lyon, CREATIS, CNRS UMR5220, Inserm U1294, INSA-Lyon, Université Lyon 1, Lyon, France

² Jagiellonian University, Kraków, Poland

³ Cancer Research Institute of Montpellier, U1194 INSERM/ICM/Montpellier University, 208 Av des Apothicaires, F-34298 Montpellier

GATE: a collaboration

- OpenGate Collaboration
 - About 22 labs, worldwide (40% in France)
 - Spoken person : Lydia Maigne
 - Technical coordinator : David Sarrut
- Organize the development of GATE
 - Meetings, projects, teaching etc
 - Developers : open-source
 - Funding
- **GATE is a collaboration before being a software**



<http://www.opengatecollaboration.org>

gate-users@lists.opengatecollaboration.org

<https://opengate.readthedocs.io>

GATE: limitations

- Too few numbers of developers
- Documentation to be improved
- Macro vs C++
- Visualisation not perfect (Geant4)
- Support



GATE: limitations

- Too few numbers of developers
- Documentation to be improved
- ~~Macro vs C++~~ Python vs C++
- Visualisation not perfect (Geant4)
- Support



Use of Gate

Gate : **imaging** and **dosimetry** in medical physics

Published studies:

- TEP, SPECT
- RT photon, low and high energy
- X-ray imaging
- RT hadron proton, carbon, helium
- RT internal dosimetry (all isotopes)
- Hadron-PET, prompt-gamma, vertex imaging

