



Lyon, Avril 17- 21

DLM12023

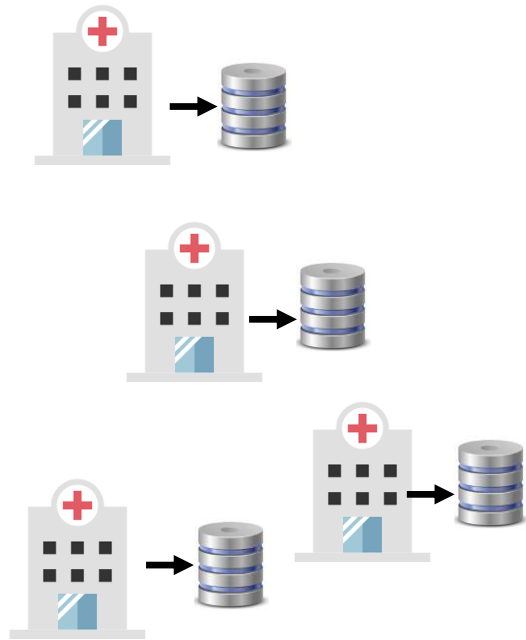


Weakly Supervised Segmentation

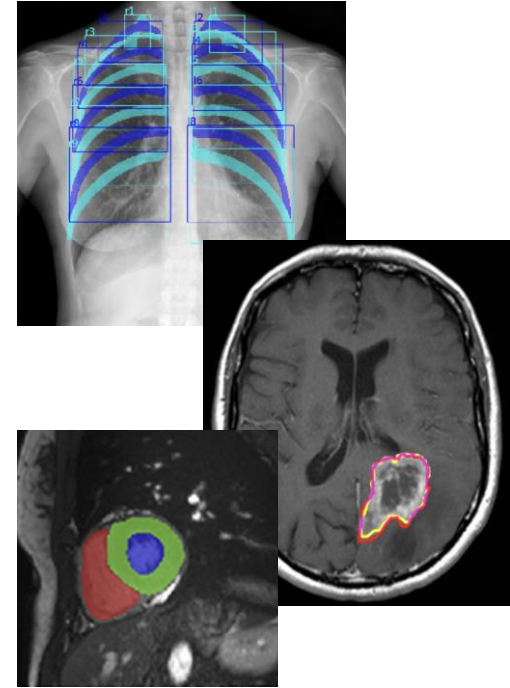
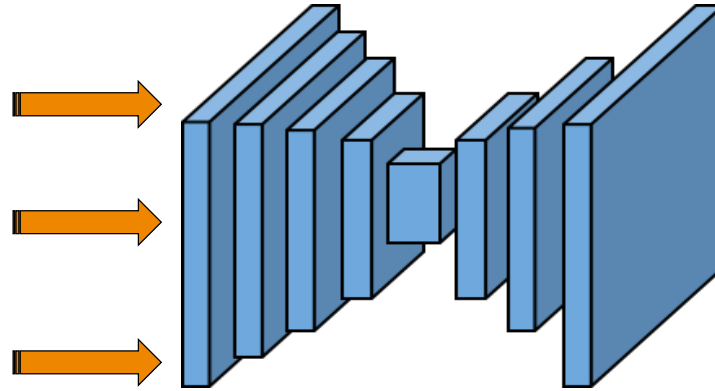
Jose Dolz

ÉTS, Montreal

Motivation



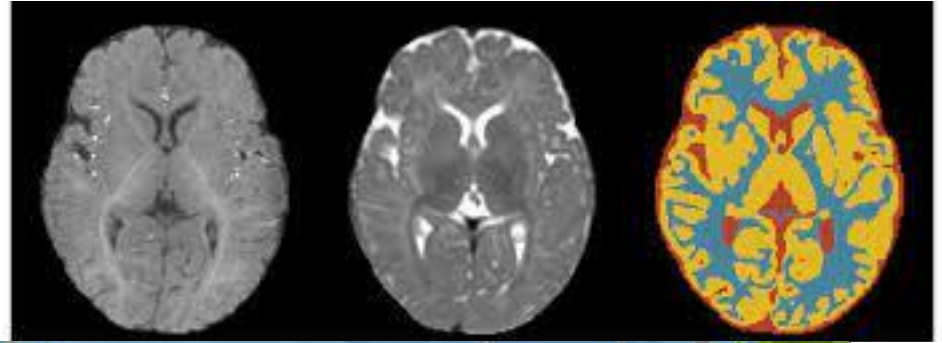
Large labeled (pixel-wise) datasets



Very good performance in many tasks

Motivation

Pixel-wise annotation is a time-consuming task...



Motivation

... which further requires domain expertise

Which images contain the class 'esophagus'?

Select all images with
esophagus
Click verify once there are none left.

⌂ 🎧 ⓘ

VERIFY

Motivation

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And where on these images the esophagus is?

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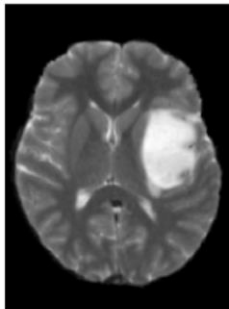
Data-driven priors (cues)

Image tags



Person

Bike



Tumor

Original
Image

Image tags

- Pathak et al., Constrained convolutional neural networks for weakly supervised segmentation, ICCV 2015
- Kervadec et al., Constrained-CNN losses for weakly supervised segmentation, MedIA 2019.

Data-driven priors (cues)

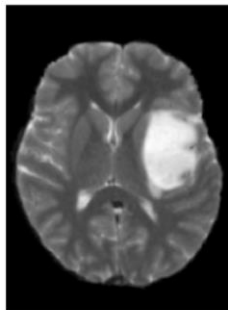
Image tags

Bounding boxes

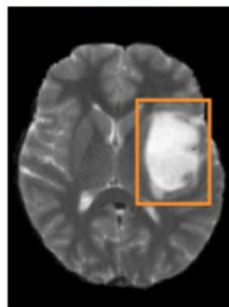


Person

Bike



Tumor



Original
Image

Image tags

Bounding
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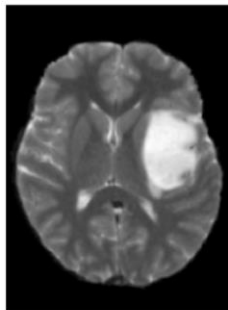
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Data-driven priors (cues)

Image tags

Bounding boxes

Scribbles



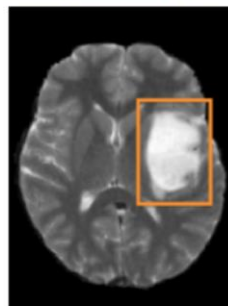
Original
Image

Person

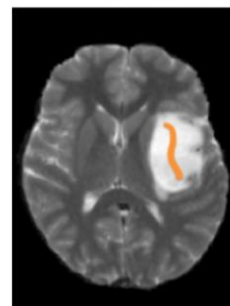
Bike

Tumor

Image tags



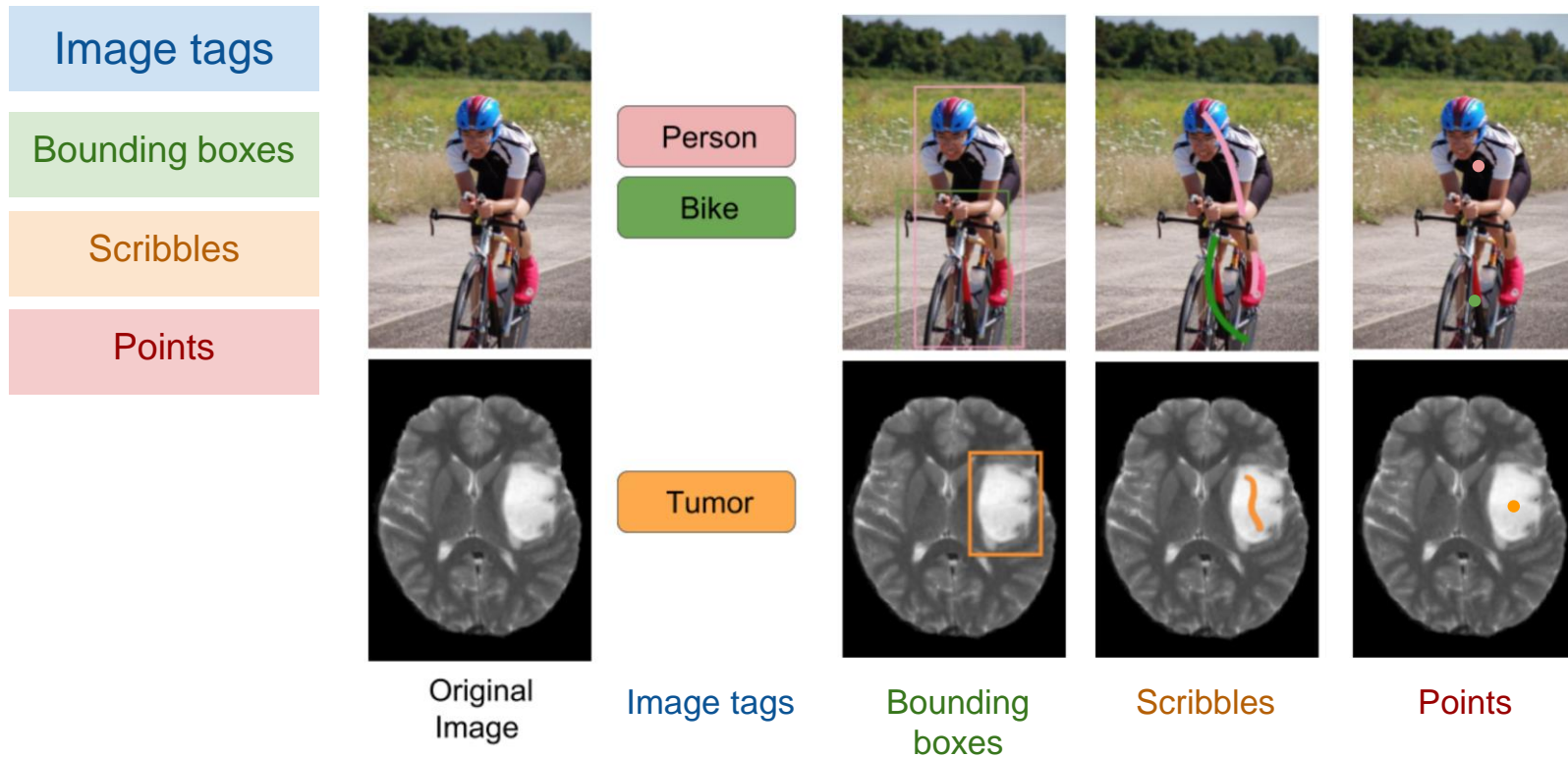
Bounding
boxes



Scribbles

- Pathak et al., Constrained convolutional neural networks for weakly supervised segmentation, ICCV 2015
- Kervadec et al., Constrained-CNN losses for weakly supervised segmentation, MedIA 2019.

Data-driven priors (cues)



- Pathak et al., Constrained convolutional neural networks for weakly supervised segmentation, ICCV 2015
- Kervadec et al., Constrained-CNN losses for weakly supervised segmentation, MedIA 2019.

Data-driven priors (cues)

Another data-driven priors

Image captions



A boy jumping on a skateboard

Extreme points

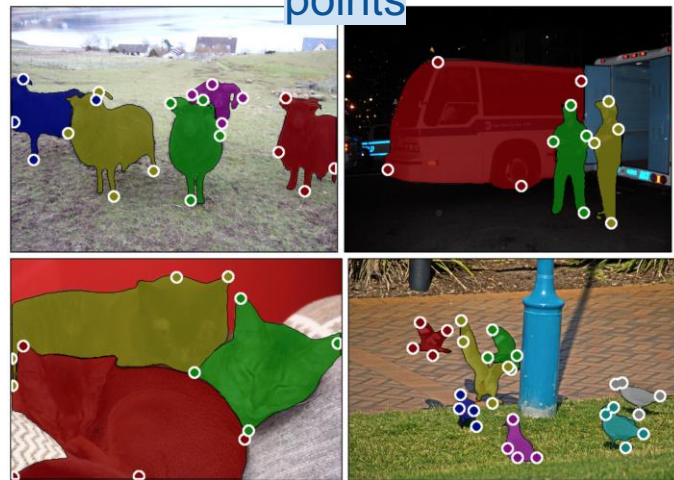


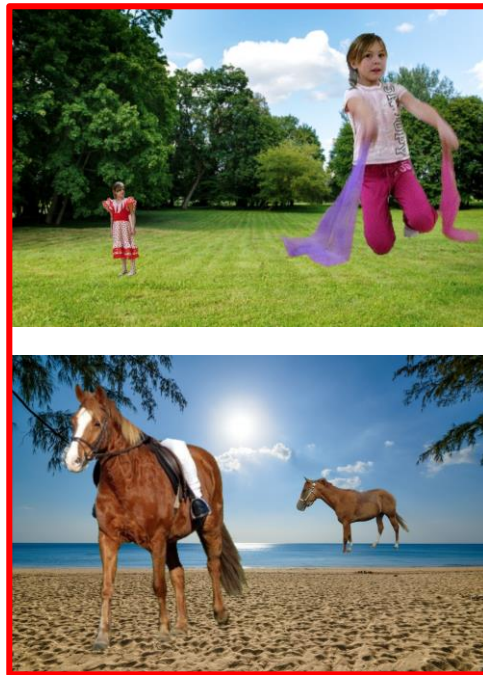
Image from Maninis et al, CVPR'18

- Maninis et al. Deep extreme cut: From extreme points to object segmentation. CVPR 2018

Knowledge-driven priors

Common priors in natural images

Target Size



Incorrect sizes



Correct sizes

- Pathak et al., Constrained convolutional neural networks for weakly supervised segmentation, ICCV 2015
- Xu et al., Learning to Segment Under Various Forms of Weak Supervision, CVPR 2015
- Zhang et al., Curriculum Domain Adaptation for Semantic Segmentation of Urban Scenes. ICCV'17

Knowledge-driven priors

Common priors in natural images

Target Location

Incorrect
location



Correct
location



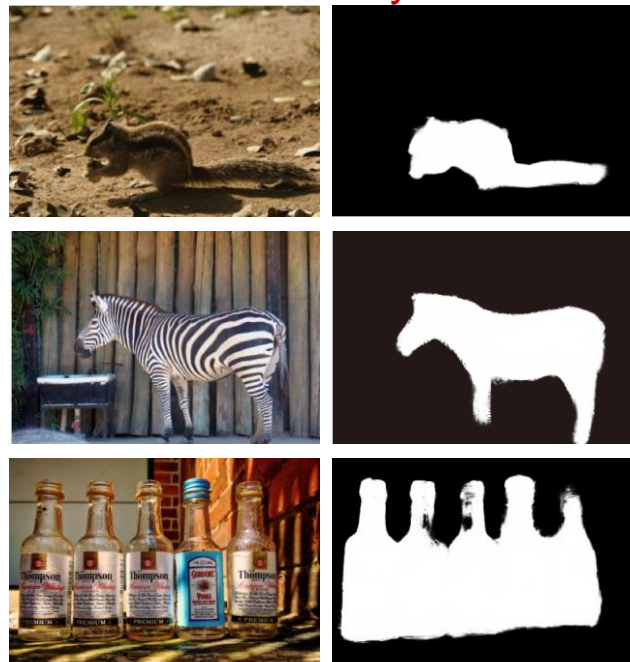
- Remez et al. Learning to segment via cut-and-paste. ECCV 2018
- Georgakis et al Synthesizing training data for object detection in indoor scenes. RSS 2017

Knowledge-driven priors

Common priors in natural images

Contrast
Foreground/Background

Saliency



Images from Hou et al, CVPR'17

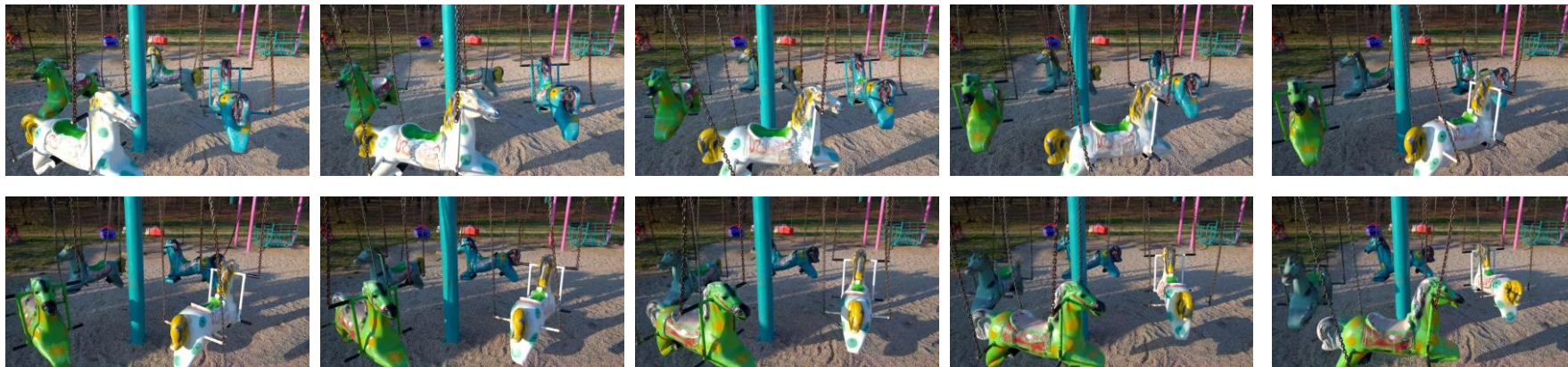
- Hou et al. Deeply supervised salient object detection with short connections. CVPR 2017
- Li et al. Instance-level salient object segmentation. CVPR 2017

Knowledge-driven priors

Common priors in natural images

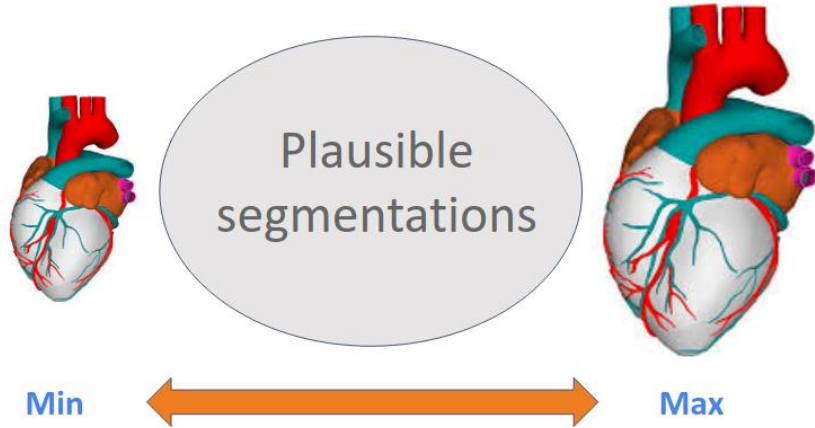
Motion

Images from the DAVIS Challenge Dataset



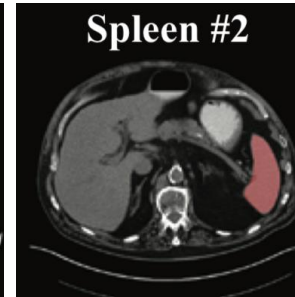
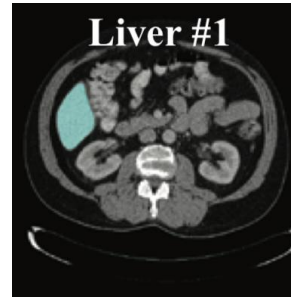
- Tokmakov et al. Weakly-supervised semantic segmentation using motion cues. ECCV 2016
- Pathak et al. Learning features by watching objects move. CVPR 2017

Knowledge-driven priors



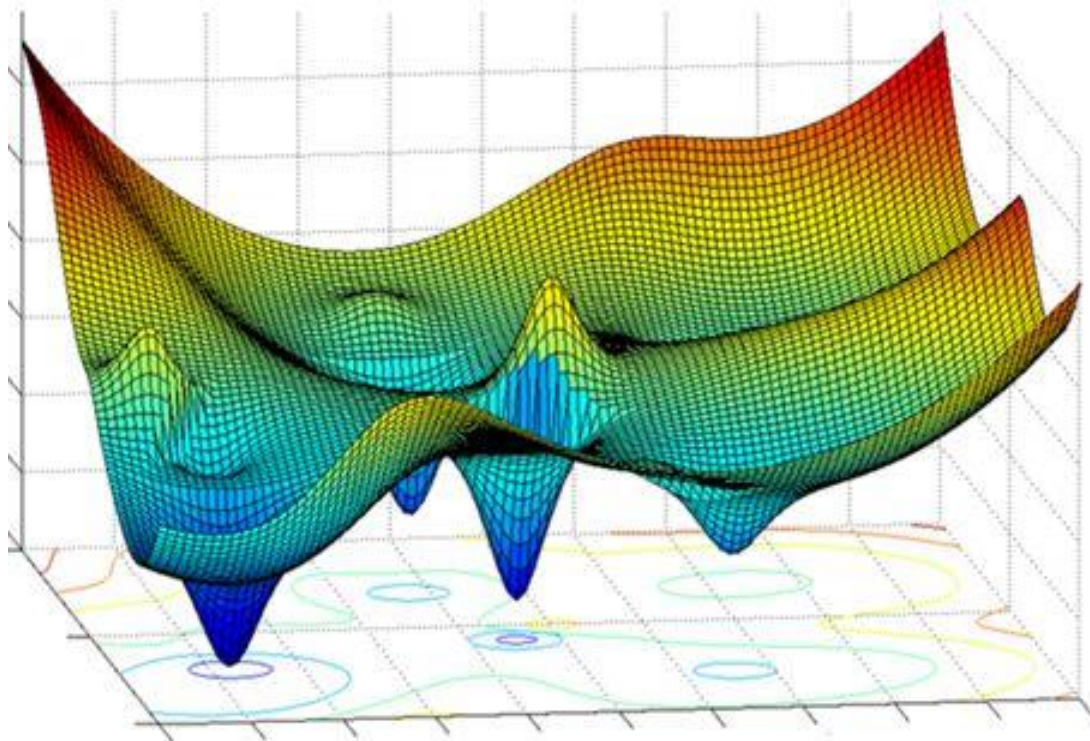
Anatomical priors

What about priors in the medical domain?

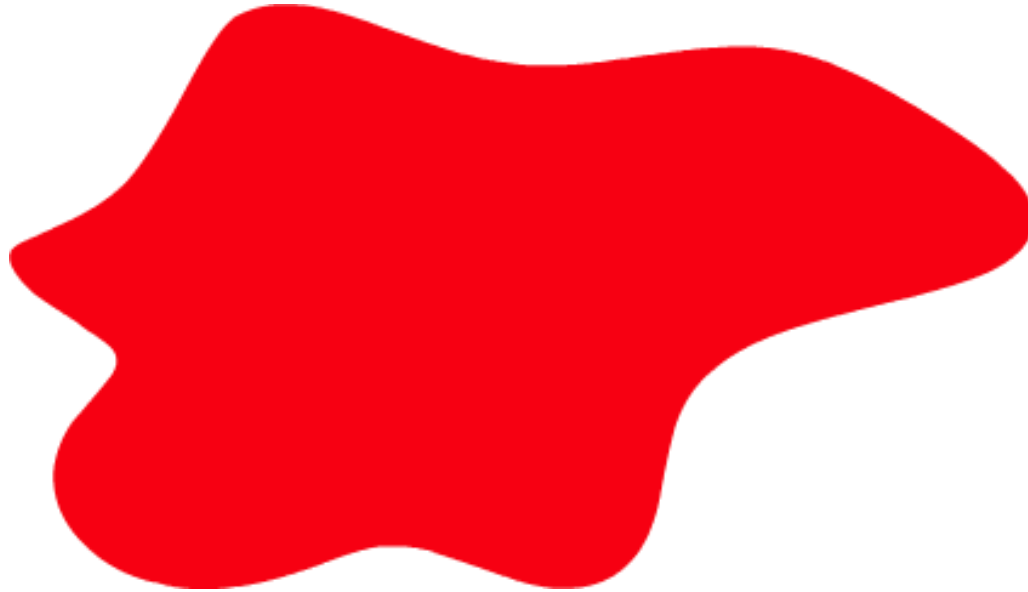


Partial labeled data
(exploit target relationships)

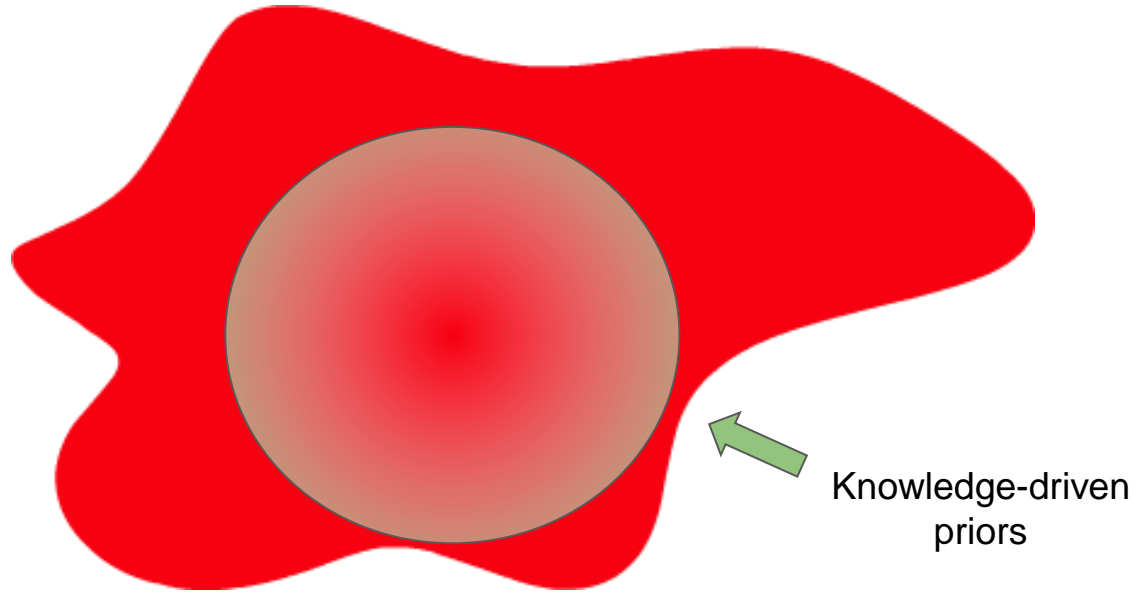
Recall of what learning means
(from a gradient descent standpoint)...



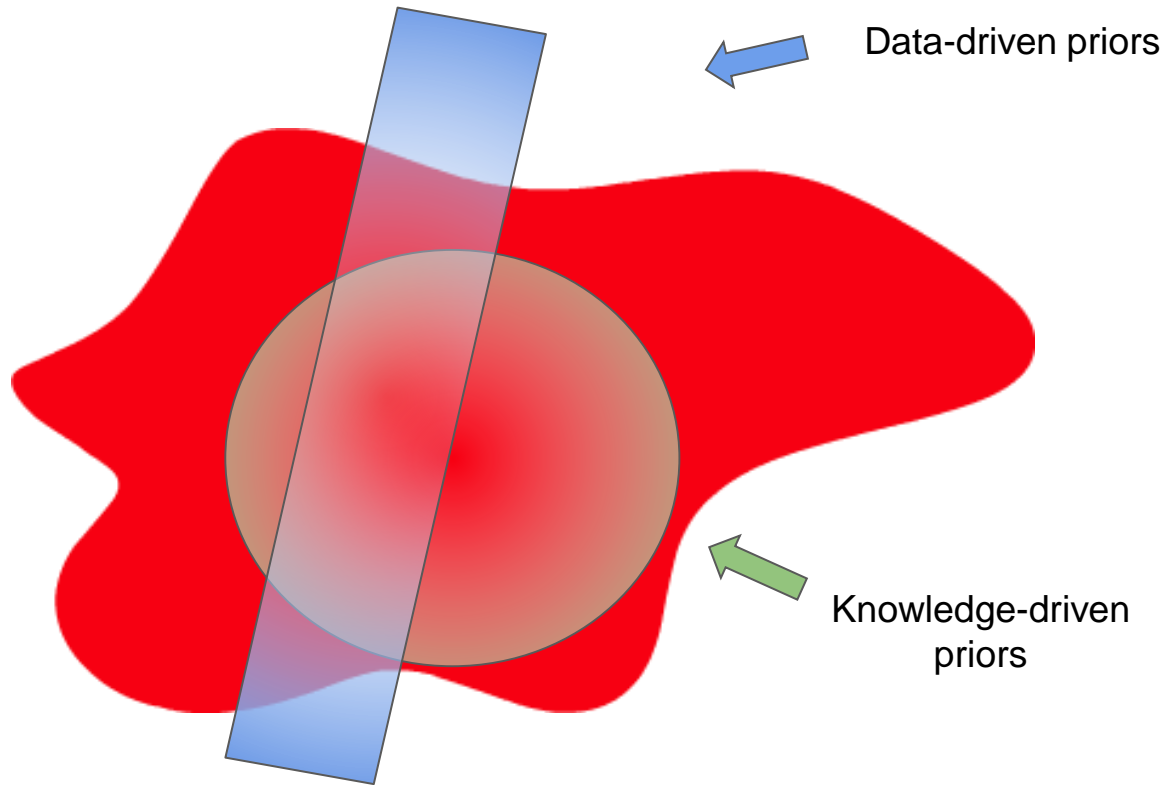
Knowledge vs data driven priors



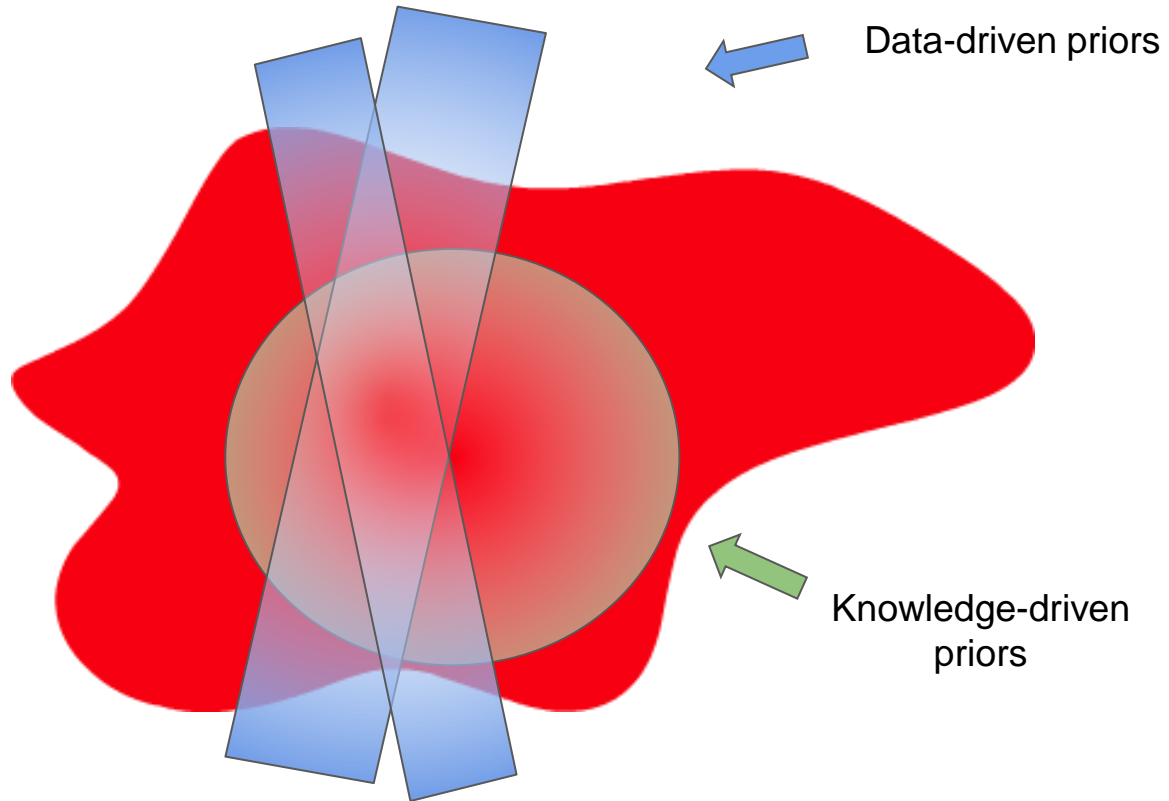
Knowledge vs data driven priors



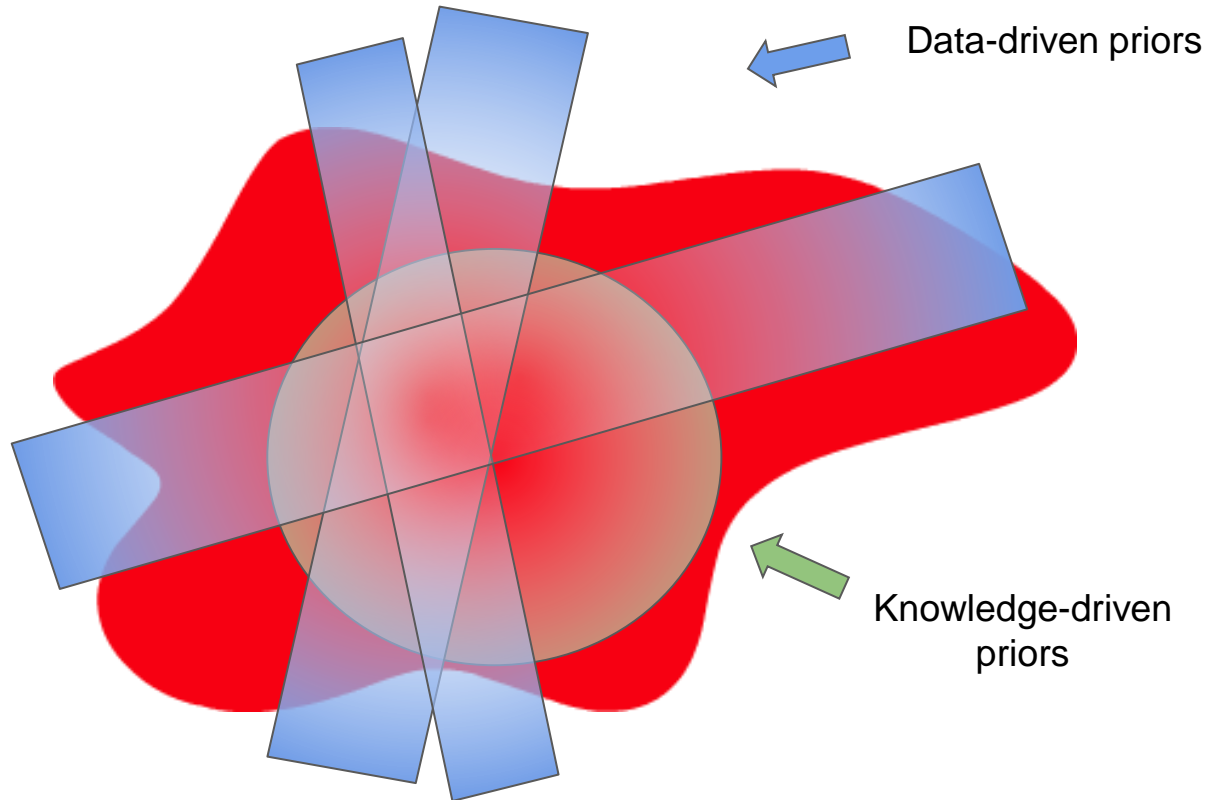
Knowledge vs data driven priors



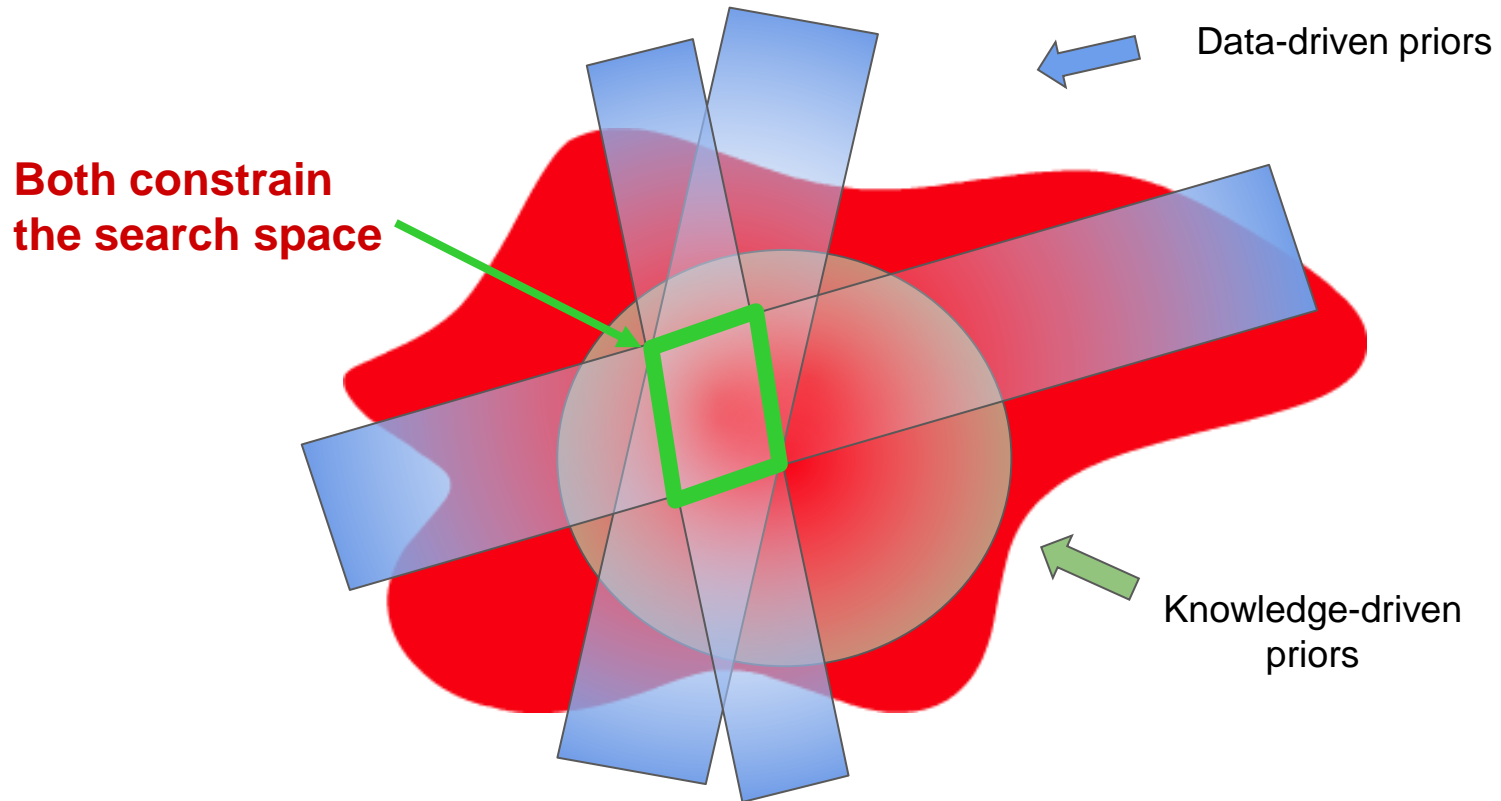
Knowledge vs data driven priors



Knowledge vs data driven priors



Knowledge vs data driven priors

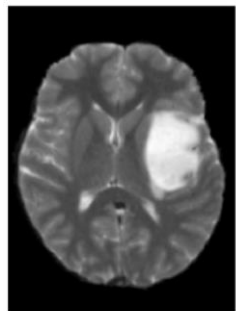


From global cues to pixel labels

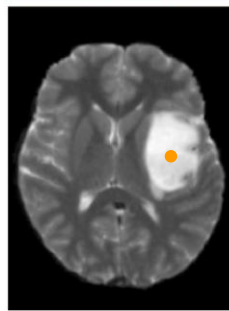
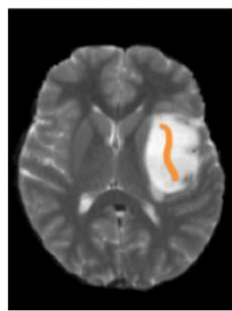
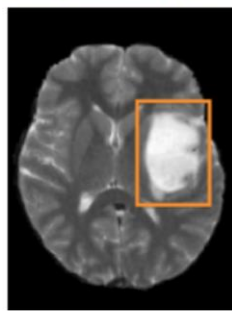


Person

Bike



Tumor



Original Image

Image tags

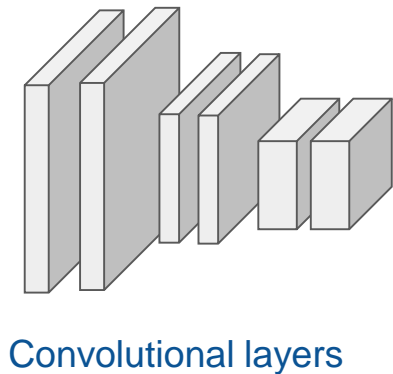
Bounding boxes

Scribbles

Points

From global cues to pixel labels

Step 1: Get a classification CNN



Convolutional layers



FC Layers

Class scores

○ Cat

○ Dog

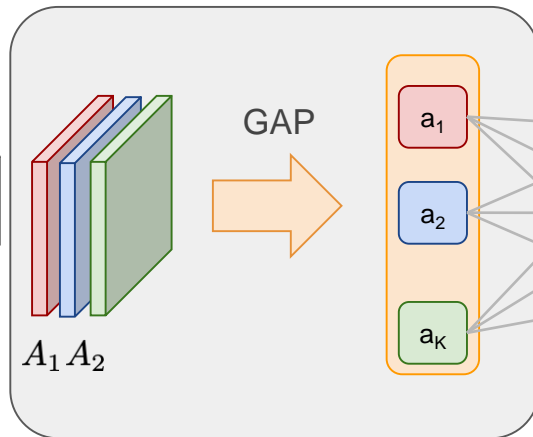
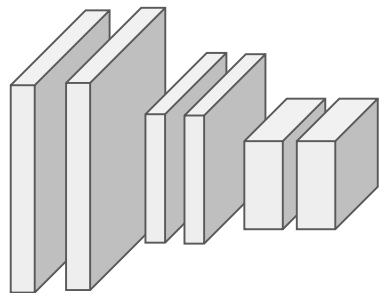
○ Parrot

From global cues to pixel labels

Step 2: Modify the last layers



Convolutional layers



Class scores

Cat
Dog
Parrot

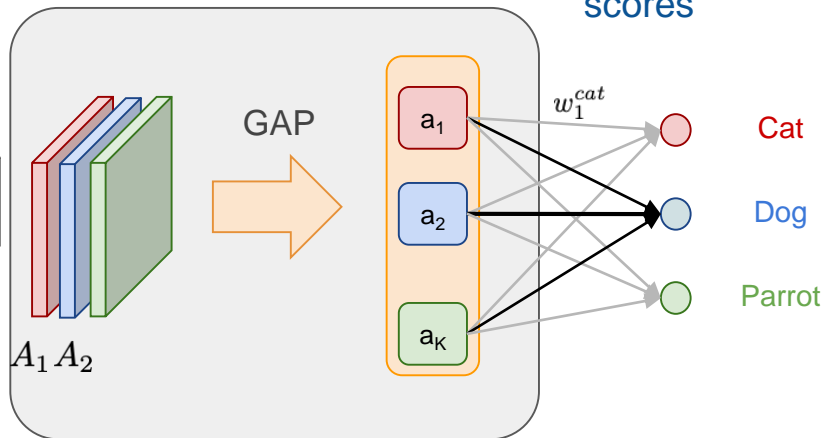
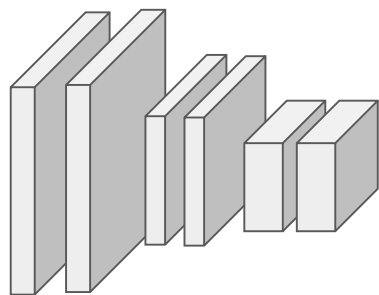
$$GAP(A_k) = a_k = \frac{1}{|N|} \sum_{x,y} A_k(x,y)$$

From global cues to pixel labels

Step 2: Modify the last layers



Convolutional layers



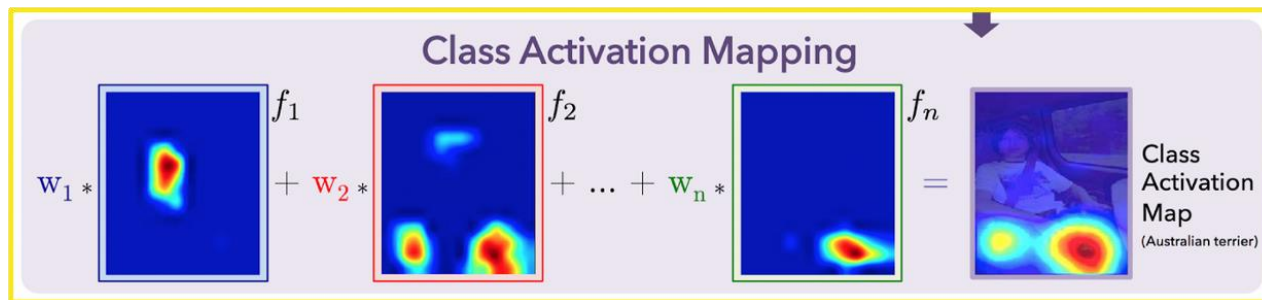
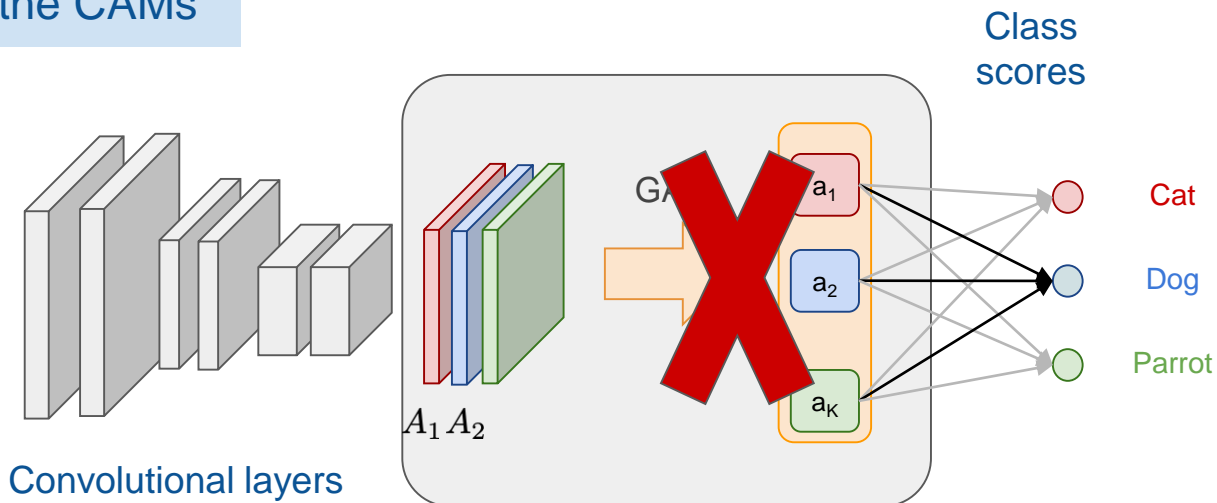
$$GAP(A_k) = a_k = \frac{1}{|N|} \sum_{x,y} A_k(x,y)$$

Class score
(logits)

$$S_c = \sum_k w_k^c a_k = \frac{1}{N} \sum_k w_k^c \sum_{x,y} a_k(x,y)$$

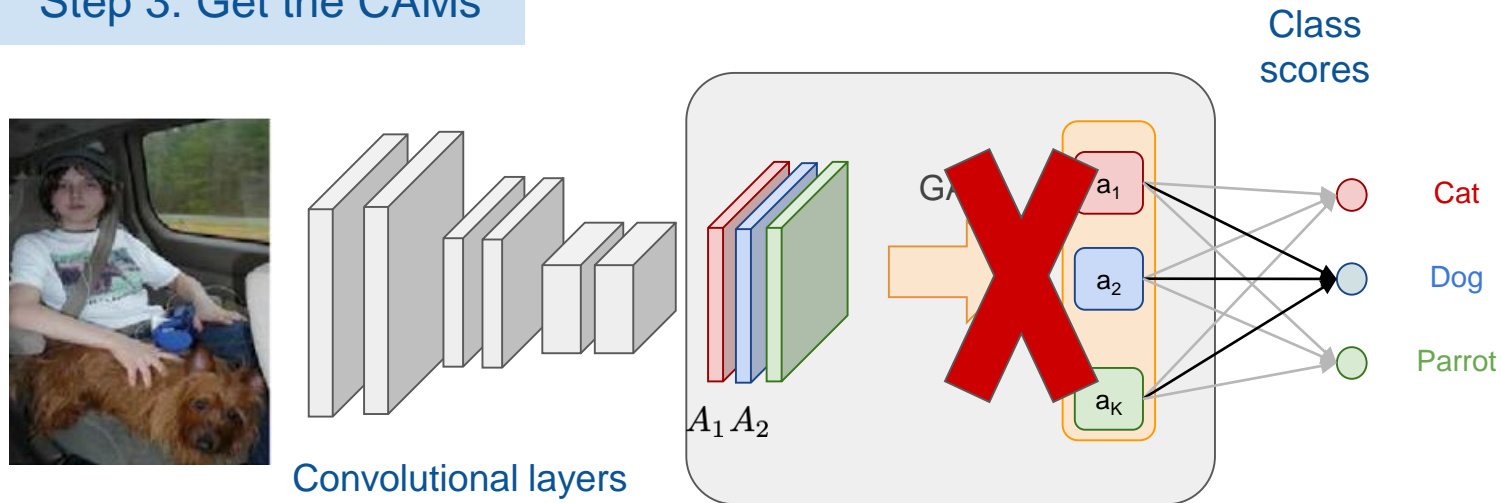
From global cues to pixel labels

Step 3: Get the CAMs



From global cues to pixel labels

Step 3: Get the CAMs



$$CAM_{Dog}(x, y) = \sum_k w_k^{Dog} A_k(x, y) =$$

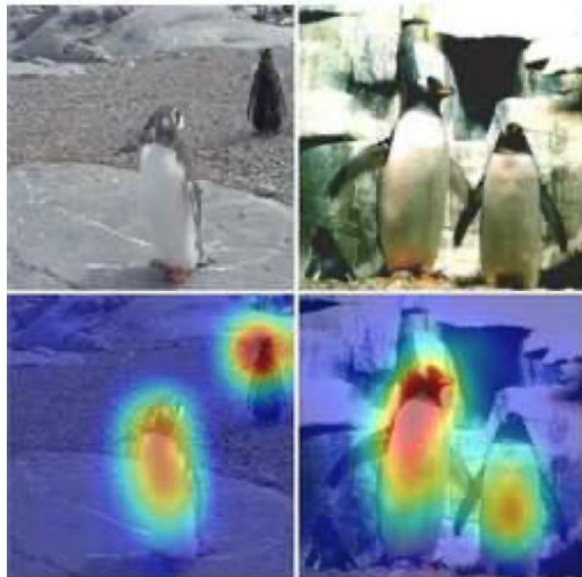


From global cues to pixel labels

Mushroom



Penguin



Teapot



- Zhou et al., Learning deep features for discriminative localization. CVPR 2016

From global cues to pixel labels

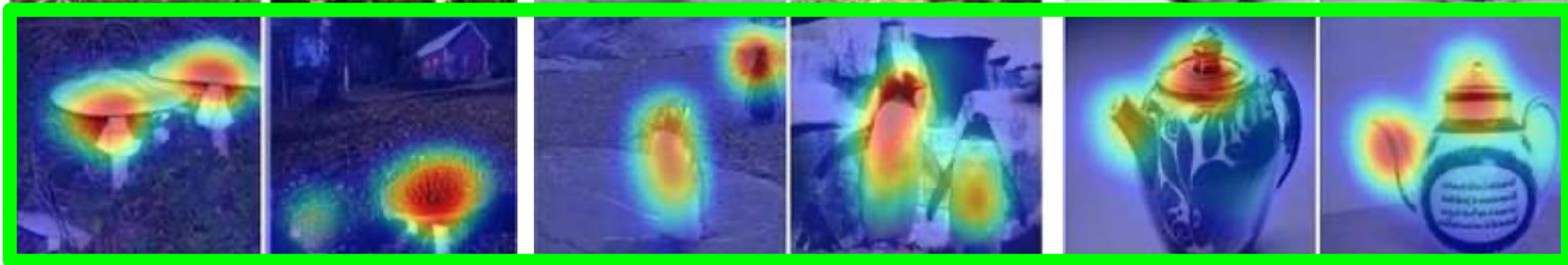
Mushroom



Penguin



Teapot



These activations maps can be used as **pseudo-masks**

$$- \sum_{i \in \Omega_i} \hat{y}_i \log(s_i)$$

- Zhou et al., Learning deep features for discriminative localization. CVPR 2016

From global cues to pixel labels

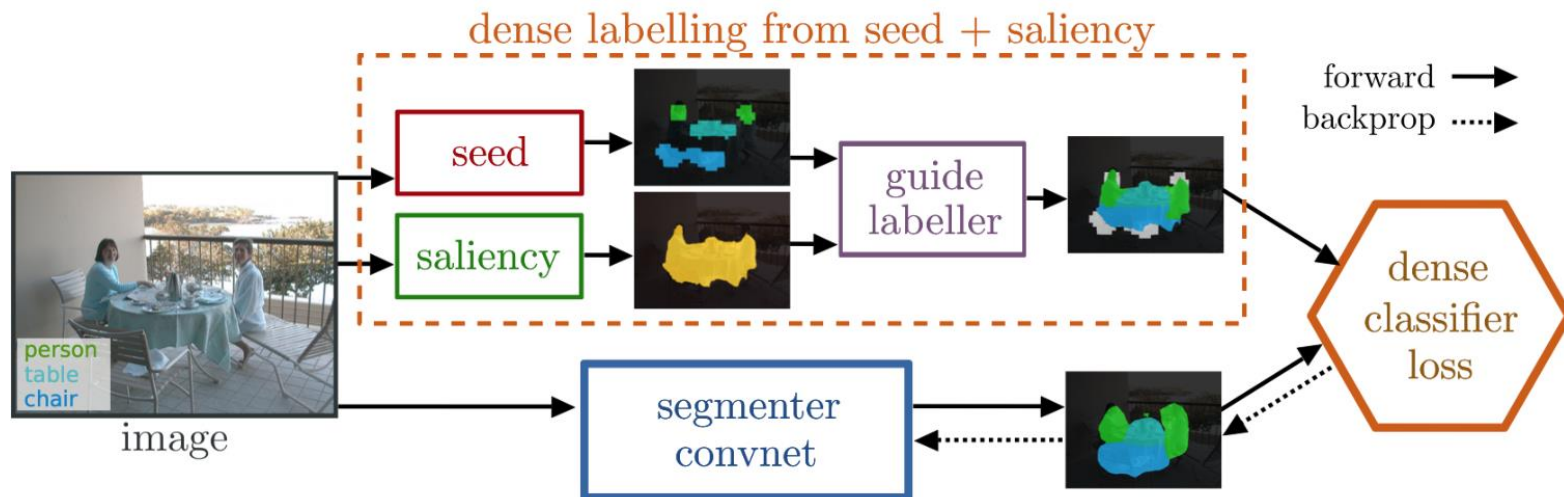
Problem: they focus only on highly discriminative regions



From global cues to pixel labels

How to improve CAMs?

Incorporate saliency maps

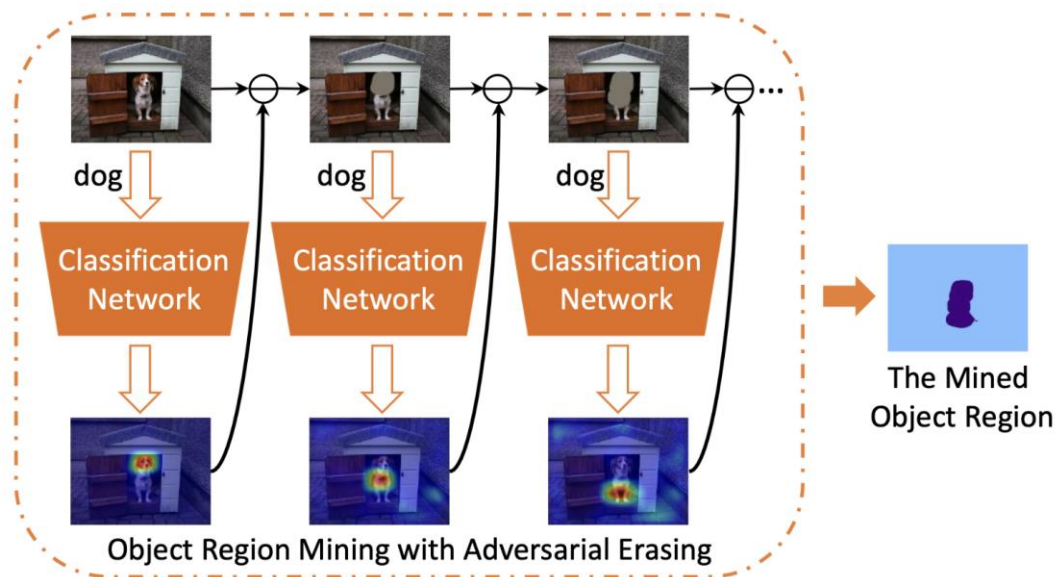


- Oh et al. Exploiting Saliency for Object Segmentation from Image Level Labels. CVPR 2017
- Fan et al. Learning Integral Objects With Intra-Class Discriminator for Weakly-Supervised Semantic Segmentation. CVPR 2020

From global cues to pixel labels

How to improve CAMs?

Region mining

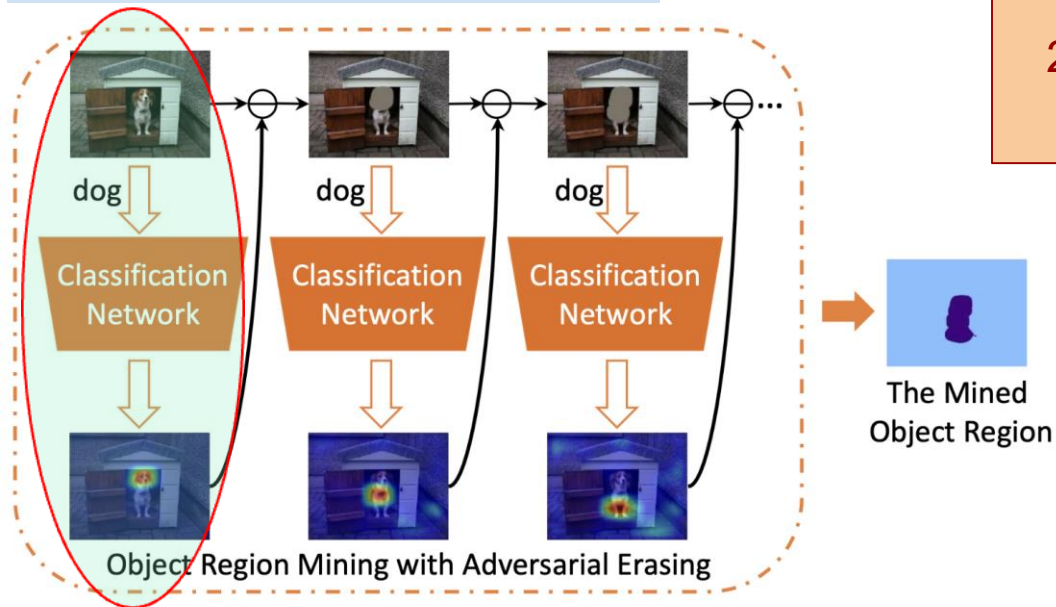


- Wei et al. Object Region Mining with Adversarial Erasing: A Simple Classification to Semantic Segmentation Approach. CVPR 2017
- Wang et al. Weakly-Supervised Semantic Segmentation by Iteratively Mining Common Object Features. CVPR 2018

From global cues to pixel labels

How to improve CAMs?

Region mining



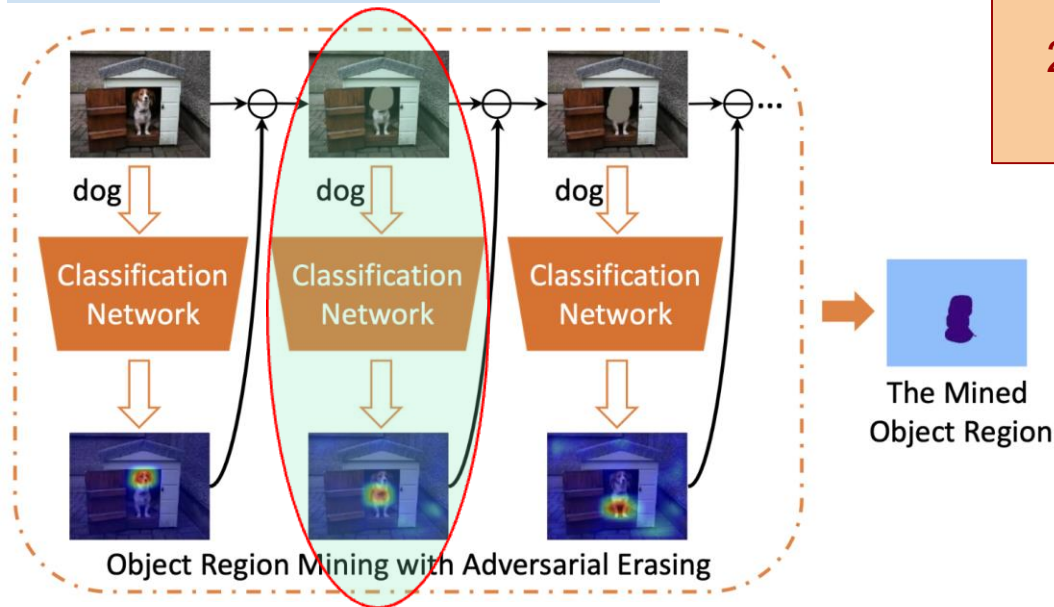
- 1 - Obtain CAM
- 2 - Mask image with that region
- 3 - Repeat

- Wei et al. Object Region Mining with Adversarial Erasing: A Simple Classification to Semantic Segmentation Approach. CVPR 2017
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From global cues to pixel labels

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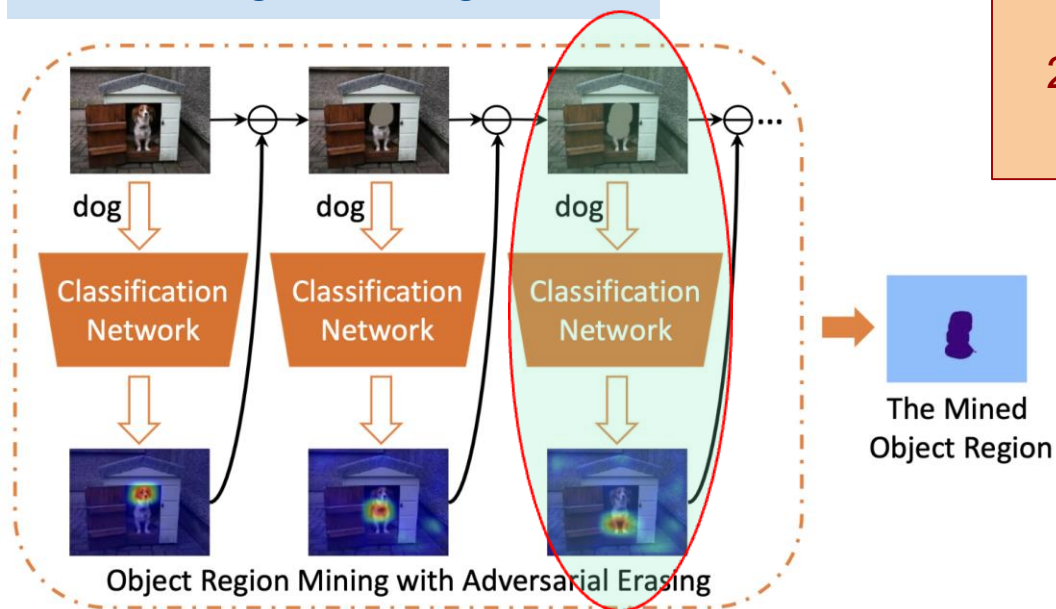
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From global cues to pixel labels

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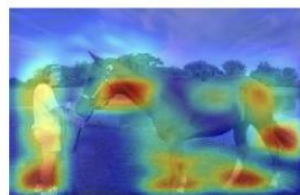
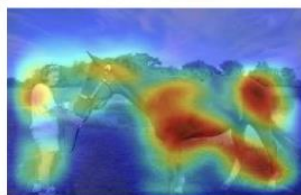
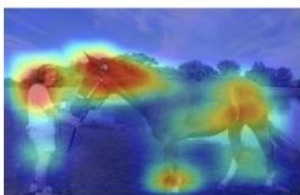
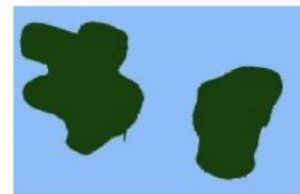
- 1 - Obtain CAM
- 2 - Mask image with that region
- 3 - Repeat

The Mined
Object Region

- Wei et al. Object Region Mining with Adversarial Erasing: A Simple Classification to Semantic Segmentation Approach. CVPR 2017
- Wang et al. Weakly-Supervised Semantic Segmentation by Iteratively Mining Common Object Features. CVPR 2018

From global cues to pixel labels

How to improve CAMs?



Image

AE-Step1

AE-Step2

AE-Step3

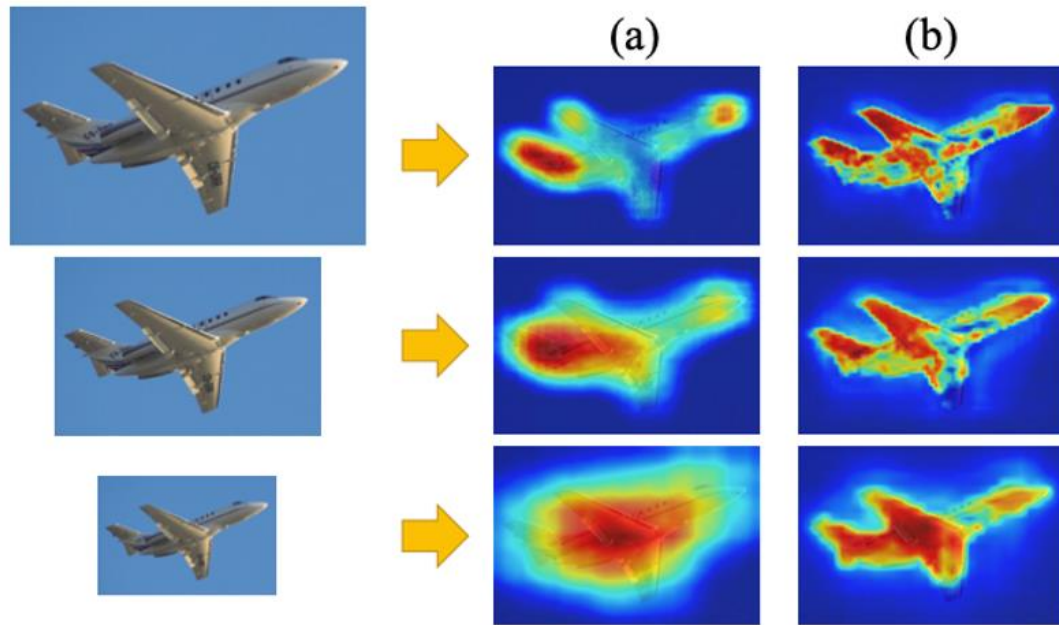
Object Region

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From global cues to pixel labels

How to improve CAMs?

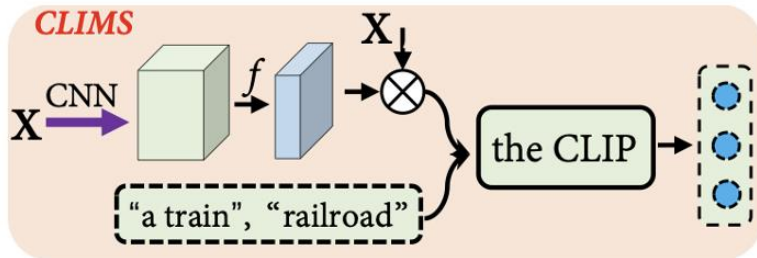
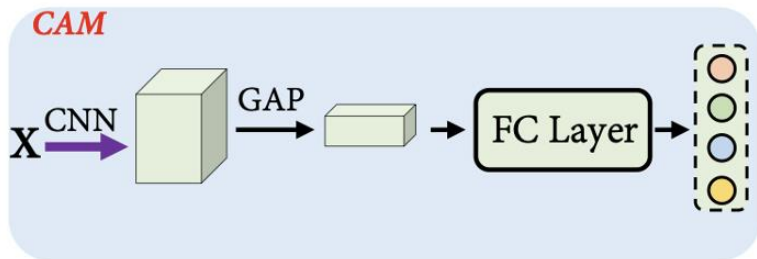
Equivariant constraints



From global cues to pixel labels

Integrating language-
vision models

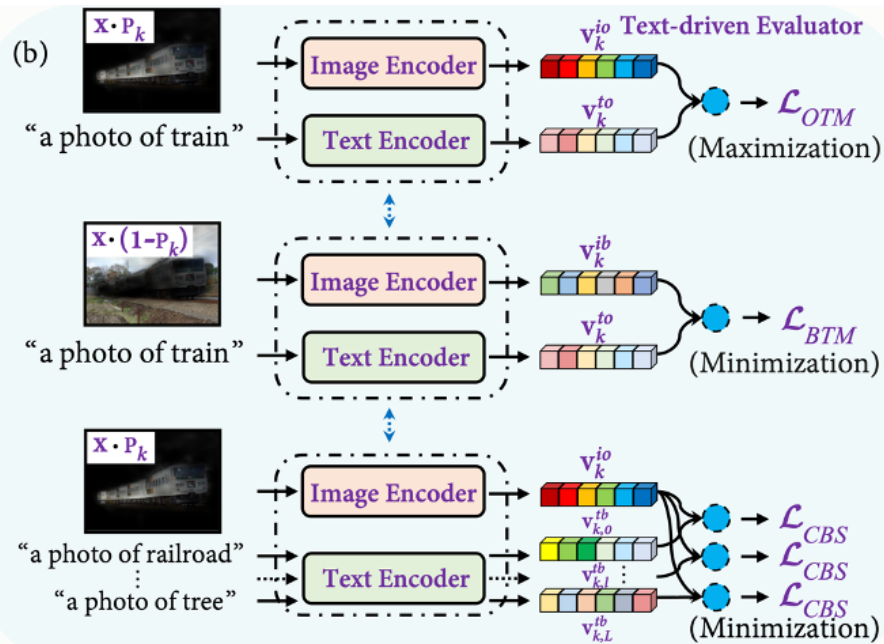
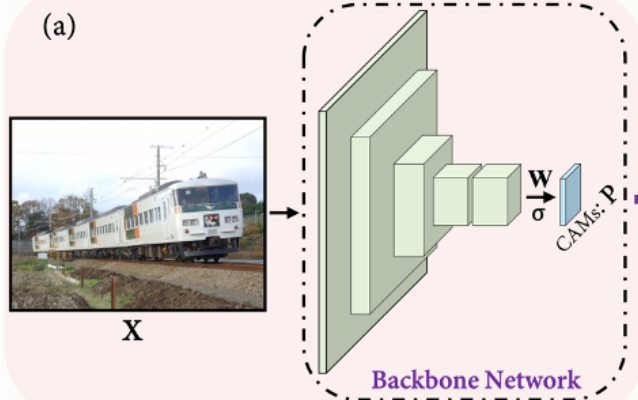
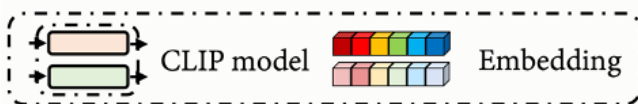
How to improve CAMs?



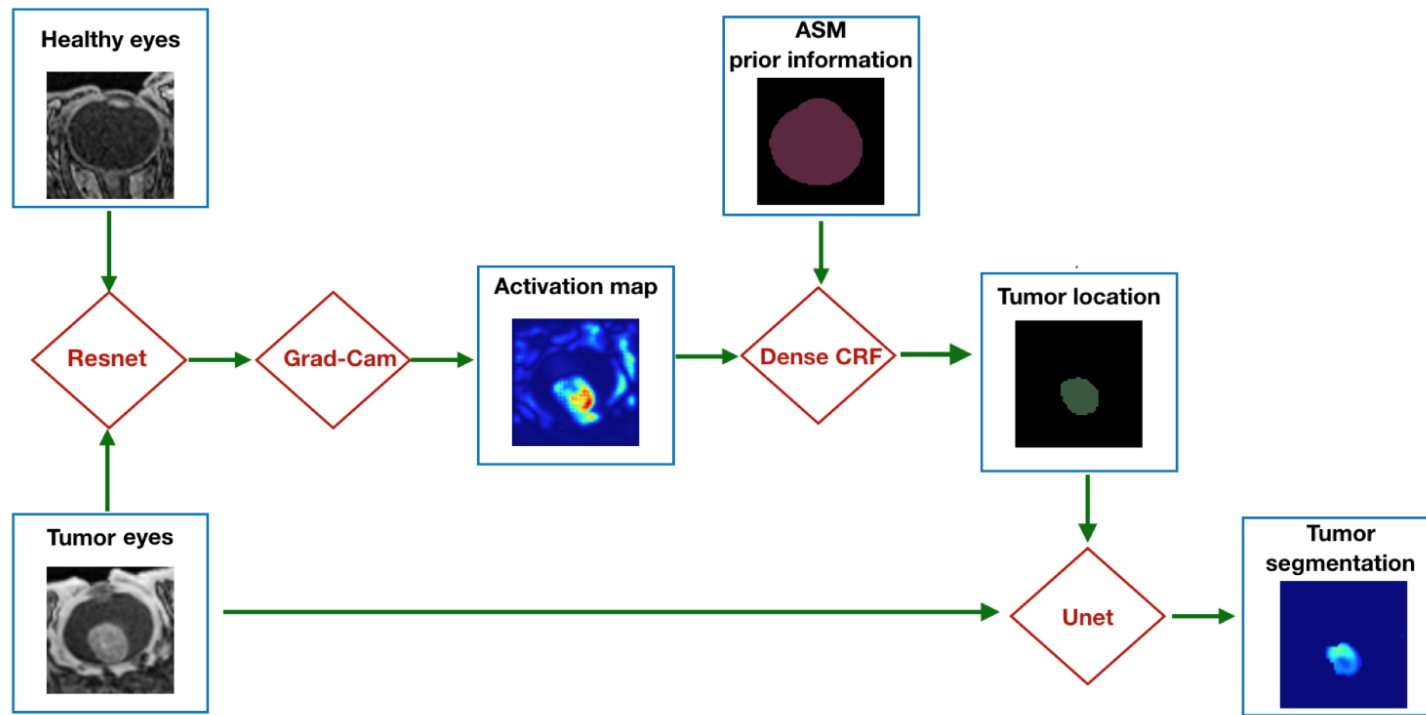
From global cues to pixel labels

Integrating language-vision models

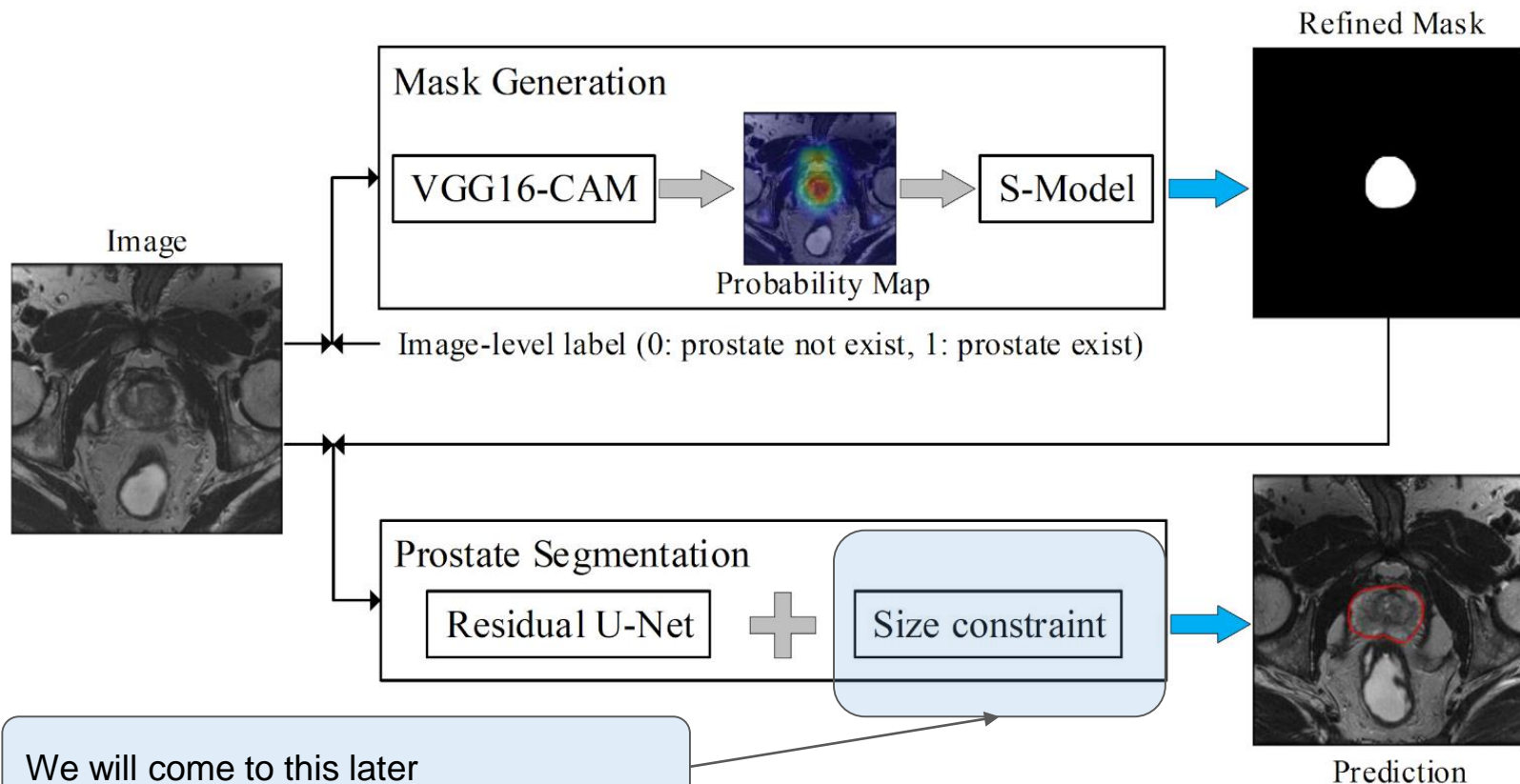
How to improve CAMs?



CAMs in the medical domain

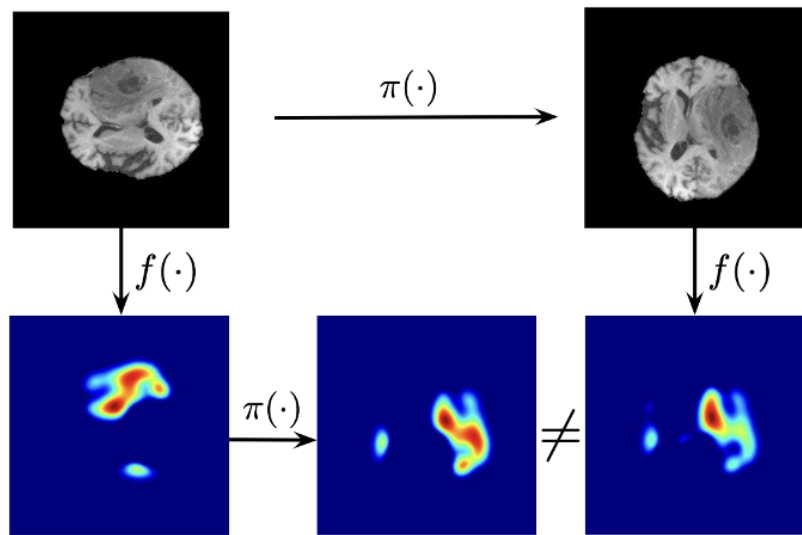


CAMs in the medical domain



CAMs in the medical domain

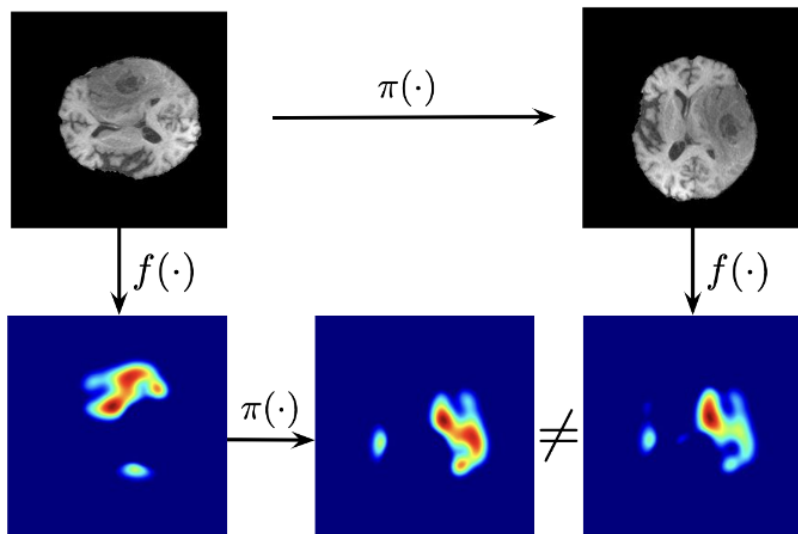
Equivariant constraints



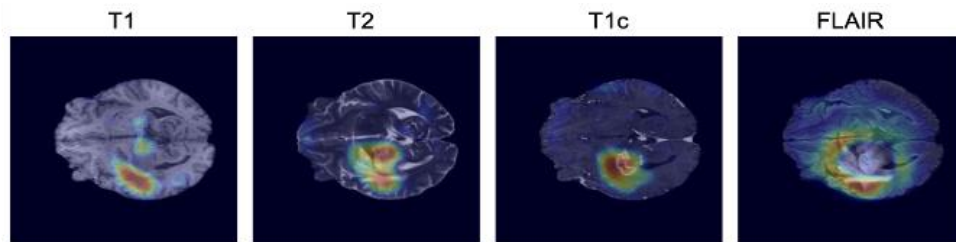
CAMs not equivariant to spatial transformations

CAMs in the medical domain

Equivariant constraints



CAMs not equivariant to spatial transformations



CAMs not consistent across modalities

CAMs in the medical domain

Equivariant constraints

Same-modality equivariant constraints

$$\mathcal{L}_{reg}(\tau(f(M_1)), f(\tau(M_1)))$$

transformations

Cross-modality equivariant constraints

$$\mathcal{L}_{reg}(\tau(f(M_1)), f(\tau(M_2)))$$

transformations

Modality 1

Modality 2

CAMs in the medical domain

Equivariant constraints

Same-modality equivariant constraints

$$\mathcal{L}_{reg}(\tau(f(M_1)), f(\tau(M_1)))$$

Cross-modality equivariant constraints

$$\mathcal{L}_{reg}(\tau(f(M_1)), f(\tau(M_2)))$$

Classification loss

$$\mathcal{L}_{class} + \mathcal{L}_{reg}(\tau(f(M_1)), f(\tau(M_1))) + \mathcal{L}_{reg}(\tau(f(M_1)), f(\tau(M_2)))$$

Intra-modal regularization

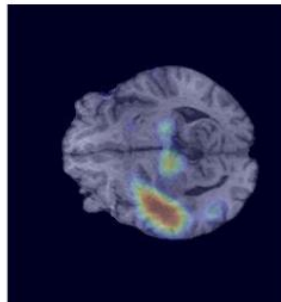
Inter-modal regularization

CAMs in the medical domain

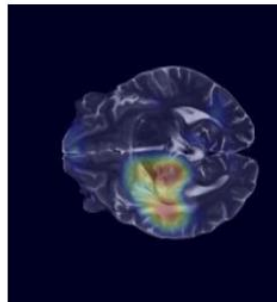
Equivariant constraints

Baseline

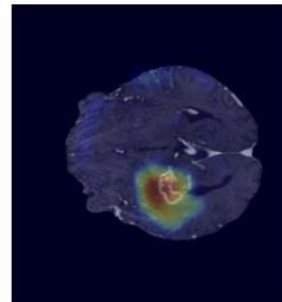
T1



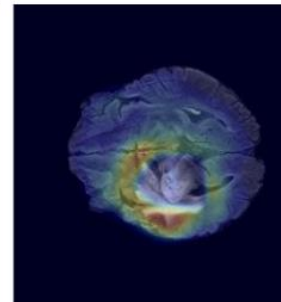
T2



T1c

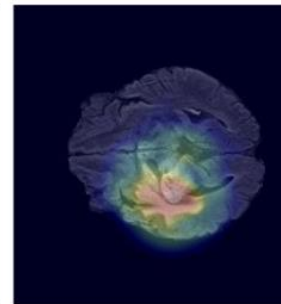
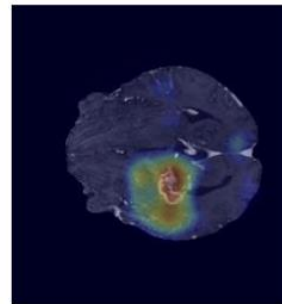
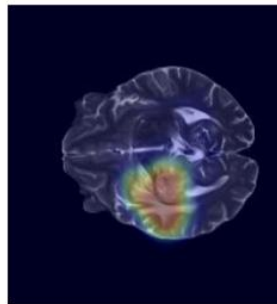
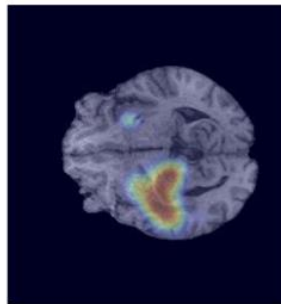


FLAIR



HIGH

Baseline
+ equivariant constraints



LOW

Constrained optimization (CNN)

Optimize (A)
↑
Task

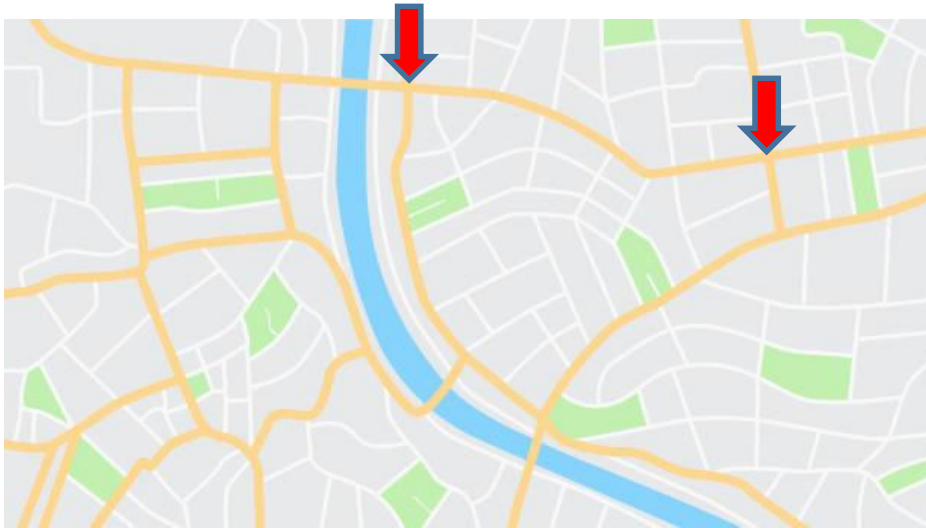
such that (B)
↑
Set of constraints

Constrained optimization (CNN)

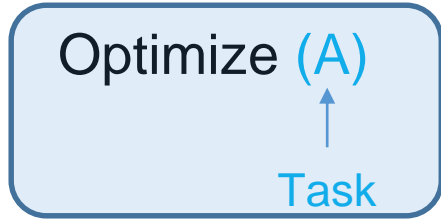
Optimize (A)
↑
Task

such that (B)
↑
Set of constraints

How we can go
from point A to B?

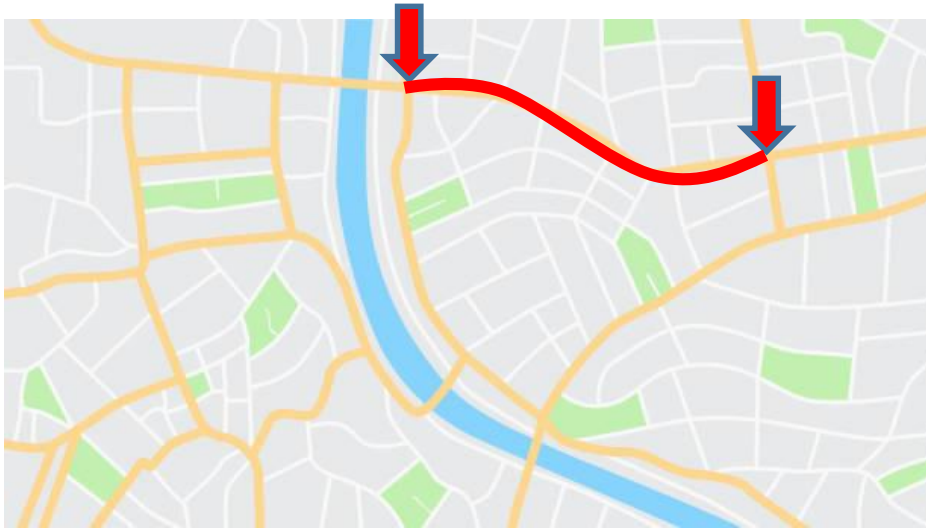


Constrained optimization (CNN)

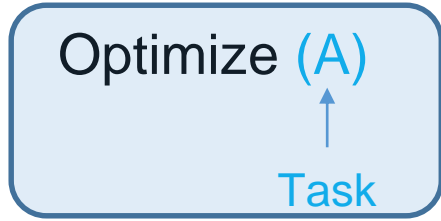


such that (B)
↑
Set of constraints

How we can go
from point A to B?



Constrained optimization (CNN)

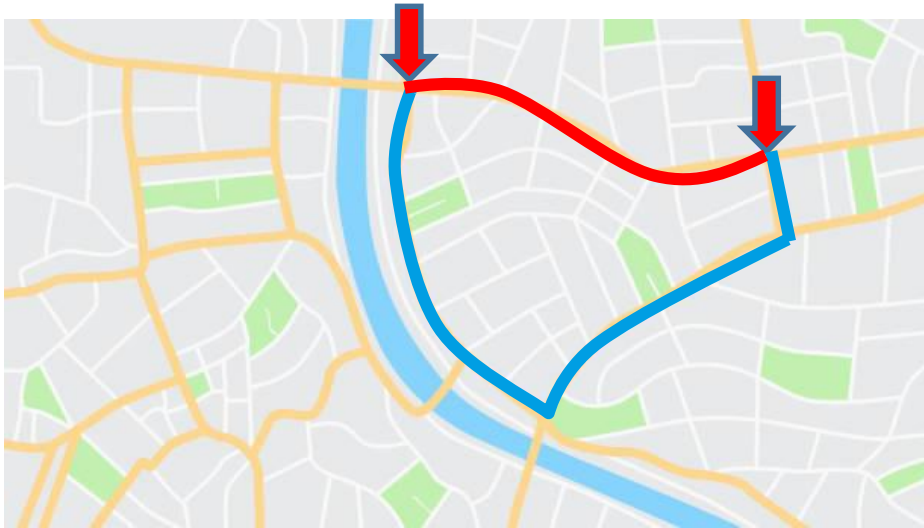


such that (B)
↑
Set of constraints

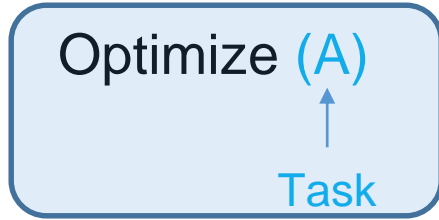
The text "such that (B)" is in black. Below it is a green upward-pointing arrow, and below the arrow is the text "Set of constraints" in green.

How we can go
from point A to B?

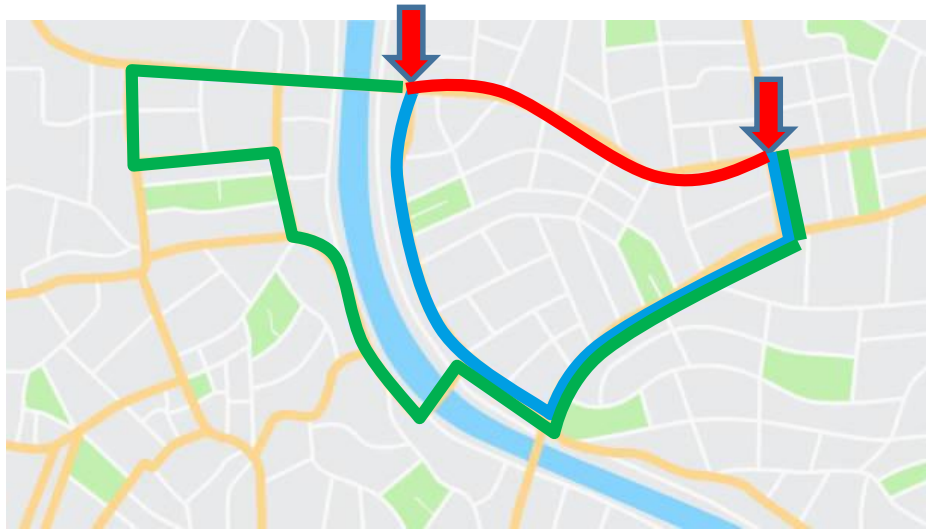
Text inside a light brown rounded rectangle.



Constrained optimization (CNN)



such that (B)
↑
Set of constraints



How we can go
from point A to B?

Which is the best
route?

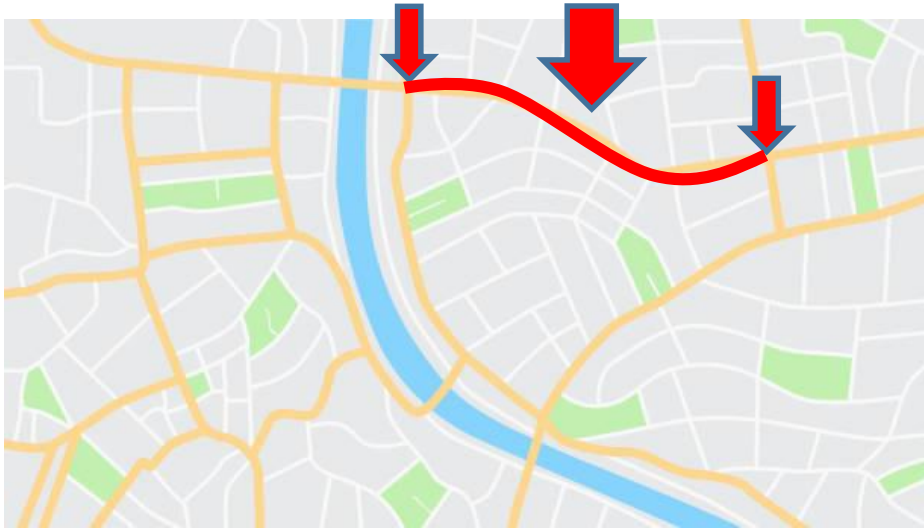
Constrained optimization (CNN)

Optimize (A)
↑
Task

such that (B)
↑
Set of constraints

How we can go
from point A to B?

Which is the best
route?
Constraint: shortest

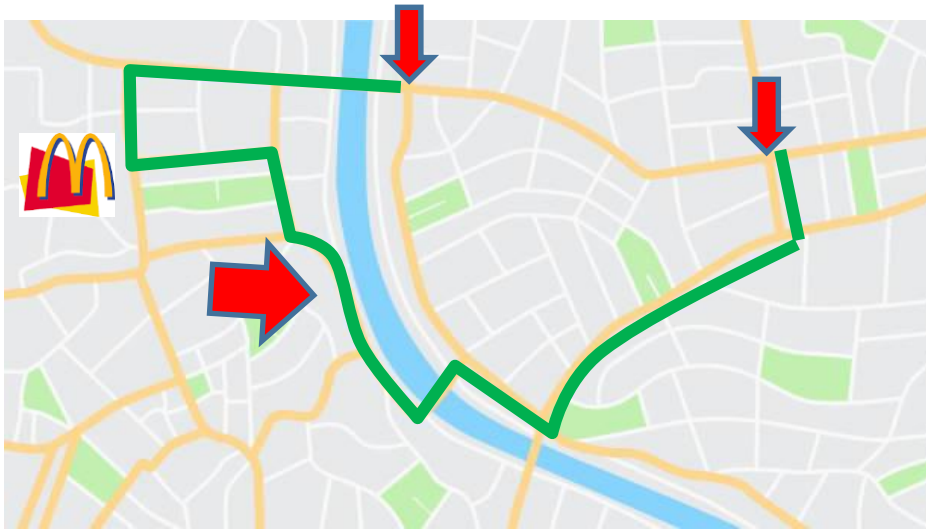


Constrained optimization (CNN)

Optimize (A)
↑
Task

such that (B)
↑
Set of constraints

How we can go from point A to B?



Which is the best route?
Constraint: shortest but going through a McDonalds

Constrained optimization (CNN)

Optimize (A) such that (B)

$$\min_{\theta} \mathcal{H}(S, Y) \quad s.t. \quad \sum_{n=0}^N s_n = A$$

Constrained problem

Constrained optimization (CNN)

Optimize (A) such that (B)

$$\min_{\theta} \mathcal{H}(S, Y) \quad s.t. \quad \sum_{n=0}^N s_n = A$$

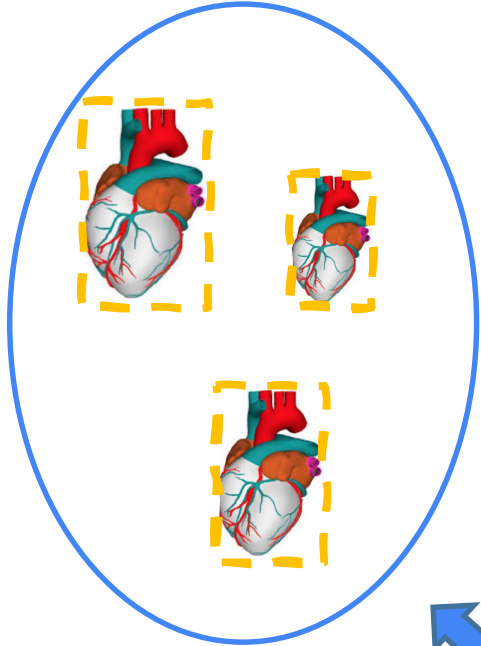
Constrained problem

$$\min_{\theta} \mathcal{H}(S, Y) + \lambda \left(\sum_{n=0}^N s_n - A \right)$$

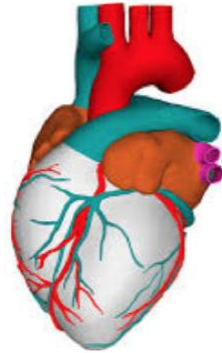
Unconstrained problem
(penalties to the rescue!)

Equality constraints

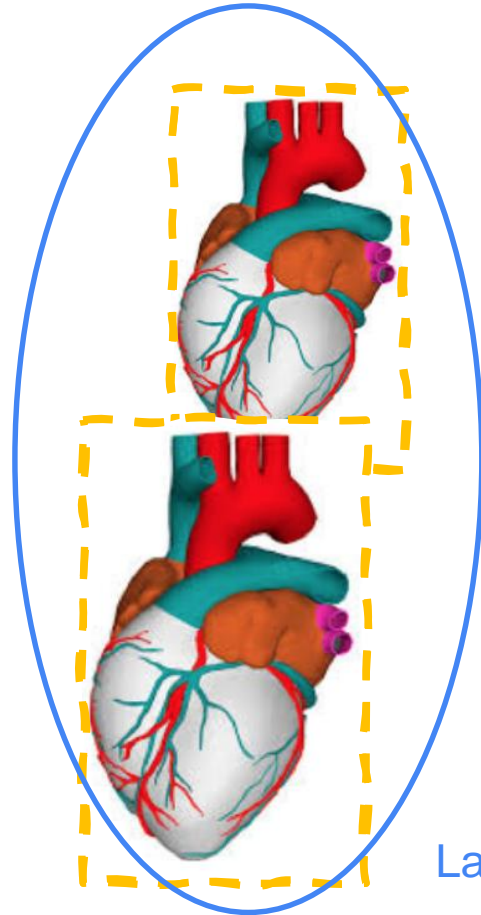
$$A=B$$



Smaller



Known size



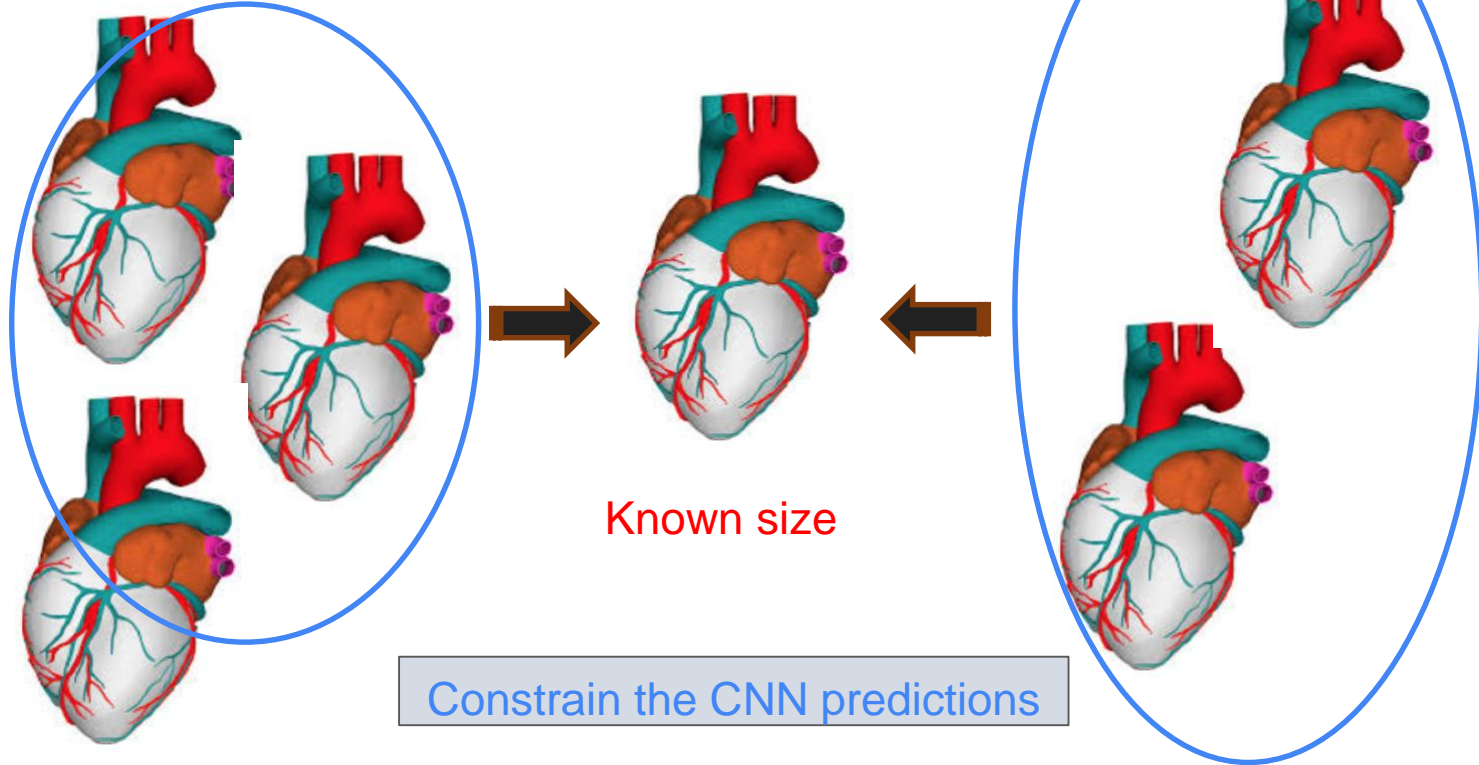
Larger



CNN predictions

Equality constraints

$$A=B$$



Equality constraints

A=B

General definition

$$\min_{\theta} \mathcal{H}(S) \quad s.t. \quad g(\mathbf{s}) = C$$

Constraint


Equality constraints

A=B

General definition

$$\min_{\theta} \mathcal{H}(S) \quad s.t. \quad g(\mathbf{s}) = C$$

Constraint


$$\min_{\theta} \mathcal{H}(S) + \lambda(g(\mathbf{s}) - C)$$

Penalty

Equality constraints

A=B

General definition

$$\min_{\theta} \mathcal{H}(S) \quad s.t. \quad g(\mathbf{s}) = C$$

Constraint

$$\min_{\theta} \mathcal{H}(S) + \lambda(g(\mathbf{s}) - C)$$

Penalty

This can be modeled with linear/quadratic penalties, KL divergence, etc

Equality constraints

L2 Penalty

Input
(Histology image)



Any CNN architecture

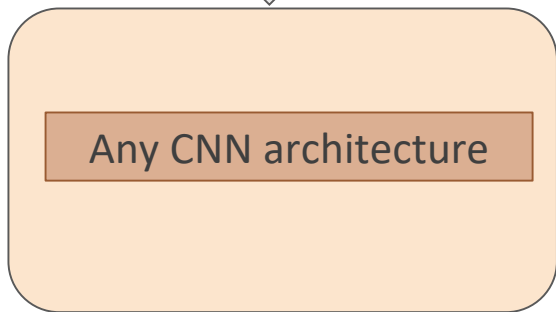


Output
(Pixel-wise prediction)

Equality constraints

L2 Penalty

Input
(Histology image)



Output
(Pixel-wise prediction)

Additional term

$$l_{ac} = \mathbf{I}(Y_i = 1) \sum_i (v_i - a_i)^2$$

Predicted relative
size (%)



$$v_i = \frac{1}{N} \sum_{p \in \Omega} s_{\theta}^{p,1}$$

Predicted size
given by experts

Equality constraints

Kullback-Leibler
(KL) Divergence

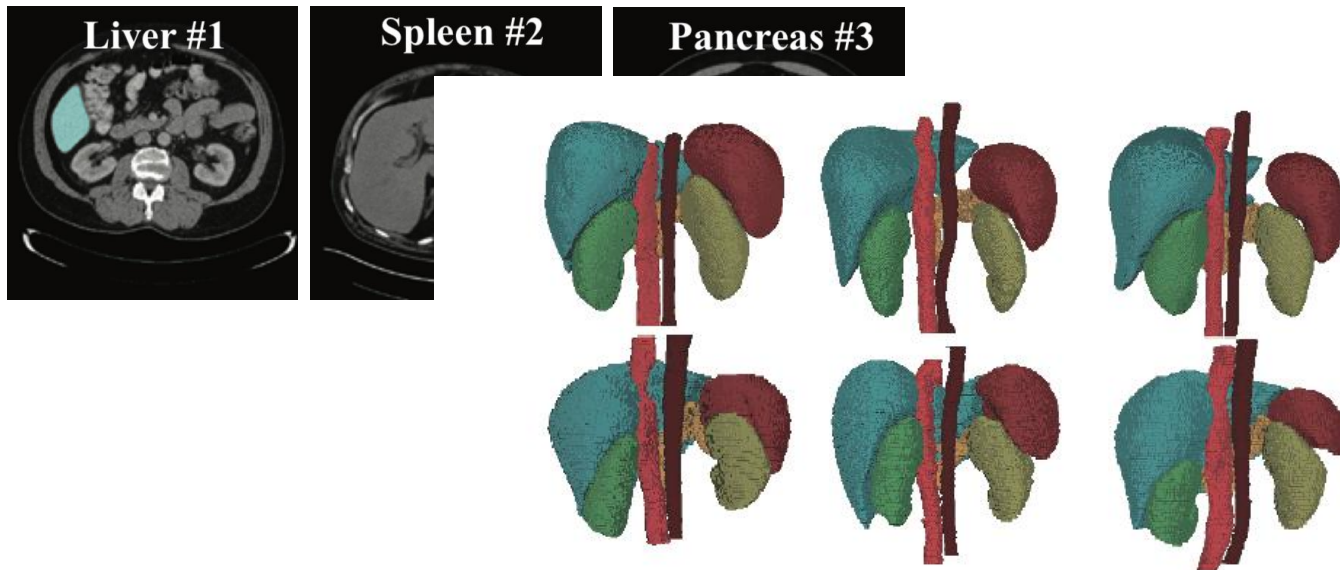
Partial annotations



Equality constraints

Kullback-Leibler
(KL) Divergence

Partial annotations



Prior on the proportion

Figure 1. 3D Visualization of several abdominal organs (liver, spleen, left kidney, right kidney, aorta, inferior vena cava) to show the similarity of patient-wise abdominal organ size distributions.

Equality constraints

Kullback-Leibler
(KL) Divergence

Partial annotations



Main objective:

$$\min \underbrace{\frac{1}{|\mathcal{L}|} \sum_{p \in \mathcal{L}} l(\mathbf{y}^p, \mathbf{s}_\theta^p)}_{\text{Fully labeled images}} + \underbrace{\lambda_1 \frac{1}{|\mathcal{P}|} \sum_{q \in \mathcal{P}} l(\mathbf{y}^q, \mathbf{s}_\theta^q)}_{\text{Partially labeled images}} + \lambda_2 \mathcal{J}(\theta)$$

Prior-aware loss

Fully labeled
images

Partially labeled images

Equality constraints

Kullback-Leibler
(KL) Divergence

Partial annotations



Prior-aware loss

Averaged predicted
distribution

$$\hat{\mathbf{p}} = \frac{1}{N} \sum_{p \in \mathcal{P}} \mathbf{s}_{\theta}^p \quad \rightarrow \quad [s_{\theta}^{p,0}, s_{\theta}^{p,1}, \dots, s_{\theta}^{p,|K|}]$$

On partially labeled images

Equality constraints

Kullback-Leibler
(KL) Divergence

Partial annotations



Prior-aware loss

Embed prior knowledge

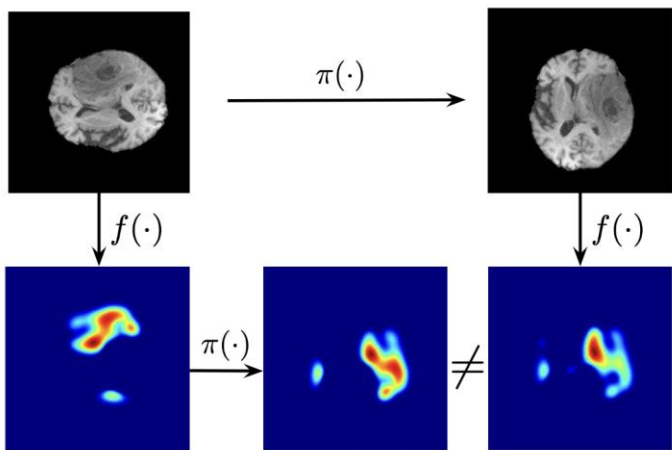
$$KL(\mathbf{q}|\hat{\mathbf{p}})$$

Real label distribution Average predicted distribution

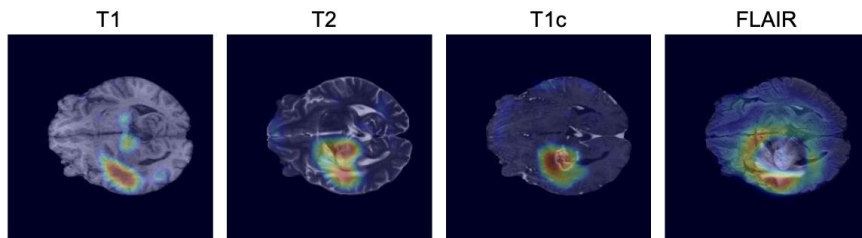
Equality constraints

At pixel level

Imposing Consistency across image modalities



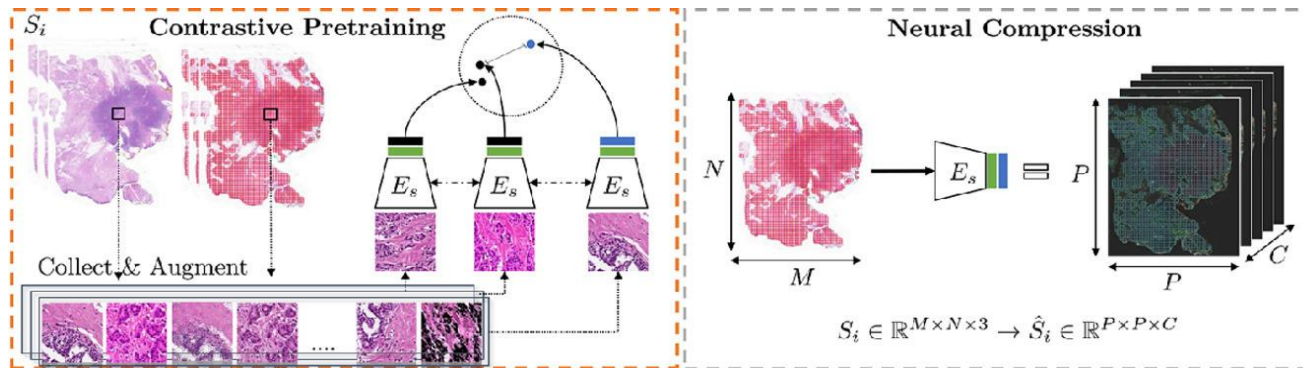
CAMs not equivariant to spatial transformations



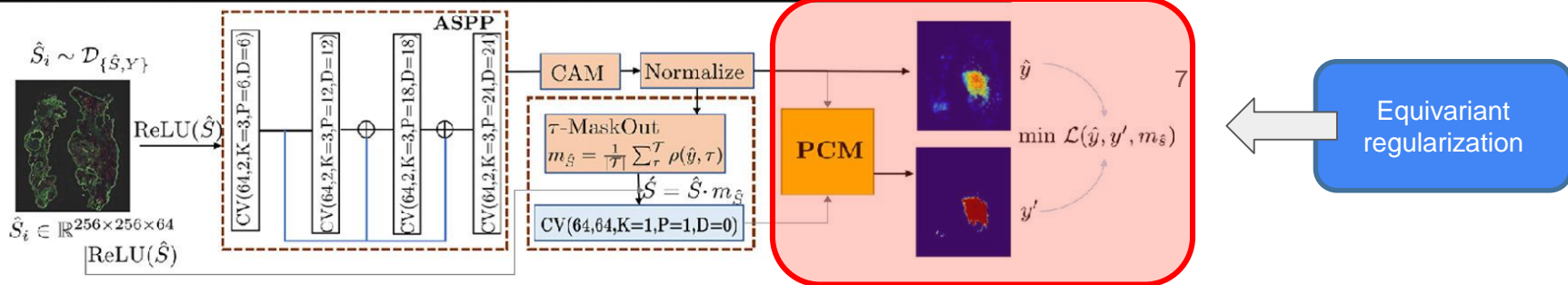
CAMs not consistent across modalities

Equality constraints

At pixel level

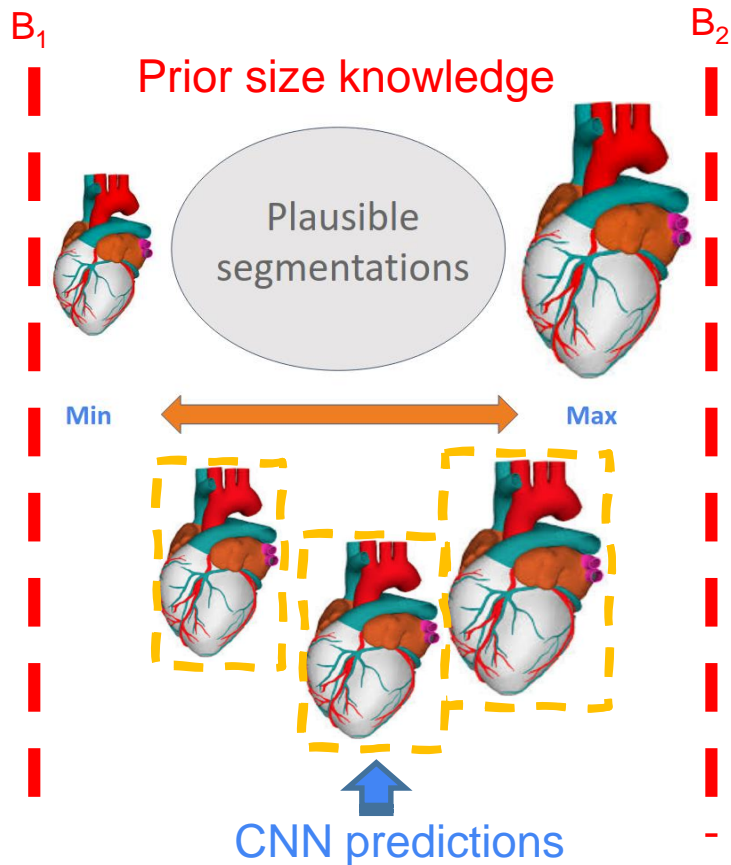


Single-Stage Masked Weakly Supervised Segmentation - WSS-SS



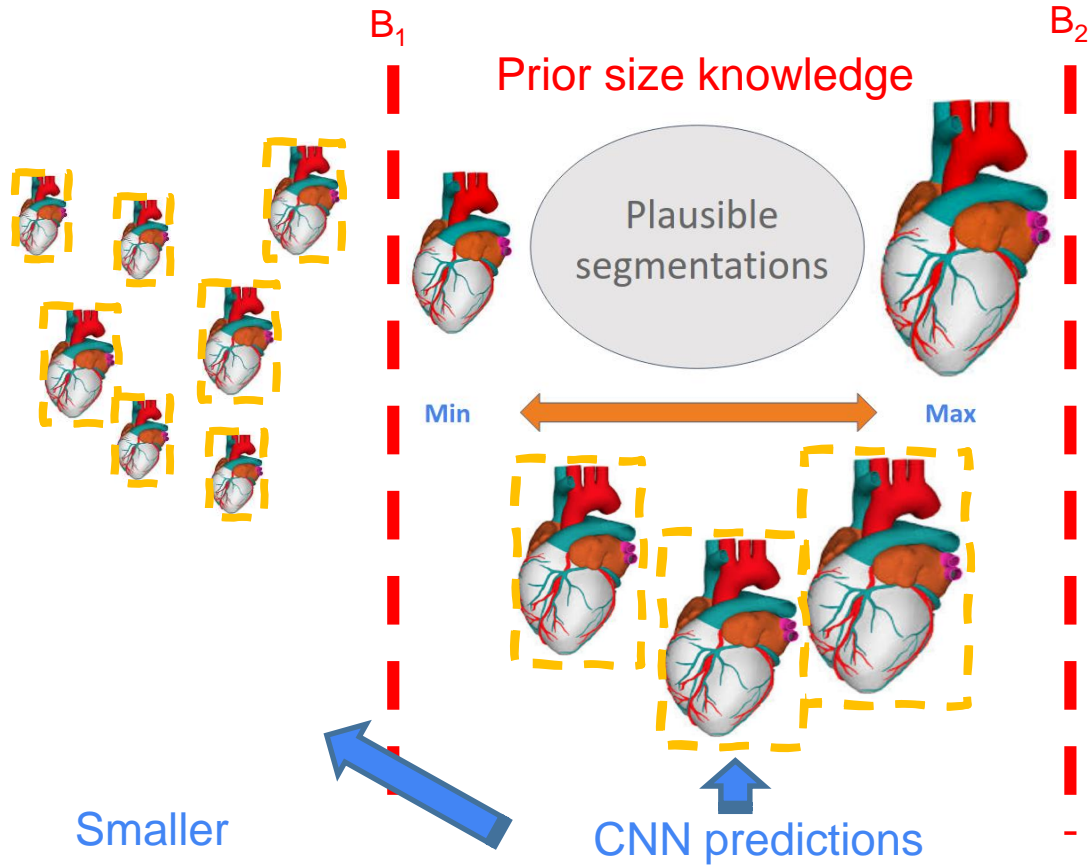
Inequality constraints

$A < B,$
 $A > B,$
 $B_1 < A < B_2$

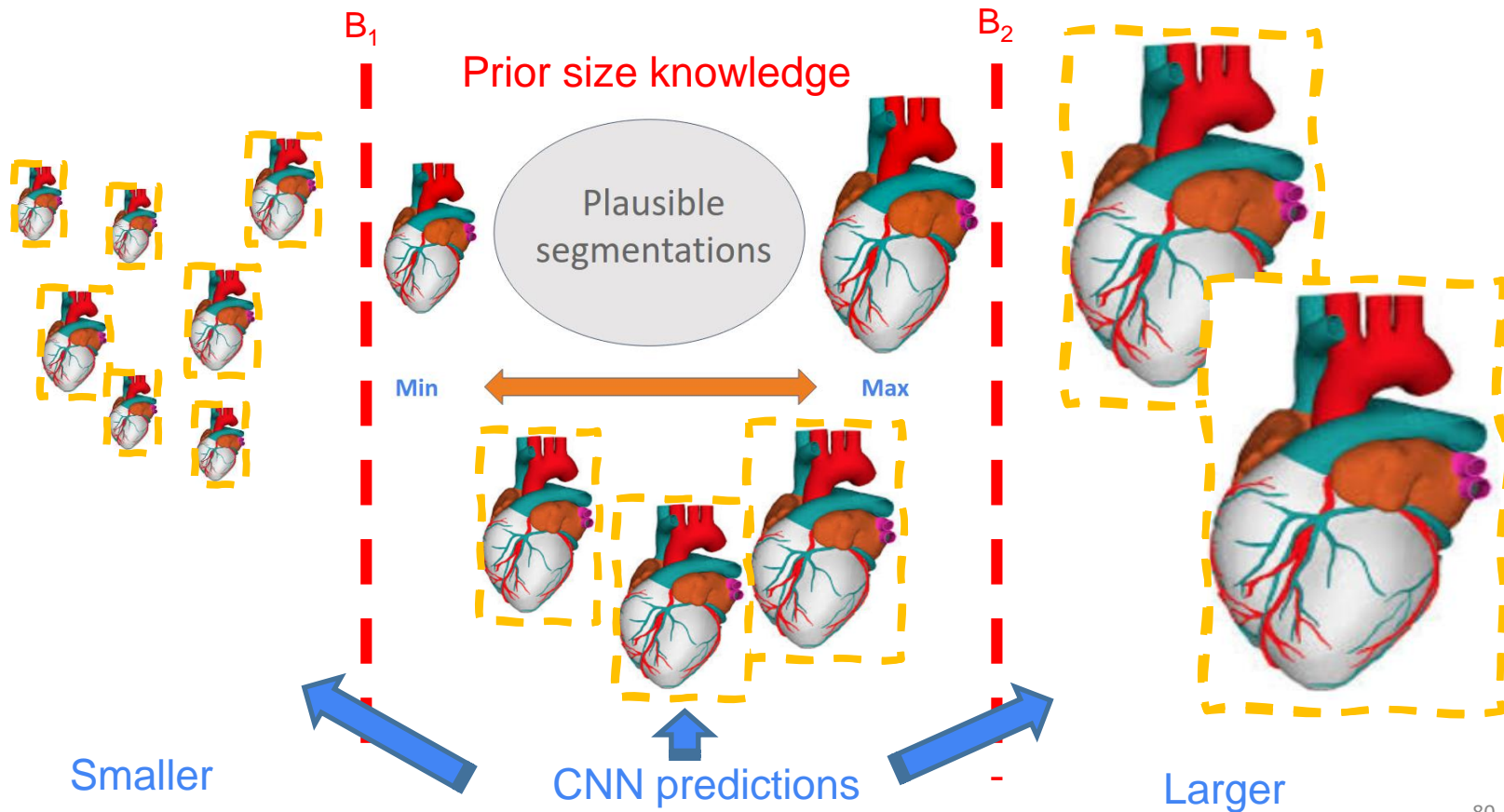


Inequality constraints

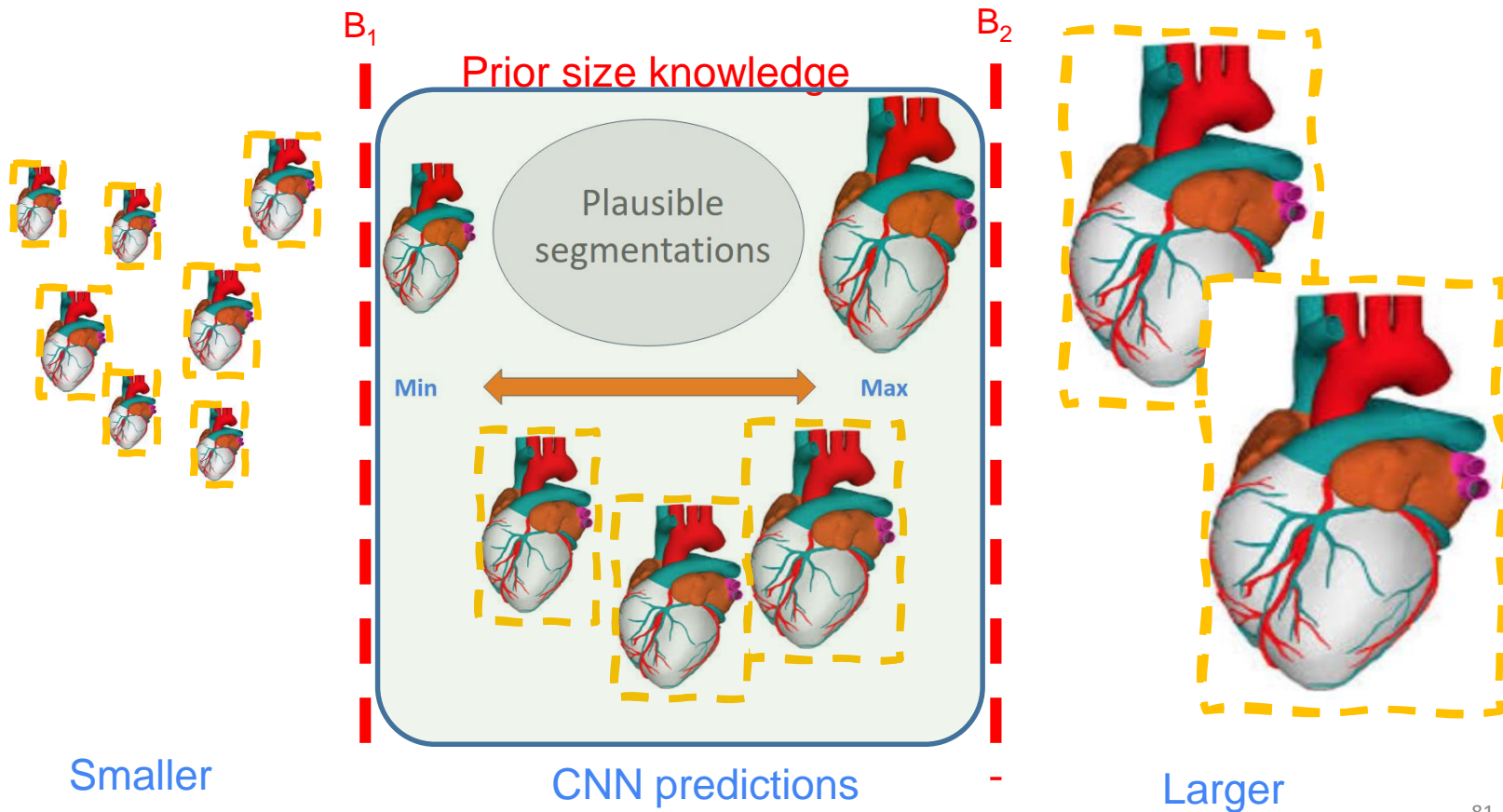
$A < B,$
 $A > B,$
 $B_1 < A < B_2$



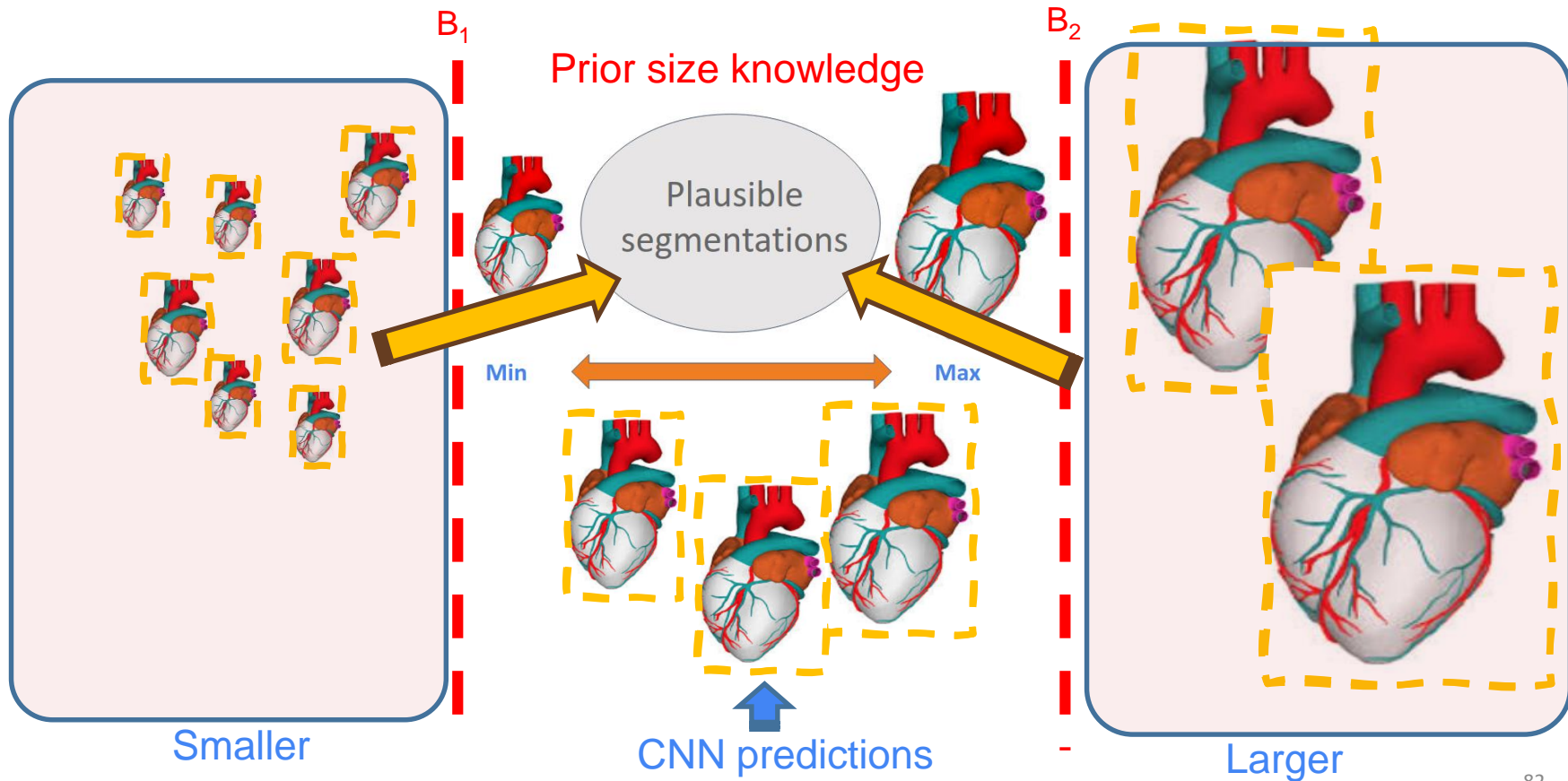
Inequality constraints



Inequality constraints



Inequality constraints



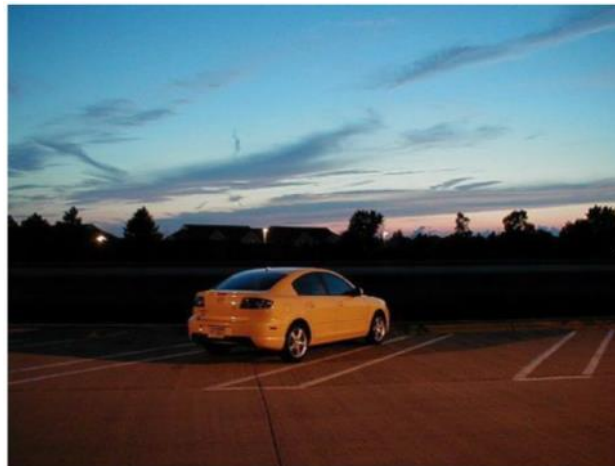
Inequality constraints

Information is given in the form of image-tags

Suppression

$$\sum_{p \in \Omega} s_{\theta}^{p,c} \leq 0 \quad \forall c \notin C$$

“Person”



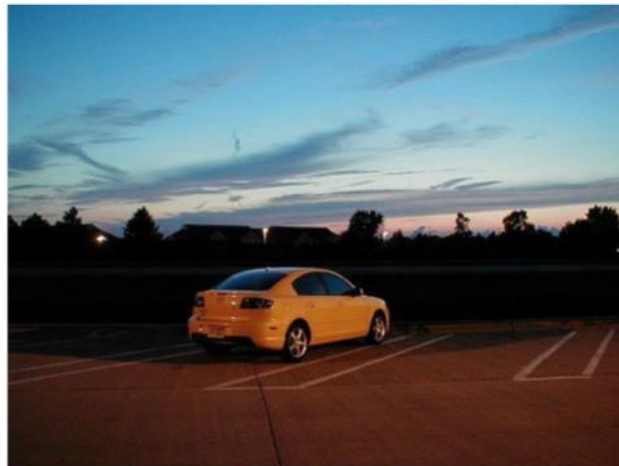
Inequality constraints

Information is given in the form of image-tags

**Inclusion
(or existence)**

$$\sum_{p \in \Omega} s_{\theta}^{p,c} \geq 1 \quad \forall c \in C$$

“Car”



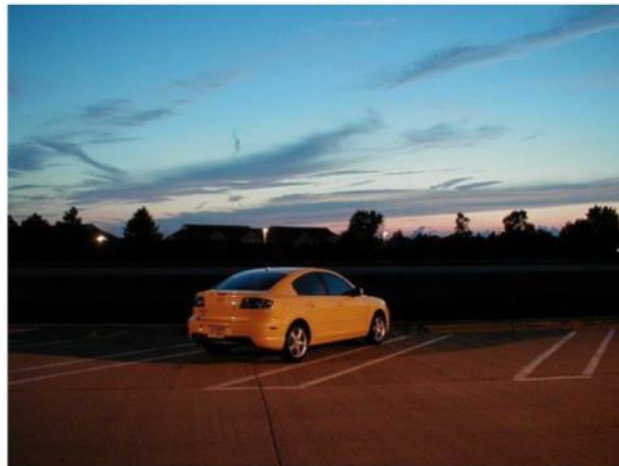
Inequality constraints

Information is given in the form of image-tags

Target Size
 $a > 1$

$$\sum_{p \in \Omega} s_{\theta}^{p,c} \geq a \quad \forall c \in C$$

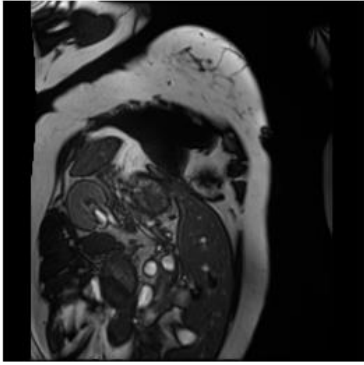
“Car”



Inequality constraints

Use case:
Size constraint

No cavity



Cavity

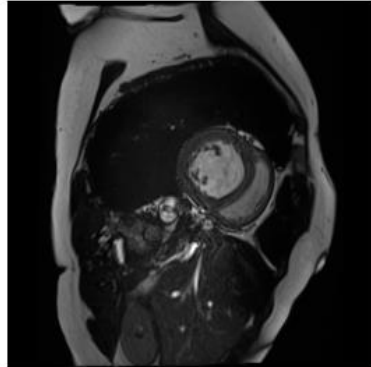


Image-tag information

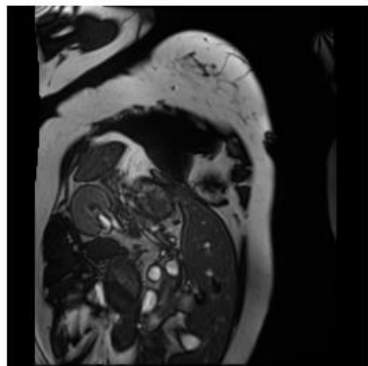
$$\sum_{p \in \Omega} s_{\theta}^{p,c} \leq 0$$

For negative image tags

Inequality constraints

Use case:
Size constraint

No cavity



Cavity

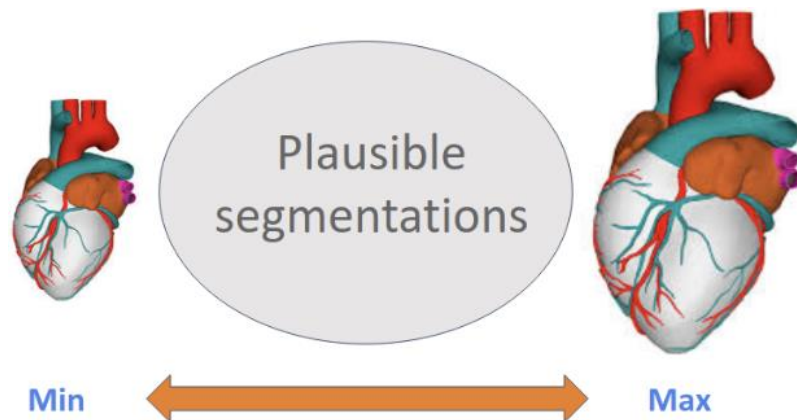
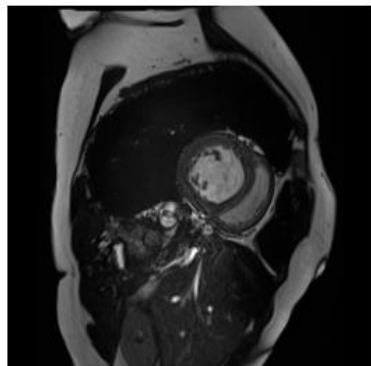


Image-tag information

$$\sum_{p \in \Omega} s_{\theta}^{p,c} \leq 0$$

For negative image tags

$$\min \leq \sum_{p \in \Omega} s_{\theta}^{p,c} \leq \max$$

For positive image tags

Inequality constraints

Formal definition

$$\min_{\theta} \mathcal{H}(S) \quad \text{s.t.} \quad a \leq \sum_{p \in \Omega} S_p \leq b$$

Inequality constraint

Use case:
Size constraint

Inequality constraints

Formal definition

Use case:
Size constraint

$$\min_{\theta} \mathcal{H}(S) \quad \text{s.t.} \quad a \leq \sum_{p \in \Omega} S_p \leq b \quad \longrightarrow \quad \mathcal{H}(S) + \lambda \mathcal{C}(V_S)$$

$$V_S = \sum_{p \in \Omega} \mathbf{s}_{\theta}^{p,c}$$

Inequality constraints

Formal definition

Use case:
Size constraint

$$\min_{\theta} \mathcal{H}(S) \quad \text{s.t.} \quad a \leq \sum_{p \in \Omega} S_p \leq b \quad \longrightarrow \quad \mathcal{H}(S) + \lambda \mathcal{C}(V_S)$$

$$\mathcal{H}(S) = - \sum_{p \in \mathcal{L}} \log(s_{\theta}^p)$$

$$V_S = \sum_{p \in \Omega} s_{\theta}^{p,c}$$

CE on the labeled pixels (if any)

Inequality constraints

Formal definition

Use case:
Size constraint

$$\min_{\theta} \mathcal{H}(S) \quad \text{s.t.} \quad a \leq \sum_{p \in \Omega} S_p \leq b \quad \longrightarrow \quad \mathcal{H}(S) + \lambda \mathcal{C}(V_S)$$

$$\mathcal{H}(S) = - \sum_{p \in \mathcal{L}} \log(s_{\theta}^p)$$

CE on the labeled pixels (if any)

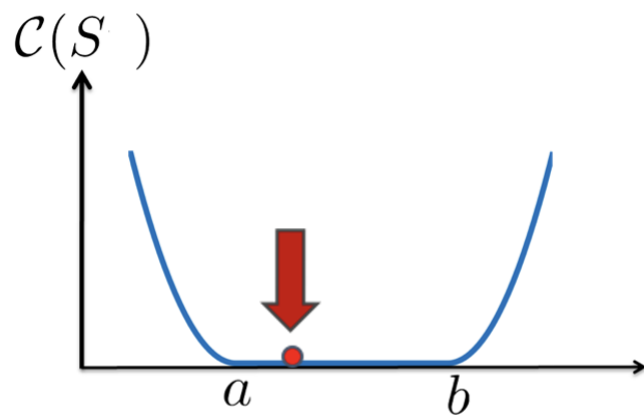
$$\mathcal{C}(V_S) = \begin{cases} (V_S - a)^2, & \text{if } V_S < a \\ (V_S - b)^2, & \text{if } V_S > b \\ 0, & \text{otherwise} \end{cases}$$

$$V_S = \sum_{p \in \Omega} s_{\theta}^{p,c}$$

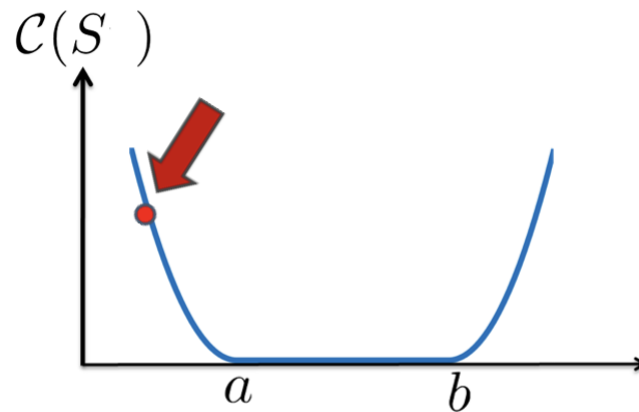
Inequality constraints

Visual intuition

Use case:
Size constraint



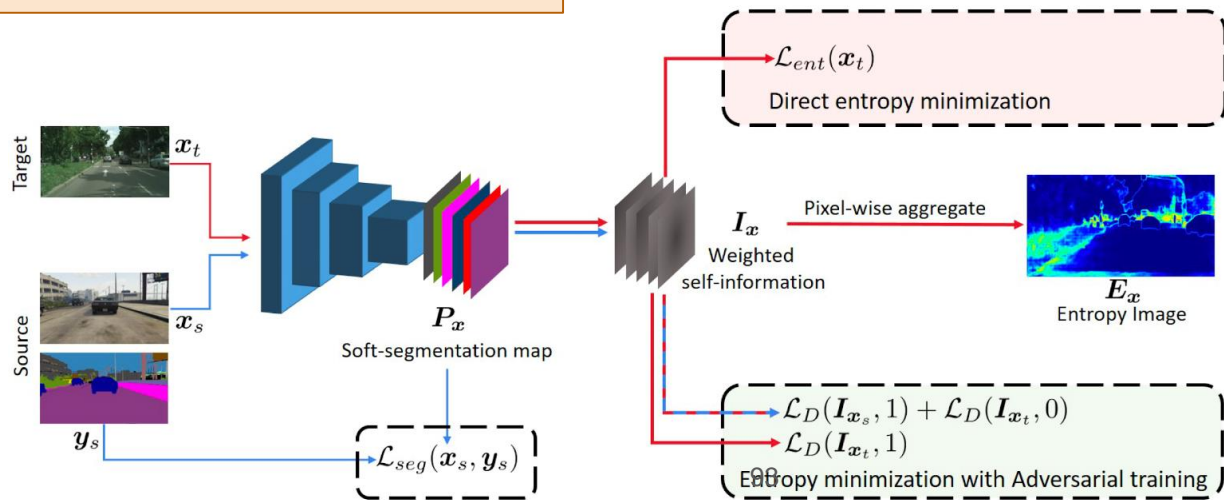
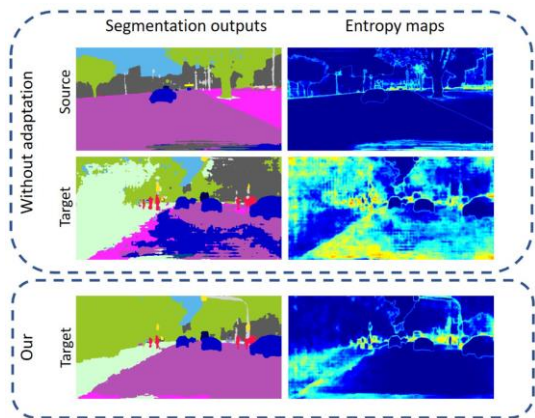
Constraint A satisfied



Constraint B violated

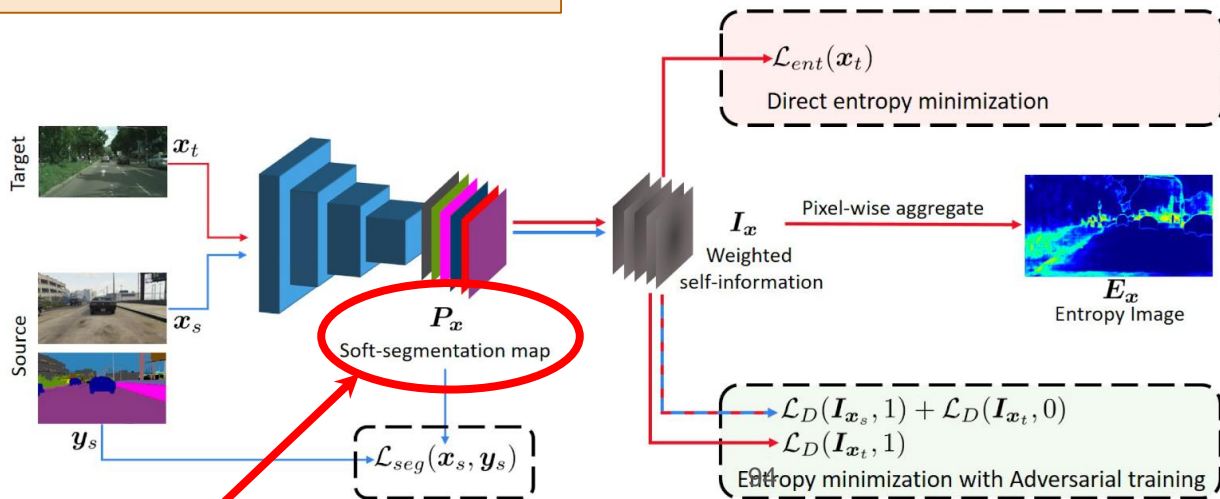
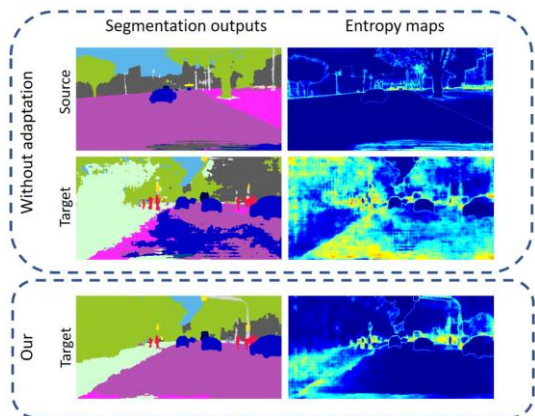
Inequality constraints

Information (proportion) is given as a prior



Inequality constraints

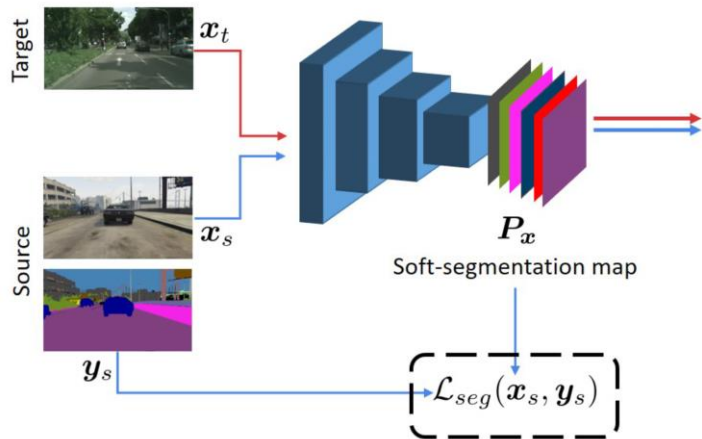
Information (proportion) is given as a prior



We focus on this now

Inequality constraints

Information (proportion) is given as a prior



Class-ratio priors

$$\mathcal{L}_{cp}(x_t) = \sum_{c=1}^C \max(0, \mu p_s^{(c)} - \mathbb{E}_c(P_{x_t}^{(c)}))$$

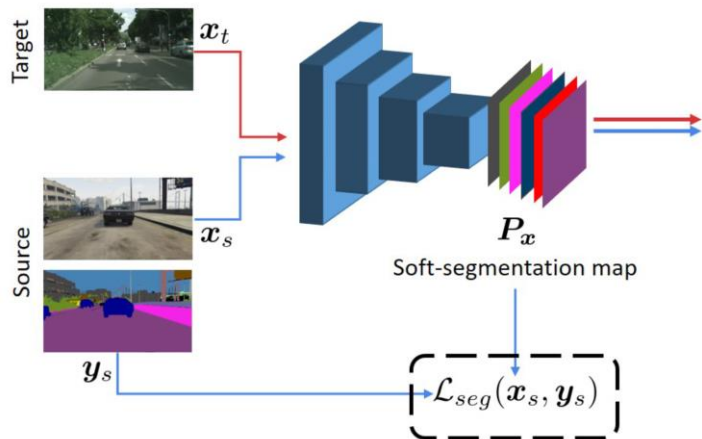
It relaxes the class prior constraint

ℓ_1 -normalized histogram (source)

Estimated size on the prediction

Inequality constraints

Information (proportion) is given as a prior



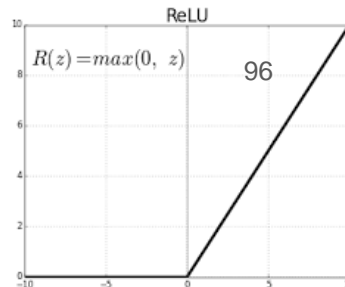
Class-ratio priors

$$\mathcal{L}_{cp}(x_t) = \sum_{c=1}^C \max(0, \mu p_s^{(c)} - \mathbb{E}_c(P_{x_t}^{(c)}))$$

It relaxes the class prior constraint

Estimated size on the prediction

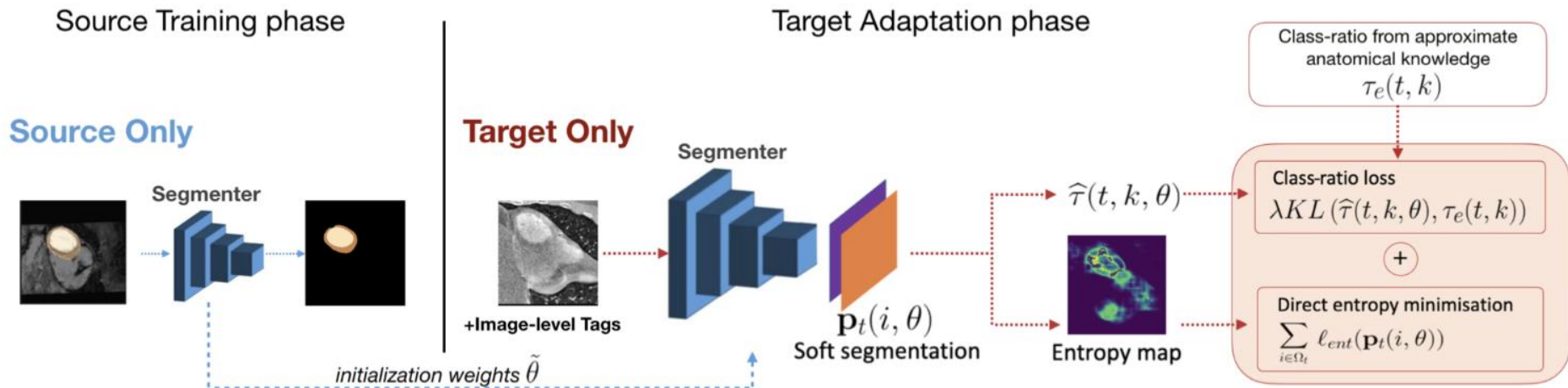
ℓ_1 -normalized histogram (source)



Inequality constraints

KL divergence

Source-free Domain Adaptation



Inequality constraints

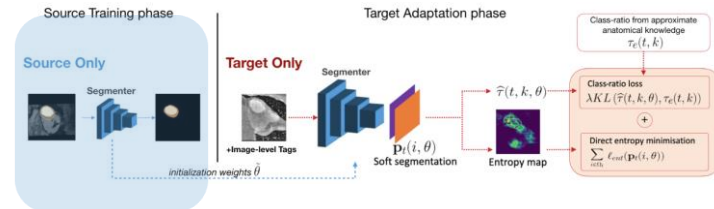
KL divergence

Source-free: no access to source data when adapting

1-Train the network on the source domain

$$\min_{\theta} \sum_{p \in \mathcal{L}} l(\mathbf{y}^p, \mathbf{s}_{\theta}^p)$$

Set of labeled
SOURCE pixels



Inequality constraints

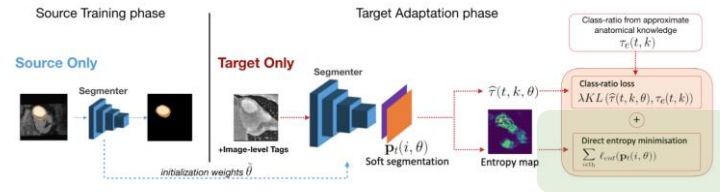
KL divergence

Source-free: no access to source data when adapting

2-Adapt the model without accessing the source data

$$\mathcal{L}_{\mathcal{H}} = - \sum_{p \in \mathcal{T}} \sum_k \mathbf{s}_{\theta}^{p,k} \log \mathbf{s}_{\theta}^{p,k} + \mathcal{D}_{KL}(\hat{\tau}, \tau_e)$$

Minimize entropy on predicted
TARGET pixels

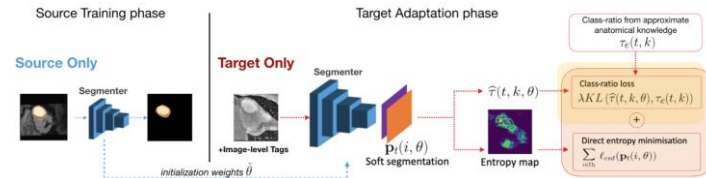


Inequality constraints

KL divergence

Source-free: no access to source data when adapting

2-Adapt the model without accessing the source data



$$\mathcal{L}_{\mathcal{H}} = - \sum_{p \in \mathcal{T}} \sum_k \mathbf{s}_{\theta}^{p,k} \log \mathbf{s}_{\theta}^{p,k} + \mathcal{D}_{KL}(\hat{\tau}, \tau_e)$$

Minimize entropy on predicted TARGET pixels

Size regularizer

Estimated size by an auxiliary network trained on the source

$$\hat{\tau}(t, k, \theta) = \frac{1}{|\Omega_t|} \sum_{i \in \Omega_t} \mathbf{s}_{\theta}^{i,k}$$

Computed size from the segmentation of the target image

Inequality constraints

L2 Penalty

But we can do more than simply the size

Shape moment $\mu_{p,q}^{(k)}(s_{\theta}) := \sum_{i \in \Omega} s_{\theta}^{(i,k)} x_{(i)}^p y_{(i)}^q,$

Central moment $\bar{\mu}_{p,q}^{(k)} := \sum_{i \in \Omega} s_{\theta}^{(i,k)} \left(x_{(i)} - \frac{\mu_{1,0}^{(k)}}{\mu_{0,0}^{(k)}} \right)^p \left(y_{(i)} - \frac{\mu_{0,1}^{(k)}}{\mu_{0,0}^{(k)}} \right)^q .$

Inequality constraints

L2 Penalty

But we can do more than simply the size

From shape and central moment

Volume

$$\mathfrak{V}^{(k)}(s_{\theta}) := \mu_{0,0}^{(k)}(s_{\theta}).$$

Centroid

$$\mathfrak{C}^{(k)}(s_{\theta}) := \left(\frac{\mu_{1,0}^{(k)}(s_{\theta})}{\mu_{0,0}^{(k)}(s_{\theta})}, \frac{\mu_{0,1}^{(k)}(s_{\theta})}{\mu_{0,0}^{(k)}(s_{\theta})} \right).$$

Length

$$\mathfrak{L}^{(k)}(s_{\theta}) := \sum_{i,j \in \mathcal{G}_{\Omega}} |s_{\theta}^{(i,k)} - s_{\theta}^{(j,k)}| L_{\Omega,i,j}.$$

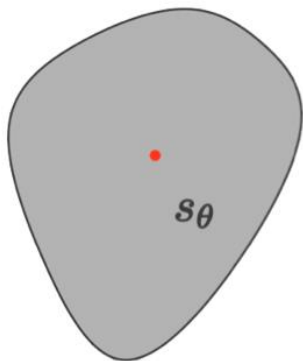
Laplacian

Inequality constraints

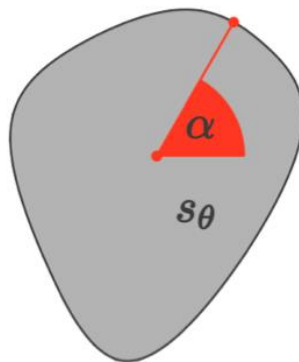
L2 Penalty

But we can do more than simply the size

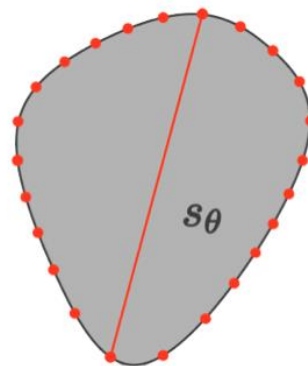
From shape and central moment



(a) Centroid $\mathfrak{C}(s_\theta)$



(b) Radius $\hat{\mathfrak{R}}_\beta(s_\theta, \alpha)$



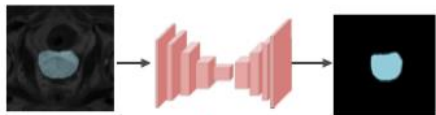
(c) Diameter $\mathfrak{D}(s_\theta)$

Inequality constraints

L2 Penalty

Test-Time Adaptation (TTA)

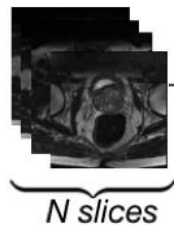
Source Training



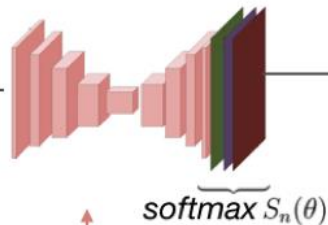
initialization weights $\tilde{\theta}$

Test-Time Adaptation with Single Target Image

One Target Subject



N slices



$\text{softmax } S_n(\theta)$



$\mathcal{M}^{(k)}(S_n(\theta))$

$\bar{\mathcal{M}}^{(k)}$

Shape Moment Estimation

Entropy minimization

$$\sum_{i \in \Omega_n} \ell_{ent}(s_n(i, \theta))$$

+

$$\text{Moment Matching}$$
$$\text{KL}(\mathcal{R}(S_n(\theta)), \bar{\mathcal{R}})$$

+

$$\lambda \mathcal{F}(\mathcal{M}^{(k)}(S_n(\theta)), \bar{\mathcal{M}}^{(k)})$$

Take-home message

- **Imposing constraints helps** weakly-supervised segmentation learning by **restricting plausible segmentations** on weakly labeled and unlabeled images
- **Few constraints have been explored** under low-labeled data regime
- Room for improvement (many opportunities beyond weakly supervised segmentation)

Thank you!