Cardiac C-arm computed tomography using a 3D + time ROI reconstruction method with spatial and temporal regularization

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Purpose: Reconstruction of the beating heart in 3D + time in the catheter laboratory using only the available C-arm system would improve diagnosis, guidance, device sizing, and outcome control for intracardiac interventions, e.g., electrophysiology, valvular disease treatment, structural or congenital heart disease. To obtain such a reconstruction, the patient’s electrocardiogram (ECG) must be recorded during the acquisition and used in the reconstruction. In this paper, the authors present a 4D reconstruction method aiming to reconstruct the heart from a single sweep 10 s acquisition.

Methods: The authors introduce the 4D RecOnstructiOn using Spatial and TEmporal Regularization (short 4D ROOSTER) method, which reconstructs all cardiac phases at once, as a 3D + time volume. The algorithm alternates between a reconstruction step based on conjugate gradient and four regularization steps: enforcing positivity, averaging along time outside a motion mask that contains the heart and vessels, 3D spatial total variation minimization, and 1D temporal total variation minimization.

Results: 4D ROOSTER recovers the different temporal representations of a moving Shepp and Logan phantom, and outperforms both ECG-gated simultaneous algebraic reconstruction technique and prior image constrained compressed sensing on a clinical case. It generates 3D + time reconstructions with sharp edges which can be used, for example, to estimate the patient’s left ventricular ejection fraction.

Conclusions: 4D ROOSTER can be applied for human cardiac C-arm CT, and potentially in other dynamic tomography areas. It can easily be adapted to other problems as regularization is decoupled from projection and back projection. © 2014 American Association of Physicists in Medicine.

Key words: C-arm, computed tomography, heart, ROOSTER, compressed sensing

1. INTRODUCTION

Reconstruction of the beating heart in 3D + time in the catheter laboratory using only the available C-arm system would improve diagnosis, guidance, device sizing, and outcome control for intracardiac interventions, e.g., electrophysiology, valvular disease treatment, structural or congenital heart disease. However, the design of a suitable acquisition protocol and of the corresponding 3D + time reconstruction method is still a challenging problem. A high resolution and almost artifact-free 3D reconstruction can be obtained by performing an ungated Feldkamp (FDK) reconstruction, but the resulting volume is static and moving organs are blurred. The goal is to reconstruct a 3D + time sequence of volumes in which the motion is rendered accurately. For the acquisition part, the C-arm rotates around the patient while acquiring projections and recording the patient’s electrocardiogram. The length of the acquisition, the number
of projections to be acquired, and whether the C-arm should perform a single or multiple sweeps are still open questions, since there is no standard protocol for cardiac C-arm imaging today. Optimized cardiac C-arm computed tomography (cardiac C-arm CT) acquisition protocols for cardiac imaging prior to transcatheter aortic valve implantation (TAVI) have been presented. The parameters to optimize include rotation speed, number of rotations, number of projections, electrical settings of the x-ray tube, amount, rate and location of contrast agent injection, and delay between injection and acquisition.

The acquisition protocol used in this paper is a tradeoff between clinical, mechanical, and algorithmic constraints encountered in the course of our study. The main clinical constraint is that the whole acquisition has to be performed during a single breath hold to avoid breathing motion. As patients with cardiac or vascular diseases often have reduced breathing capabilities, and must start holding their breath before and stop after the acquisition, acquisition itself should not last longer than 10 s. The amount of contrast agent should also be limited, as it adds up to the contrast injected during the intervention. This second constraint also pledges for a short acquisition. On the other hand, because of mechanical constraints, C-arms rotate much slower than CT scanners and short acquisition.

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Therefore, the projections must be sorted and discarded during the intervention. This second constraint also pledges for a short acquisition. On the other hand, because of mechanical constraints, C-arms rotate much slower than CT scanners and cannot perform step and shoot acquisitions. Current C-arms perform a 200° rotation in a minimum of 3–5 s, which implies that a cardiac acquisition always covers several cardiac cycles. Therefore, the projections must be sorted and discarded. In tomography with few views, the better the projections cover the angular range around the object, the better is the reconstruction. In cardiac C-arm CT, electrocardiogram gating (ECG gating) results in a few clusters of consecutive projections (one cluster per heart beat), separated by empty angular regions (where other cardiac phases were acquired). To obtain the best possible angular coverage, it is desirable to have as many heart cycles acquired during the C-arm rotation as possible, and thus a long acquisition time. Therefore, the duration of the acquisition must be the result of a tradeoff between the image quality and the safety and comfort of the patient. The 4D reconstruction method presented in this paper targets a cardiac reconstruction from a single sweep 10 s acquisition.

In the last decade, several classes of 4D reconstruction methods have been proposed. Motion compensated reconstructions attempt to estimate the motion of the heart, and take it into account in the reconstruction process. They depend on the accuracy of the motion estimation, and as of now have not proven to be efficient on single sweep cardiac C-arm CT data. Methods based on compressed sensing, and in particular the prior image constrained compressed sensing method (short PICCS), which is the current state of the art in cardiac C-arm CT, compensate the loss of information caused by ECG-gating by introducing sparsity-based regularization priors in the solution. Methods attempt to reconstruct each cardiac phase individually, and do not take advantage of the strong similarity between successive cardiac phases. By imposing that each cardiac phase be close to a single “prior” image, PICCS indirectly enforces similarity between cardiac phases, but this similarity is not stronger between successive phases (e.g., midsystole and end systole) than between distant phases (e.g., end systole and end diastole), which would be a desirable property.

Recently, new algorithms introducing temporal regularization between consecutive cardiac phases have been proposed. The additional constraint introduced by temporal regularization restricts the space of admissible solutions to the temporally consistent ones. As such, it allows the reconstruction algorithm to better exploit the data. A 4D-regularized reconstruction method, based on temporal non-local means (TNLM), was proposed by Jia et al. Langet et al. have proposed a 3D + time reconstruction algorithm for injected arteries, which is a specific problem leading to specialized algorithms. Momey et al. proposed a 2D + time reconstruction method based on total variation (short TV) regularization, and later extended it to 3D + time. In the present paper, we introduce a new 3D + time reconstruction method, which we name 4D ROOSTER (for 4D RecOnstruction using Spatial and TEmporal Regularization), by starting from ECG-gated simultaneous algebraic reconstruction technique [SART (Ref. 21)] and adding regularization constraints one by one: first positivity, then restriction of motion to a region of interest (ROI) containing the heart and the vessels, and then spatial and temporal total variation minimization.

It is shown that the proposed method outperforms PICCS both on simulated and real data, and can successfully reconstruct a 3D + time sequence from a 10 s single sweep human cardiac C-arm CT acquisition.

2. MATERIALS AND METHODS

2.A. The 4D ROOSTER method

The 4D ROOSTER method derives from the desired properties of the solution to the problem:

- (P1) Forward projection through the reconstructed 4D volume should match the measured projection data as accurately as possible.
- (P2) All voxels should have non-negative attenuation.
- (P3) No movement should occur outside the heart and the vascular system.
- (P4) Each volume of the sequence should have some kind of spatial regularity, i.e., be spatially smooth except on the edges of the organs and be free of streak artifacts.
- (P5) Consecutive volumes in the sequence should be similar.

Before describing the details of the reconstruction method, let us express these requirements in a more formal way. Let \( f_1, f_2, \ldots, f_N \) be 3D volumes, each one representing a single cardiac phase, and let \( f = ( f_1 : \ldots : f_N ) \) be a 4D volume. Cardiac phases are often expressed in percentage of the cardiac cycle: here the volume \( f_1 \) represents the cardiac phase \( t = (i/N) \). The \( f_1, f_2, \ldots, f_N \) are column vectors of size \( M \), where \( M \) is
the number of voxels in a 3D volume. Thus \( f \) is a column vector of size \( MN \). For clarity, the intensity at a voxel \((x, y, z)\) in each volume \( f_i \) will also be denoted \( f_i(x, y, z) \). \( p_0 \) is the real projection measured at angle \( \theta \), and \( R_0 \) a ray-driven forward projection operator (also called x-ray transform) for angle \( \theta \). Note that \( R_0 \) is an approximation of the real x-ray transform, and does not take into account scattering, beam hardening, detector cross talk, or gain effects. Corrections for these effects are applied by preprocessing the projections, and the \( p_0 \) are in fact the corrected projections. The \( p_0 \) are column vectors of size \( P \), where \( P \) is the number of pixels in a projection, and the \( R_0 \) are matrices with \( P \) lines and \( M \) columns.

\( S_0 \) is an interpolation operator which, from the 3D + time sequence, estimates the 3D volume through which projection \( \theta \) has been acquired. It is defined as follows: from the ECG, we know in which phase \( t(\theta) \) the patient’s heart was when projection \( p_0 \) was acquired. The forward projection at angle \( \theta \), which will be compared to the measured projection \( p_0 \), should be computed through an estimate of the patient’s thorax at \( t(\theta) \), which by a slight abuse in notation we will denote \( f_0(\theta) \), and which is obtained by interpolating between some of the volumes \( f_i \). If \( N = 10 \), \( f_1 \) is the volume at 10% of the cardiac cycle, \( f_2 \) the volume at 20%, and so on. With \( t(\theta) = 87\% \), the interpolated volume would be \( S_0 f = f_0(\theta) = 0.3 f_8 + 0.7 f_9 \). In this example, and in the implementation we used, \( S_0 \) is a linear interpolator. However, other interpolation methods could be tested, like nearest neighbors or splines. Note that \( S_0 \) is a huge matrix with \( M \) lines and \( MN \) columns, but is not explicitly computed in practice.

It is assumed that a ROI of the heart and main vessels is available (for instance, derived from a rough segmentation of the ungated FDK reconstruction), from which the operator \( H \) is derived. \( H \) is a binary diagonal matrix with \( M \) lines, which “selects” those voxels in a volume that are located outside the heart. As a result, for any \( i \),

\[
\begin{align*}
H f_i(x, y, z) &= f_i(x, y, z) \text{ if } (x, y, z) \text{ is outside the heart,} \\
H f_i(x, y, z) &= 0 \text{ if } (x, y, z) \text{ is inside the heart.}
\end{align*}
\]

(1)

Multiplication by the matrix \( H \) is the linear algebra equivalent of multiplying by a motion mask. The mask’s edges are sharp, which can lead to artifacts at its borders. The spatial regularity constraint seems to be sufficient to mitigate these artifacts in the cases we have studied. Should the need arise, changing to a mask with soft edges would only require slight modifications.

Now, let us formalize our five requirements on the solution:

- \((P_1)\), taken in the least squares sense, means that

\[
\sum_i \left\| (R_0 S_0 f - p_0) \right\|^2_2 \text{ should be small.}
\]

- \((P_2)\) is equivalent to imposing that \( \forall i \) and \( \forall (x, y, z), f_i(x, y, z) \geq 0. \)

- \((P_3)\) means that for any \( i \) and \( j \), \( H f_i = H f_j. \)

- \((P_4)\) can be enforced by numerous regularization methods. We chose to express it as a constraint on 3D total variation on each volume \( f_i \). Total variation is defined by

\[
TV(f) = \| \nabla f \|_1 = \sqrt{(\nabla_x f)^2 + (\nabla_y f)^2 + (\nabla_z f)^2}.
\]

(2)

The \( \nabla \) operator accounts for the spacing between voxels, which can vary from one direction to another.

- \((P_5)\) can also be expressed as a constraint on total variation, although this time a one-dimension total variation has to be used. The following constraint is derived:

\[
TV(f) = \| \nabla f \|_1
\]

(3)

should be small. The discrete gradient along time is computed with a circular boundary condition because the sequence of volumes is meant to be cyclic.

The algorithm we propose in order to derive a 3D + time sequence \( f \) that has the aforementioned properties consists in the following steps:

- Start from \( k = 0 \) and \( f^{(k)} = 0 \)
- Until \( k = k_{\text{max}} \)
  - Compute \( \hat{f}^{(k+1)} = \arg \min_f \sum_i \| (R_0 S_0 f - p_0) \|^2_2 \) by a conjugate gradient descent initialized with \( f^{(k)} \)
  - Set all negative voxels to zero
  - In each \( f_i \), replace the area outside the heart by its temporal mean \( \frac{1}{T} \sum_j H \hat{f}_j \)
  - For each \( \hat{f}_i \), compute \( \hat{g}_i = \arg \min_g \lambda_{\text{space}} \| g - \hat{f}_i \|^2_2 + TV(g) \) using a gradient descent, as described by Chan, and concatenate the \( \hat{g}_i \) into \( \hat{g} \)
  - Compute \( f^{(k+1)} = \arg \min_f \| f - \hat{g} \|^2_2 + TV(f) \) by the same method
  - \( k = k + 1 \)

The parameters of the algorithm are the number of main loop iterations \( k_{\text{max}} \) (for all results presented throughout the paper, except those used for Fig. 6, \( k_{\text{max}} = 30 \)), the number of nested conjugate gradient iterations (set to 4 throughout the paper), the number of iterations used in the TV minimization, the parameters \( \lambda_{\text{space}} \) and \( \lambda_{\text{time}} \), which are data attachment coefficients for TV minimization, and the steps of the gradient descents.

In order to account for the data truncation when working on real cardiac C-arm CT data, the reconstruction volume was chosen slightly larger than the field of view.\(^{23,24}\)

In order to demonstrate the impact of each individual regularization step, modified versions of this method have been tested. Each regularization step has been turned off while all others were turned on. The results are presented in Sec. 3.

2.B. The PICCS method

The PICCS method is based on minimizing the following cost function:

\[
\text{Cost}(f) = G \| (R f - p) \|^2_2 + \alpha TV(f - f^*) \\
+ (1 - \alpha) TV(f)
\]

(4)
where $f$ is the 3D volume being reconstructed, $f^*$ is a prior image close to the solution we seek (usually the FDK reconstruction using all projections,\textsuperscript{3} also called “ungated FDK”), $\text{TV}$ is the total variation operator, $R$ is the x-ray transform operator, $p$ is the set of measured projections, and $G$ is an ECG-gating operator. $G$ is diagonal and, in our case, binary (ECG-gating can be performed with various window shapes,\textsuperscript{25} and $G$ is not binary if the chosen shape is not a gate).

There are several ways to estimate a solution $f$ that minimizes this cost function. In this paper, we have implemented a method very close to the one described by Chen et al.,\textsuperscript{15} in which it was proposed to alternate between iterations of ECG-gated ART,\textsuperscript{25, 26} to minimize the data attachment term, and steepest descent iterations, to minimize the rest of the cost function, i.e., $(1 - \alpha)\text{TV}(f - f^*) + \alpha \text{TV}(f)$. We used SART (Ref. 21) instead of ART, and turned the cost function minimized by the steepest descent iterations into $\lambda \| f - f_{\text{SART}} \|_2^2 + \alpha \text{TV}(f - f^*) + (1 - \alpha)\text{TV}(f)$, where $f_{\text{SART}}$ is the volume returned by the SART step. Adding such a data-attachment term avoids blurring the edges of the reconstructed volume when $\alpha \to 0$.

2.C. Implementation

Both PICCS and 4D ROOSTER have been implemented using the Reconstruction ToolKit (short RTK), a library based on the Insight ToolKit (short ITK).\textsuperscript{27} Data truncation was handled the same way in both 4D ROOSTER and PICCS: the reconstruction volume was set larger than the field of view. RTK supports CUDA, thus 4D ROOSTER and PICCS were implemented mostly on GPU. Reconstructions were performed on a 2.8 GHz Intel Xeon with 6 cores, equipped with an nVidia Tesla C2070.

With our implementation of PICCS, it takes about 15 min to reconstruct a single phase, meaning a single $284 \times 284 \times 284$ voxels volume, from about 61 projections (20% of 308 projections) of 512 × 396 pixels each.

With our implementation of 4D ROOSTER, it takes about 90 min to reconstruct ten phases, meaning a $284 \times 216 \times 284 \times 10$ voxels 3D + time sequence, from 308 projections of 512 × 396 pixels each.

2.D. Simulations

4D ROOSTER is demonstrated on a 3D Shepp and Logan phantom, in which the size of one of the ellipses varies periodically to simulate a beating heart. The simulated acquisition geometry was chosen close to that of the real acquisition (308 projections regularly distributed over a 205° trajectory, acquired over 10 s, and 60 beats/min). The instant when the beating ellipse is the smallest is called “end systole,” and the instant when it is the largest is called “end diastole.” The ground truth images for end systole and end diastole are displayed in Fig. 1. The region in which movement is allowed, and in which the local root mean square error (RMSE) is computed (see Table II), is delineated by a circle on the end diastolic image. It has been chosen a little larger than the beating ellipse in end diastole to illustrate the fact that the segmentation of the heart can be rough and include a margin of error.

2.E. Clinical data

The clinical datasets used in this paper were acquired at the Division of Cardiology, University of Colorado, Denver, USA. The C-arm CT acquisition was performed on an Allura XPer FD20 (Philips Healthcare, Best, The Netherlands). 308 projections were acquired in 10.3 s over a 205° circular arc trajectory, during a single breath hold. Each projection contains 1024 × 792 pixels of 0.37 × 0.37 mm (note that for this work the projections have been downsampled by a factor of 2 in both directions). The projections are corrected for detector cross talk, pixel gain, beam hardening, and scatter.\textsuperscript{28, 29} The tube was set to 83 kV, 650 mA, 10 ms per projection. The CTDI dose delivered to the patient is 4.3 mSv.\textsuperscript{30} Patient 1 had a heart rate of 90 beats/min (which is a favorable configuration, see Sec. 1), and patient 2 a heart rate of 60 bpm (which is the target). More details on the acquisition protocol can be found in Schwartz et al.\textsuperscript{2} Projections 50 and 250 for both patients are displayed in Fig. 2.

As can be observed in projection 50, at its initial concentration, before it gets diluted into blood, the contrast medium has

![Fig. 1. Ground truth of the Shepp and Logan phantom with a beating ellipse, in end systole (on the left) and end diastole (on the right). The region in which movement is allowed, and in which local RMSE is computed, is delineated by a circle on the end diastolic image.](Image 321x94 to 561x279)

![Fig. 2. Projection 50 out of 308 (left column) and 250 out of 308 (right column) of the injected C-arm CT scan performed on patient 1 (top row) and patient 2 (bottom row). The arrows point out the highly concentrated contrast agent in the superior vena cava in projection 50.](Image 381x657 to 501x737)
a high absorption. This creates hyperattenuation artifacts in the reconstructed volumes, just like metallic objects would do.

Moreover, the contrast medium flows in the vascular system. Its distribution in space can be considered periodic inside the heart if the injection is performed carefully, but is never periodic outside the heart. Therefore, projections acquired at the same ECG-phase can represent different volumes: the flow of the contrast medium makes the projection data inconsistent. Cardiac reconstruction algorithms are nevertheless built on the assumption that the attenuation of a voxel depends only on its position in space and on the ECG-phase considered, or in other words, that the imaged object’s attenuation varies periodically like the ECG.

Another source of error is the truncation of data: patients are typically larger than the field of view, so that certain parts of their chest are visible on some projections and not on the others. This also makes the projection dataset inconsistent. In order to mitigate the artifacts caused by truncation, the reconstructed volume has been slightly extended outside the field of view.24

2.F. Quantitative evaluation of sharpness

Two methods were used to quantitatively assess the sharpness of the reconstructed clinical data:

- Kriminski’s blur criterion,31 based on the work of Boykov et al.,32,33 which consists in creating a graph from the image, performing a graph cut segmentation, and using the maximum flow (or equivalently the minimal cut weight) as a measure of blur, as performed in Rit et al.23
- Contrast to noise ratio (CNR).

Kriminski’s method provides a measure of blur derived from a graph cut segmentation. It makes particular sense in our case to introduce a segmentation-based criterion since one of the main goals of the cardiac reconstruction we are targeting is to segment the blood in the left ventricle, e.g., to compute the left ventricular ejection fraction. Kriminski’s blur criterion requires only one parameter, which can roughly be interpreted as an intensity threshold and was tuned manually for each reconstructed image in order to obtain the best possible segmentation.

CNR does not exactly measure sharpness, but it gives an indication of how distinguishable from one another two adjacent regions are. It was computed as

\[
\text{CNR} = \frac{|M_{\text{blood}} - M_{\text{muscle}}|}{\sigma_{\text{muscle}}},
\]

where \(M_{\text{blood}}\) and \(M_{\text{muscle}}\) are the mean attenuations in the blood and muscle ROIs, respectively, and \(\sigma_{\text{muscle}}\) is the standard deviation in the muscle ROI.

Figure 3 shows the subimage used for the max flow measurement, and the ROIs used for the CNR measurement, on both patients.

3. RESULTS

3.A. Simulations on a modified Shepp and Logan phantom: From ECG-gated SART to 4D ROOSTER

The 4D ROOSTER method is introduced here by going back to ECG-gated SART, and modifying it step by step to obtain 4D ROOSTER. Reconstructions of the modified Shepp and Logan phantom are shown in Figs. 4 and 5, and the reconstruction parameters for ECG-gated SART and 4D ROOSTER are listed in Table I.

In Fig. 4, all reconstructions are initialized with a zero volume. In Fig. 5, the algorithms are initialized with the ungated FDK reconstruction. In both figures, the top line contains the reconstructions of the systolic phase, the bottom lines the reconstructions of the diastolic phase. From left to right, the algorithms used are the following:

- ECG-gated SART;
- 4D reconstruction by conjugate gradient without any regularization (\(P_1\));
- 4D reconstruction by conjugate gradient alternated with positivity enforcement (\(P_1 + P_2\));
- 4D reconstruction by conjugate gradient, alternated with positivity enforcement and averaging along time outside the heart (\(P_1 + P_2 + P_3\));
- 4D reconstruction by conjugate gradient, alternated with positivity enforcement, averaging along time outside the heart and minimization of spatial TV (\(P_1 + P_2 + P_3 + P_4\));
- 4D ROOSTER as described in Sec. 2.A (\(P_1 + P_2 + P_3 + P_4 + P_5\)).

Figures 4 and 5 both show that each regularization step brings some improvement, either by reducing the impact of artifacts, sharpening the borders of the beating ellipse or enforcing smoothness in homogeneous regions. The comparison
between Figures 4 and 5 also reveals that ECG-gated SART is much more dependent on initialization than 4D ROOSTER is.

A numerical evaluation of the results presented in Figs. 4 and 5 was performed. The parameters retained are the RMSE with respect to the 4D phantom in the whole 4D sequence, and the RMSE in the region where movement can occur (local RMSE) for the 4D phantom. These values are shown in Table II and confirm the gradual improvement brought by adding each regularization step, which can be appreciated by visual evaluation of Figs. 4 and 5.

Table II shows a reduction of the RMSE and the RMSE in the motion mask when the various regularization steps are added.

Figure 6 shows the evolution of RMSE during the 4D ROOSTER reconstructions of the moving Shepp and Logan phantom. It constitutes a numerical validation of the
TABLE I. Parameters used for the reconstructions of the beating Shepp and Logan with ECG-gated SART and 4D ROOSTER.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>SART</th>
<th>4D ROOSTER</th>
</tr>
</thead>
<tbody>
<tr>
<td>Size (in voxels)</td>
<td>$256 \times 256 \times 256$</td>
<td>$256 \times 256 \times 256$</td>
</tr>
<tr>
<td>Voxel spacing (in mm)</td>
<td>$1 \times 1 \times 1$</td>
<td>$1 \times 1 \times 1$</td>
</tr>
<tr>
<td>Main loop iterations</td>
<td>100</td>
<td>30</td>
</tr>
<tr>
<td>SART-specific parameters</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SART relaxation parameter</td>
<td>0.5</td>
<td></td>
</tr>
<tr>
<td>Gating window width (% of cardiac cycle)</td>
<td>20</td>
<td></td>
</tr>
<tr>
<td>4D ROOSTER-specific parameters</td>
<td></td>
<td></td>
</tr>
<tr>
<td>lambda_space</td>
<td>100</td>
<td></td>
</tr>
<tr>
<td>lambda_time</td>
<td>100</td>
<td></td>
</tr>
<tr>
<td>Nested iterations for spatial TV</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>Nested iterations for temporal TV</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>Gradient descent step for spatial TV</td>
<td>0.001</td>
<td></td>
</tr>
<tr>
<td>Gradient descent step for temporal TV</td>
<td>0.001</td>
<td></td>
</tr>
</tbody>
</table>

Convergence of 4D ROOSTER, for which we give no formal proof in this paper. More details on convergence can be found in Sec. 4.B. It also highlights the benefit of initializing 4D ROOSTER with the ungated FDK image. In the rest of the paper, 4D ROOSTER has been configured to perform 30 iterations, which in practice seems sufficient, and to start from the ungated FDK reconstruction.

We present in Fig. 7 the absolute value of the difference between the first and second instants of the cardiac cycle (10% and 20% of the cardiac cycle, respectively) for the ECG-gated SART (on the left) and 4D ROOSTER (on the right) reconstructions initialized with ungated FDK. We have zoomed on the region where movement occurs (the ROI is delineated by a circle in Fig. 7). The slice considered is the same as in Figs. 4 and 5. Both the background and the inside of the ROI appear corrupted by temporally moving artifacts in the case of ECG-gated SART, while no such artifacts are present in the background and very little in the ROI on 4D ROOSTER results. It can also be observed that the ring corresponding to the beating ellipse is sharper and more contrasted on the 4D ROOSTER result.

TABLE II. Root mean square error ECG-gated SART, 4D ROOSTER, and all intermediate reconstruction methods with partial regularization.

<table>
<thead>
<tr>
<th></th>
<th>Initialization: zero</th>
<th>Initialization: ungated FDK</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>RMSE</td>
<td>RMSE in ROI</td>
</tr>
<tr>
<td>ECG-gated SART</td>
<td>0.0954</td>
<td>0.0319</td>
</tr>
<tr>
<td>4D CG</td>
<td>0.1134</td>
<td>0.0345</td>
</tr>
<tr>
<td>4D CG + positivity</td>
<td>0.0698</td>
<td>0.0247</td>
</tr>
<tr>
<td>4D CG + positivity + motion mask</td>
<td>0.0387</td>
<td>0.0168</td>
</tr>
<tr>
<td>4D CG + positivity + motion mask + spatial TV</td>
<td>0.0365</td>
<td>0.0122</td>
</tr>
<tr>
<td>4D ROOSTER</td>
<td>0.0363</td>
<td>0.0113</td>
</tr>
</tbody>
</table>

3.B. Clinical results: Comparison with ECG-gated SART and PICCS

In this section, reconstruction results obtained with ECG-gated SART, PICCS, and 4D ROOSTER on two clinical cases are presented. The results were not converted to Hounsfield. 
TABLE III. Parameters used for the reconstructions of the clinical case with ECG-gated SART, PICCS, and 4D ROOSTER.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>SART</th>
<th>PICCS</th>
<th>4D ROOSTER</th>
</tr>
</thead>
<tbody>
<tr>
<td>Size (in voxels)</td>
<td>$284 \times 216 \times 284$</td>
<td>$284 \times 216 \times 284$</td>
<td>$284 \times 216 \times 284$</td>
</tr>
<tr>
<td>Voxel spacing (in mm)</td>
<td>$1 \times 1 \times 1$</td>
<td>$1 \times 1 \times 1$</td>
<td>$1 \times 1 \times 1$</td>
</tr>
<tr>
<td>Main loop iterations</td>
<td>100</td>
<td>30</td>
<td>30</td>
</tr>
<tr>
<td>SART-specific parameters</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SART relaxation parameter</td>
<td>0.5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Gating window width (% of cardiac cycle)</td>
<td>20</td>
<td></td>
<td></td>
</tr>
<tr>
<td>PICCS-specific parameters</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Alpha</td>
<td>0.5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Lambda</td>
<td>500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SART relaxation parameter</td>
<td>0.5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Nested gradient descent iterations</td>
<td>20</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Gradient descent step</td>
<td>0.002</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Gating window width (% of cardiac cycle)</td>
<td>20</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4D ROOSTER-specific parameters</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>lambda_space</td>
<td>10000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>lambda_time</td>
<td>1000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Nested iterations for spatial TV</td>
<td>10</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Nested iterations for temporal TV</td>
<td>10</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Gradient descent step for spatial TV</td>
<td>0.0002</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Gradient descent step for temporal TV</td>
<td>0.0002</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

units: attenuations are expressed in $\text{mm}^{-1}$. The parameters used for the reconstructions of this section are listed in Table III.

Figure 8 shows reconstructions of the end systolic and end diastolic phases of the first patient’s heart, on a long axis cut of the left ventricle.

Figure 9 shows the reconstructions of the end systolic and end diastolic phases of the first patient’s heart, on a short axis cut. In both Figs. 8 and 9, the 4D ROOSTER results are sharper than the PICCS ones, and far less noisy than the ECG-gated SART results. The border between the endocardium and the interior of the left ventricle, pointed out by an arrow, is easy to identify on the 4D ROOSTER results while it is hard to determine with precision on the PICCS or SART results.

In the PICCS reconstructions, some streak artifacts remain and cause variations of the attenuation in regions that should be static. They can be observed in Fig. 8, in the top left corner of the PICCS reconstructions, which differ a lot while they should not. However, our main objective is to obtain a good reconstruction inside the heart region. From this standpoint, Figure 10 is more relevant. It shows the difference between two consecutive cardiac phases for both PICCS and 4D ROOSTER, and highlights the temporal consistency of 4D ROOSTER reconstructions both outside and inside the heart.

Figures 11 and 12 show the reconstructions of the second patient, in long axis cut for Fig. 11 and in short axis cut for Fig. 12. Because patient 2 has a lower heart rhythm than patient 1, the undersampling problem is more acute, and the reconstructed images are less sharp. The arrow in Fig. 11 points a portion of the border between blood and myocardium where sharpness differs a lot between SART, PICCS, and ROOSTER results.

A quantitative evaluation of sharpness using the methods described in Sec. 2.F is presented in Table IV. SART reconstructions are noisier and blurrier than PICCS images, which in turn are noisier and blurrier than 4D ROOSTER reconstructions.

![Fig. 8. Long axis cuts of the left ventricle in ECG-gated SART, PICCS, and 4D ROOSTER reconstructions of patient 1. The display window is [0.018; 0.042].](image-url)
3.C. Impact of each regularization step

Understanding the practical impact of each regularization step on the final result is crucial to be able to fine-tune the parameters of the 4D ROOSTER algorithm. This section presents the results obtained with 4D ROOSTER on the clinical dataset when all regularization steps but one are active, so as to give some insight on the role of each step. Figure 13 shows that positivity enforcement has little impact in this case. However, it does not deteriorate the image, comes at a very small computational cost (see Table V), and as it can be seen in Fig. 4, it plays an important role when initializing with zero. Therefore, we recommend keeping this regularization step.
Table IV. Quantitative evaluation of sharpness in reconstructions of clinical cases.

<table>
<thead>
<tr>
<th>Patient</th>
<th>SART</th>
<th>PICCS</th>
<th>ROOSTER</th>
</tr>
</thead>
<tbody>
<tr>
<td>Blur criterion</td>
<td>13.7</td>
<td>10.8</td>
<td>7.8</td>
</tr>
<tr>
<td>CNR</td>
<td>1.33</td>
<td>3.3</td>
<td>4.47</td>
</tr>
</tbody>
</table>

The effect of spatial regularization is shown in Fig. 14. Minimizing the 3D total variation effectively removes high frequency noise and favors solutions with homogeneous regions separated by sharp edges.

Figure 15 highlights the role of averaging along time outside the motion mask and of minimizing temporal TV by displaying the difference image between two consecutive heart phases. Minimizing temporal TV seems to have a higher impact on image quality than averaging outside the motion mask, but both regularization steps appear complementary.

4. DISCUSSION AND CONCLUSION

4.A. Comparison with PICCS

The 4D ROOSTER method has been introduced and compared to PICCS on real human cardiac C-arm CT data. As PICCS is designed to reconstruct textured data, we have chosen to present comparisons between PICCS and 4D ROOSTER on the moving Shepp and Logan phantom, which would have been unfair to PICCS and irrelevant. The results obtained on real data confirm the superiority of 4D ROOSTER over PICCS. The main reasons why 4D ROOSTER achieves better results than PICCS are the following:

- It uses a motion mask to allow movement only where it is supposed to occur. This is a strong hypothesis, which considerably reduces the number of unknowns of the reconstruction problem.
- It uses regularization along time, which rules out many inconsistent solutions, and is also highly efficient in removing streak artifacts.

Table V. Computation time required for each step of the 4D ROOSTER method.

<table>
<thead>
<tr>
<th>Algorithm step</th>
<th>Computation time (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Conjugate gradient minimization of data attachment</td>
<td>110</td>
</tr>
<tr>
<td>Positivity enforcement</td>
<td>0.1</td>
</tr>
<tr>
<td>Temporal averaging outside heart ROI</td>
<td>14</td>
</tr>
<tr>
<td>Spatial TV minimization</td>
<td>14</td>
</tr>
<tr>
<td>Temporal TV minimization</td>
<td>30</td>
</tr>
</tbody>
</table>

A clinical study with more patients, and in particular patients with lower heart rates, is necessary to confirm the results of this comparison.

It could be argued that, with different parameters, it would have been possible to obtain better images using PICCS (potentially better than using 4D ROOSTER). There are indeed many parameters in both methods, and we cannot guarantee that the ones we chose are the best. For each method, the results presented in the paper are the best ones we were able to obtain, and the parameters used to obtain them are listed in Tables I and III.

4.B. Convergence of the 4D ROOSTER method

Unlike a large class of reconstruction methods based on compressed sensing, 7,14,20,34 4D ROOSTER does not consist in minimizing a cost function defined as the sum of a data-attachment term and one or more regularization terms. Instead, it alternates between several optimization goals. Similar methods include the adaptive steepest descent-projection onto convex sets (ASD-POCS) (Ref. 13) and some PICCS implementations, like the one we used. The proof of convergence for such an alternating algorithm is typically harder than for a method minimizing a single cost function.

This section provides the theoretical background to prove that if the algorithm has at least one fixed point, it converges to one of its fixed points. We do not prove here that such a fixed point does exist. Using the same notations as in Sec. 2.A, a few definitions from the theory of nonexpansive mappings are reminded:

- A mapping \( T: \mathbb{R}^{MN} \rightarrow \mathbb{R}^{MN} \) is nonexpansive if \( \forall x, y \in \mathbb{R}^{MN}, \|Tx - Ty\|_2 \leq \|x - y\|_2 \).
Comparison between 4D ROOSTER in the left column, 4D ROOSTER without motion mask [i.e., removing property (P3)] in the middle column and 4D ROOSTER without temporal regularization [i.e., removing property (P5)] in the right column. The top row shows the end-diastolic phase and the bottom row shows the absolute value of the difference between two consecutive cardiac phases. Even in large homogeneous areas where the attenuation should not change much over time, like inside the left ventricle near the base, important differences are noticeable between successive phases if temporal regularization is not applied. Averaging outside the motion mask also removes some of the high frequency noise. The display window is [0.017; 0.04] for the top row and [0; 0.005] for the bottom row.

- $T$ is strongly nonexpansive if $T$ is nonexpansive and whenever $(x_n)_n \in \mathbb{N}$ and $(y_n)_n \in \mathbb{N}$ are sequences in $\mathbb{R}^{MN}$ such that $(x_n - y_n)_n \in \mathbb{N}$ is bounded and $\|x_n - y_n\|_2 - \|Tx_n - Ty_n\|_2 \to 0$, it follows that $(x_n - y_n) - (Tx_n - Ty_n) \to 0$.
- $T$ is firmly nonexpansive if $\forall x, y \in \mathbb{R}^{MN}$, $\|Tx - Ty\|_2^2 \leq \langle Tx - Ty, x - y \rangle$.

All operators involved in 4D ROOSTER are strongly nonexpansive:
- In our problem, with enough iterations, conjugate gradient descent is strongly nonexpansive.
- Positivity enforcement is a projector onto a nonempty closed convex set, therefore it is firmly nonexpansive, and therefore strongly nonexpansive (see fact 4.2 of Bauschke et al.\textsuperscript{35}).
- It is easy to prove that averaging along time outside the motion mask is a firmly nonexpansive mapping.
- The spatial and temporal TV regularization operators are proximal mappings, therefore they are firmly nonexpansive,\textsuperscript{36} and therefore strongly nonexpansive.

As stated in fact 4.2 of Bauschke et al.,\textsuperscript{35} the composition of a finite number of strongly nonexpansive mappings is a strongly nonexpansive mapping. Thus, each iteration of the main loop of 4D ROOSTER amounts to applying a strongly nonexpansive mapping $T$ on the current 3D + time sequence $f_k$, such that $f_{k+1} = T(f_k)$. Applying the theorem reminded in fact 4.3 of Bauschke et al.,\textsuperscript{35} if $T$ has at least one fixed point, 4D ROOSTER converges to one of its fixed points.

### 4.C. Segmentation of the heart and vessels

The constraint that the sequence be static outside the heart and vessels reduces the number of unknowns by an order of magnitude, but assumes that a segmentation of the heart and vessels is available. For this paper the segmentation has been performed on the ungated FDK reconstruction using the semiautomatic segmentation tool LiveMorph.\textsuperscript{37} It could be replaced by a fully automatic method,\textsuperscript{2} especially because the segmentation used by 4D ROOSTER can be very rough, and can handle small segmentation errors.

### 4.D. Perspectives

Future work on the method includes the study of regularization methods other than total variation minimization, potentially better suited to textured data (e.g., wavelets, curvelets, nonlocal means, etc.). For the clinical part, 4D ROOSTER could be tested on—and maybe adapted to—specific applications like late enhancement cardiac C-arm CT for myocardial infarction imaging or cardiac imaging in children with congenital heart defect.

### 4.E. Conclusion

4D ROOSTER can be applied for single sweep human cardiac C-arm CT, and potentially other dynamic tomography areas. It can easily be adapted by modifying the regularization constraints, as regularization is decoupled from projection and back projection.

### ACKNOWLEDGMENT

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